
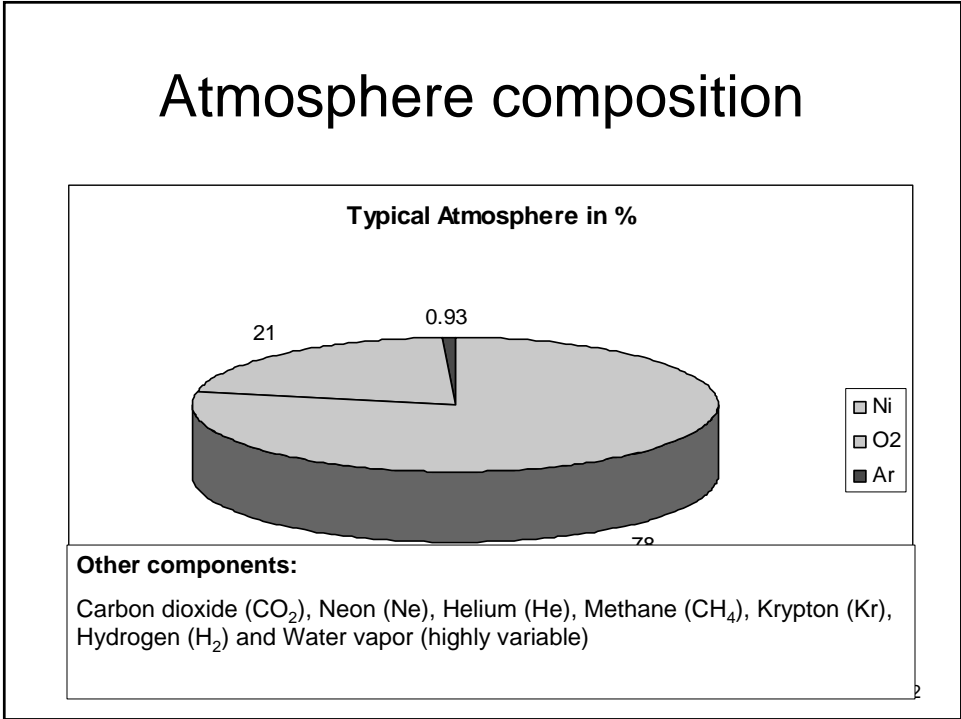


# Microwave Interactions with the Atmosphere

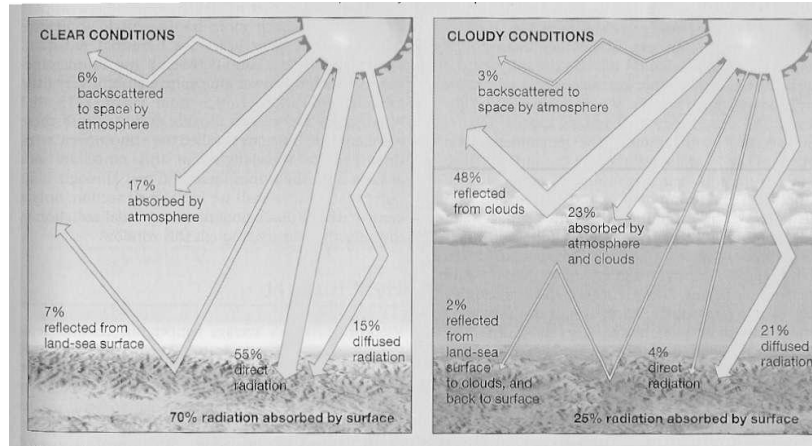
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## Atmospheric Constituents



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## Introduction

- Up to now, we have assumed lossless atm.
- For  $1 \text{ GHz} < f < 15 \text{ GHz}$  ~lossless
- For higher frequencies, =>absorption bands



- 22.235 GHz
- 183.3 GHz
- IR & visible



- 50-70GHz
- 118.7GHz
- IR & visible

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# Outline



I. The atmosphere: composition, profile

II. Gases: many molecules

1. *Shapes*( $G, VVW, L$ ): below 100GHz, up to 300GHz

e.g.  $H_2O, O_2$

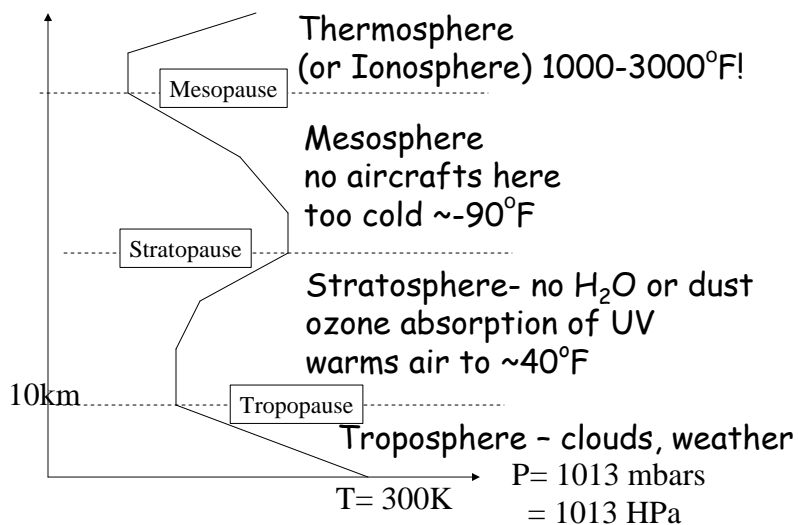
2. *Total Atmospheric*

Absorption  $\kappa_g$ , opacity  $\tau_\theta$ , and atm-losses  $L_\theta$

3.  $T_B$ : Downwelling Emission by Atmosphere

Sky Temp= cosmic + galaxy

# U.S. Standard Atmosphere



## Atmospheric Profiles

US Standard Atmosphere 1962

- Temperature

$$T(z) = \begin{cases} T_o - az & 0 \leq z \leq 11 \text{ km} \\ T_{(11)} & 11 \text{ km} \leq z \leq 20 \text{ km} \\ T_{(11)} + (z - 20) & 20 \text{ km} \leq z \leq 32 \text{ km} \end{cases}$$

- Density

$$\rho_{air}(z) = 1.225e^{-z/H_1} \quad \text{where } H_1 = 9.5 \text{ km density scale height}$$

or  $\rho_{air}(z) = 1.225e^{-z/7.3} [1 + 0.3 \sin(z/7.3)]$

- Pressure  $P = nRT/V = \rho_{air}RT/M$  or  $P_o e^{-z/H_3}$

where  $H_3 = 7.7 \text{ km}$  Pressure scale height

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## Water Vapor Profile

Depends on factors like weather, seasons, time of the day.

It's a function of air temperature.

- Cold air can't hold water
- Hot air can support higher humidities. ( $P$  dependence)

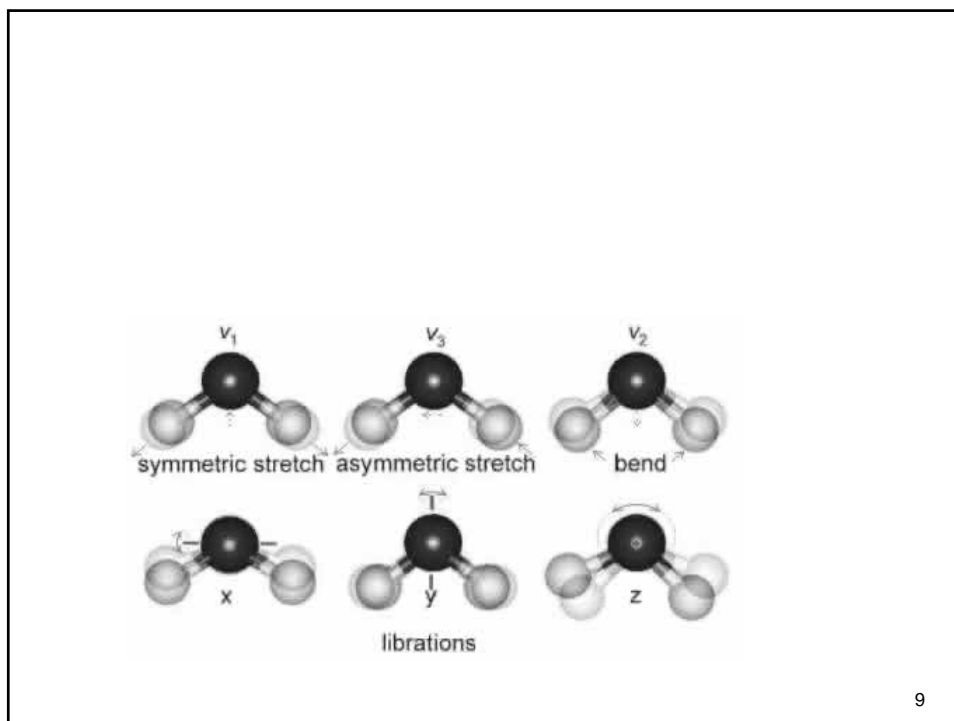
$$\rho_v(z) = \rho_o e^{-z/H_4} \quad [\text{g/m}^3]$$

where  $\rho_o$  averages 7.72 in mid latitudes  
and the total mass of water vapor in a  
column of unit cross section is

$$M_v = \int_0^{\infty} \rho_v(z) dz = \rho_o H_4$$

where  $H_4 =$  between 2–2.5 km water - vapor scale height

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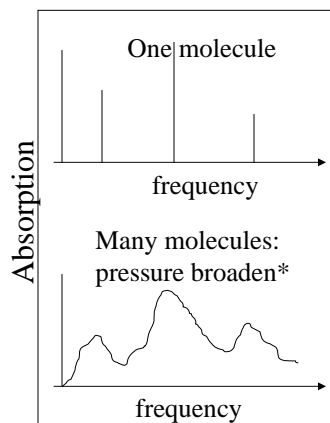
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## EM interaction with Molecules

- **Total internal energy state for a molecule**
  - electronic energy corresponding to atomic level
  - vibration of atoms about their equilibrium position
  - rotation of atoms about center of molecule
  - $\mathcal{E} = \mathcal{E}_e + \mathcal{E}_v + \mathcal{E}_r$
- **Bohr condition**  $f_{m\ell} = (\mathcal{E}_m - \mathcal{E}_l) / h$
- **Values for energy differences for**
  - *electronic*: 2 to 10 eV
  - *vibrational-rotational*: 0.1 to 2 eV
  - *pure rotational*:  $10^{-4}$  to  $5 \times 10^{-2}$  eV ( microwaves)

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## Line Shapes



$$\kappa_a(f, f_{lm}) = \frac{4\pi f}{c} S_{lm} F(f, f_{lm})$$

where,

- $S_{lm}$  is the line strength
- $F(f, f_{lm})$  is the line shape

### LINE SHAPES

- Lorentz
- Gross
- Van-Vleck-Weisskopf

\*caused by collision between molecules

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## Line shapes

- Lorentz 
$$F_L(f, f_{lm}) = \frac{1}{\pi} \frac{\gamma}{(f - f_{lm})^2 + \gamma^2}$$

- Gross 
$$F_G(f, f_{lm}) = \frac{1}{\pi} \frac{4ff_{lm}}{(f_{lm}^2 - f^2)^2 + 4f^2\gamma^2}$$

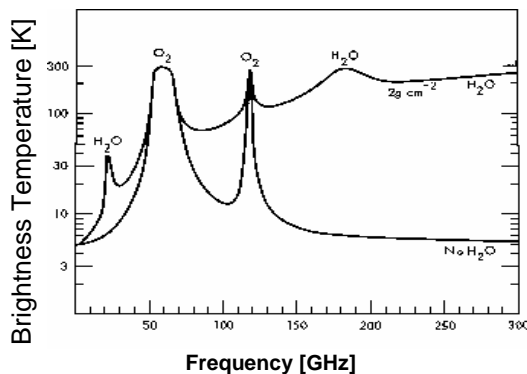
- Van-Vleck-Weisskopf

$$F_{vw}(f, f_{lm}) = \frac{1}{\pi} \left( \frac{f}{f_{lm}} \right)^2 \frac{\gamma}{(f_{lm} - f)^2 + \gamma^2} + \frac{\gamma}{(f_{lm} + f)^2 + \gamma^2}$$

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## Absorption Bands

- Mainly water and oxygen for microwaves



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## Total Atmospheric

- Absorption  $\kappa_g$

$$\kappa_g = \kappa_{H_2O} + \kappa_{O_2}$$

- Opacity  $\tau_\theta$

$$\tau_\theta = \int_0^\infty \kappa_g(z) \sec \theta dz$$

$$= \sec \theta \tau_o$$

- Loss factor  $L_\theta$

$$L_\theta = e^{\tau_o \sec \theta} = e^{\int_0^\infty \kappa_g(z) \sec \theta dz}$$

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## Atmospheric Emission

- For clear atmosphere

$$T_{DN} = \sec \theta \int_0^{\infty} \kappa_a(z') T(z') e^{-\tau(0,z') \sec \theta} dz'$$

where

$$\tau(0,z') = \int_0^{\infty} \kappa_a(z) dz$$

Also there is some background radiation

$$T_{extra} = T_{cosmic} + T_{galactic}$$

$T_{cos} = 2.7K$  from the Big Bang and  $T_{gal} \sim 0$  above 5GHz

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## Relative Humidity

Air Temperature	Vapor air can hold	Actual Vapor in the air [gr per kg dry air]	Relative humidity
86°F	27.6	10.83	39%
77°F	20.4	10.83	53%
68°F	14.9	10.83	72%
59°F	10.8	10.83	100%

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