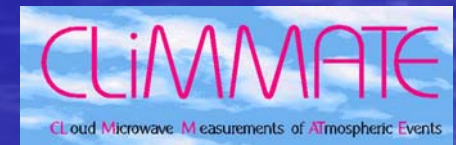




# Non-Precipitating Stratus Cloud Characterization Using a Ground- Based Microwave Doppler Radar

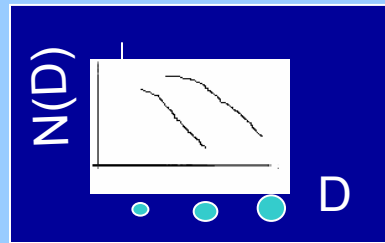
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Center for Cloud Microwave Measurements of Atmospheric Events  
University of Puerto Rico, Mayaguez Campus

Stephen M. Sekelsky, PhD  
Microwave Remote Sensing Laboratory  
University of Massachusetts, Amherst

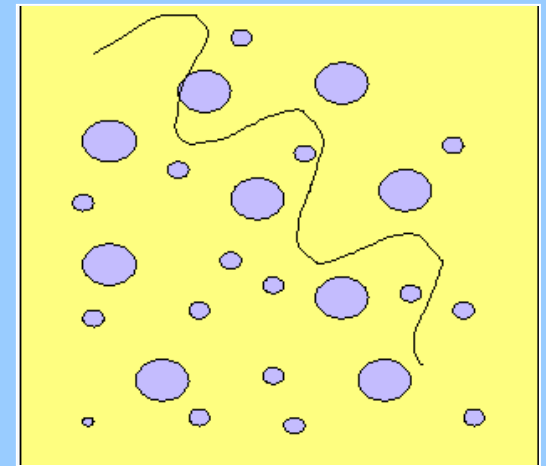


# Cloud's Microphysical Properties

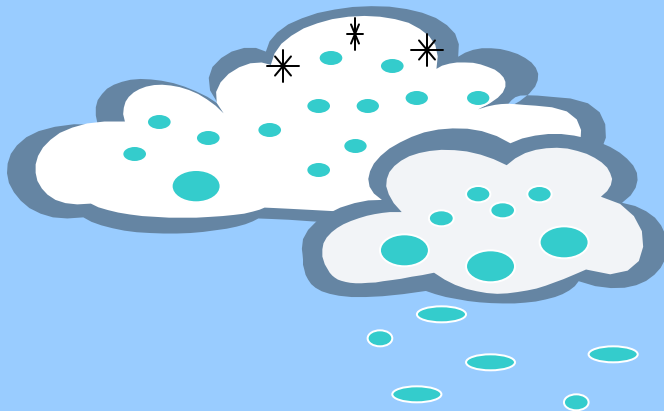
Exponential Distribution



Rayleigh Scattering

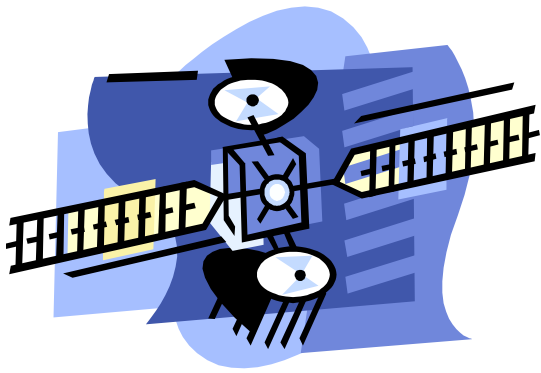


Suspended Water Droplets

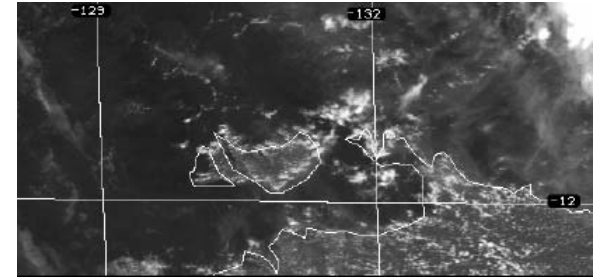


# Clouds Types on the Atmosphere





# Problem



## Atmospheric Correction

Knowing the cloud's macrophysical and microphysical properties the attenuation due to the cloud can be known, with this the cloud can be removed from satellite imagery

## Meteorology

Knowing the microphysical and macrophysical and microphysical properties for weather and global change studies.



# Objectives

- Estimate the microphysical properties of non precipitating stratus cloud
  - Retrieve drop size distribution *parameters* of a stratus cloud
  - Extract the liquid water content
- Validate the exponential size distribution by Marshall and Palmer.



# Cloud Profiling Radar System

Developed by UMass 1994

Field Experiment  
SPG Cart Site, Lamont Oklahoma

Spring 2000



# Horizontally Stratified Atmosphere

$P_n, T_n, P_{wv,n}, h_n, SH_n$

$P_{n-1}, T_{n-1}, P_{wv,n-1}, h_{n-1}, SH_{n-1}$

- 
- 
- 



$P_3, T_3, P_{wv,3}, h_3, SH_3$

$P_2, T_2, P_{wv,2}, h_2, SH_2$

$P_1, T_1, P_{wv,1}, h_1, SH_1$

$P_0, T_0, P_{wv,0}, h_0, SH_0$

Height

Specific Humidity  
vs.  
Height

Pressure  
vs. Height

Temperature  
vs. Height

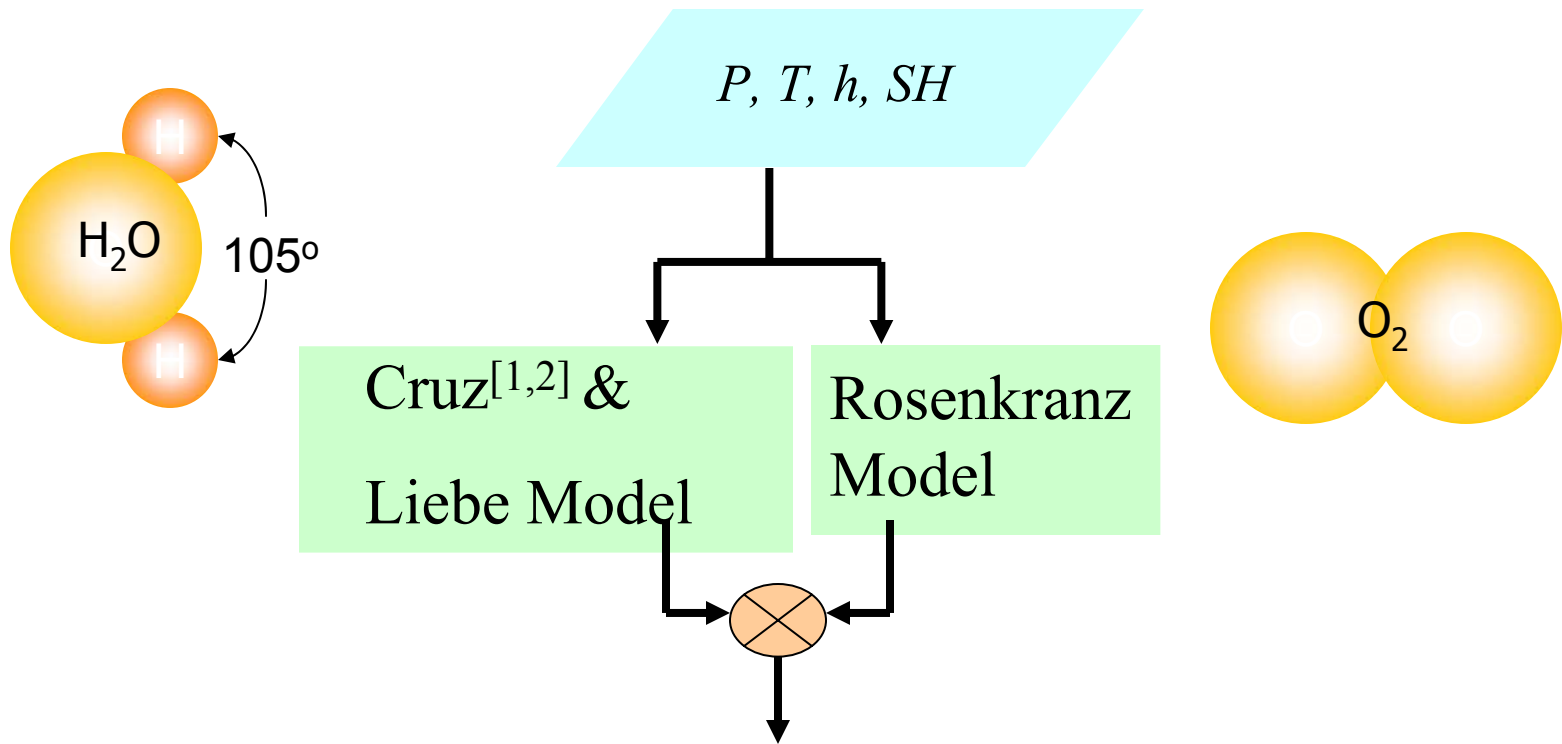


Dual-  
channel  
microwave  
Radiometer

Total integrated  
or column water  
vapor and liquid  
water



# Radiosonde Data Processing



$$K_{Gaseous}(i, f) = K_{WaterVapor}(i, f) + K_{O_2}(i, f)$$

<sup>1</sup> Keihm et al., *IEEE Trans. On Geoscience and Remote Sensing*, June 2002

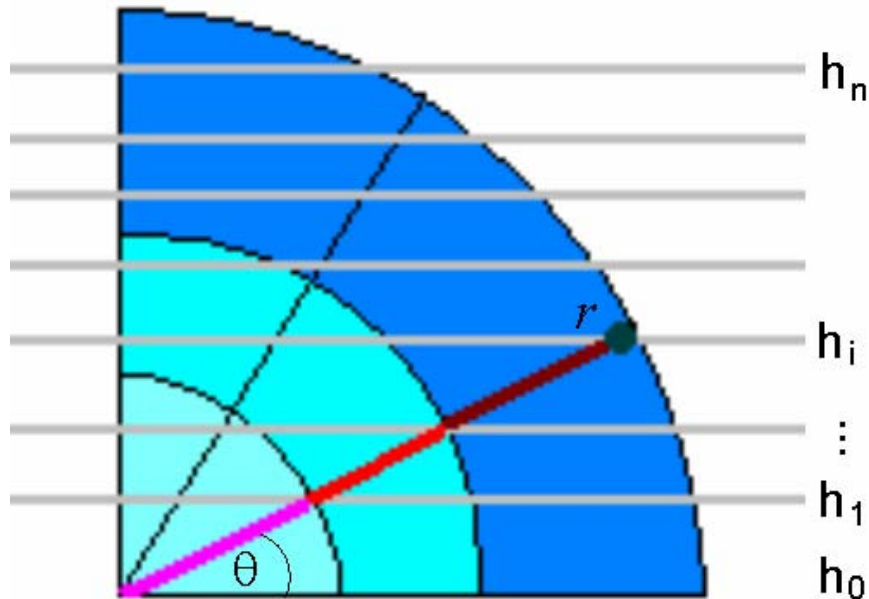
<sup>2</sup> Cruz-Pol et al., "Improve Atmospheric Absorption Model...", *Radio Science*, 2000



Accumulative attenuation is calculated for every radar radius at a fixed angle.

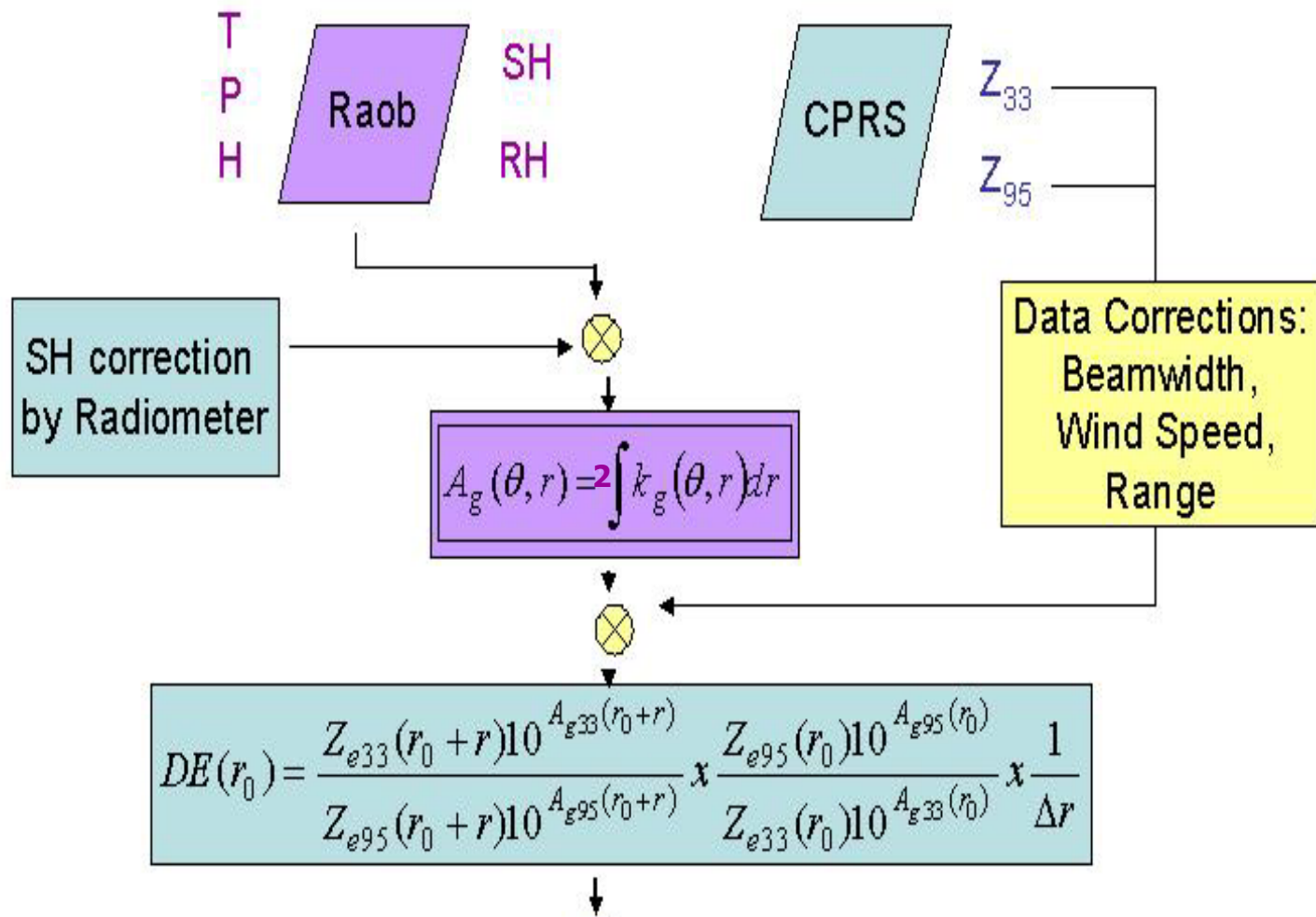
# Cumulative Gaseous Attenuation

$$A_g(\theta, r, f) = \sum_{i=0}^{n-1} k_g(i) [h(i+1) - h(i)] \sin(\theta)$$



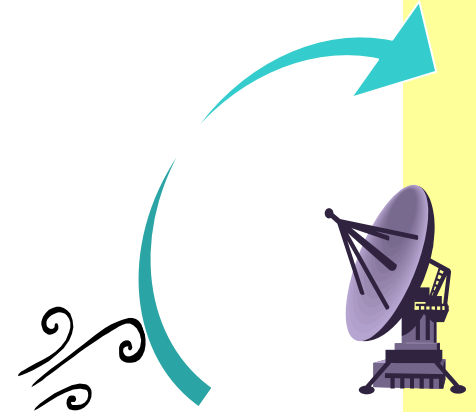
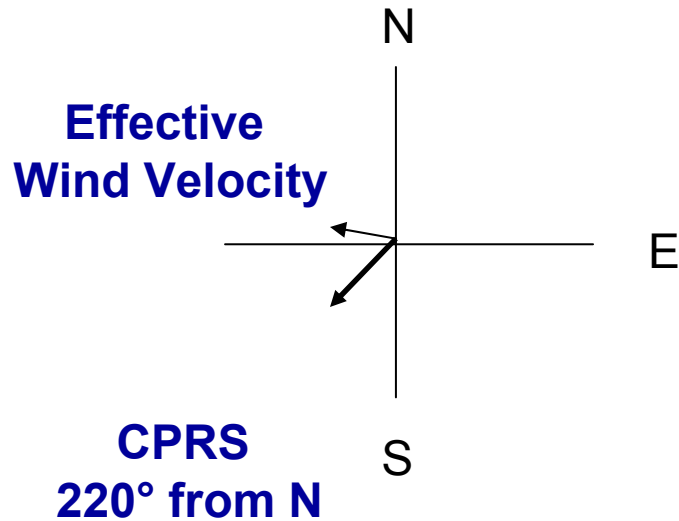
$$\Delta r(i) = [h(i+1) - h(i)] \sin(\theta)$$

# Flow Diagram



# Wind Speed Correction

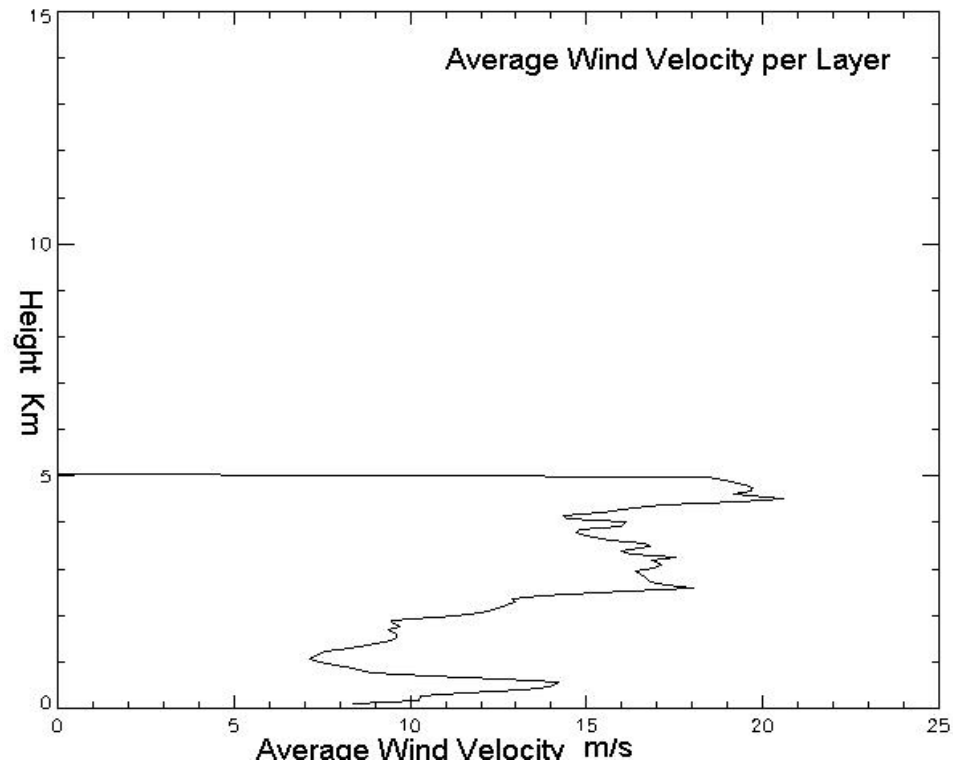
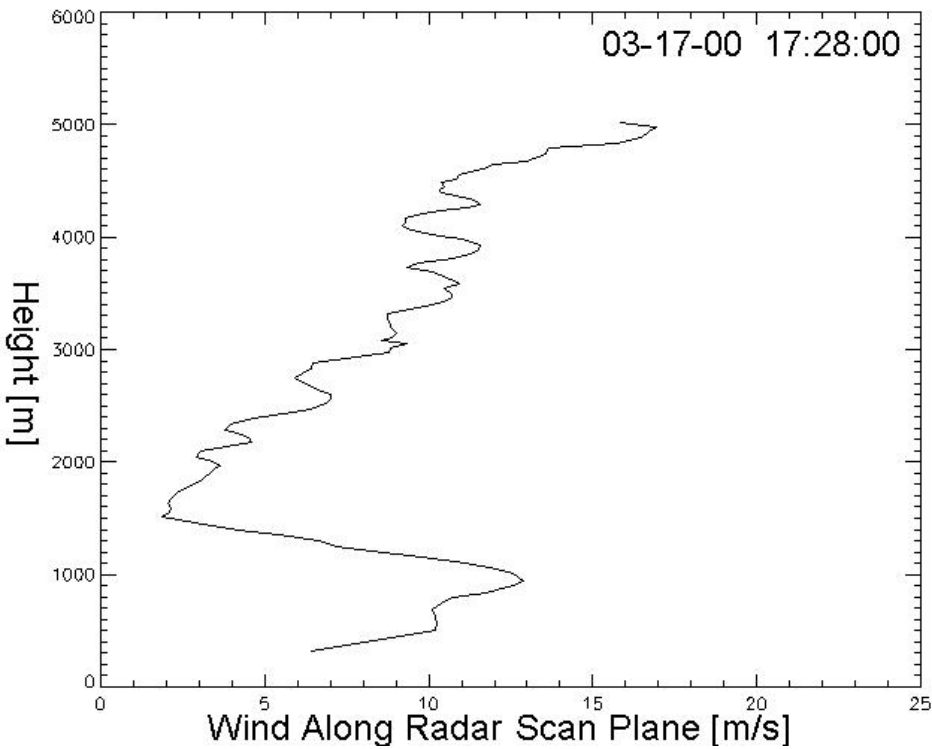
Effective Wind Velocity



N Component  
E Component

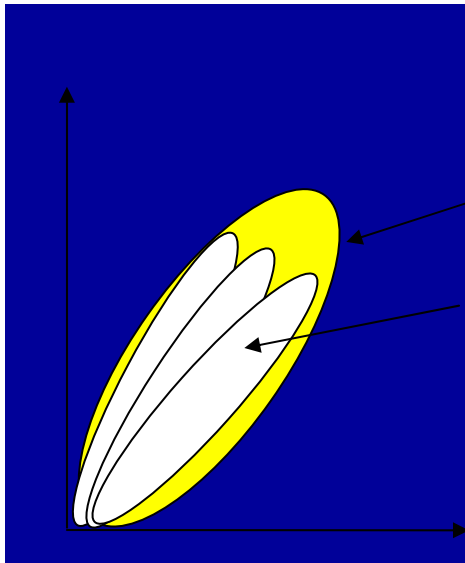


# Effective Wind Velocity



# Beamwidth Correction

$$\operatorname{erf}\left(2\sqrt{\ln 4} \frac{\phi}{\theta_1}\right) - \operatorname{erf}\left(\frac{2\sqrt{\ln 4}[\phi - \alpha MT_s]}{\theta_1}\right) - \frac{1}{2} \operatorname{erf}\left(\sqrt{\ln 4} \frac{\alpha MT_s}{\theta_1}\right) = 0$$



**33 GHz Beamwidth**

**95 GHz Beamwidth**

Half-Power Beamwidth

33 GHz = 0.18 degrees

95 GHz = 0.06 degrees

To degrade the resolution of the 95 GHz to match the sampling volume at 33GHz



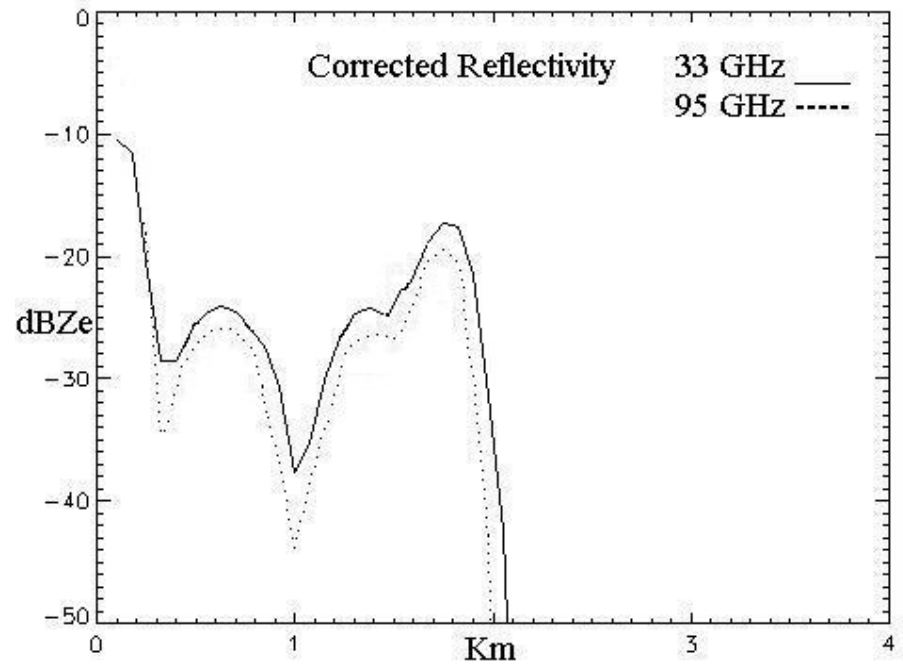
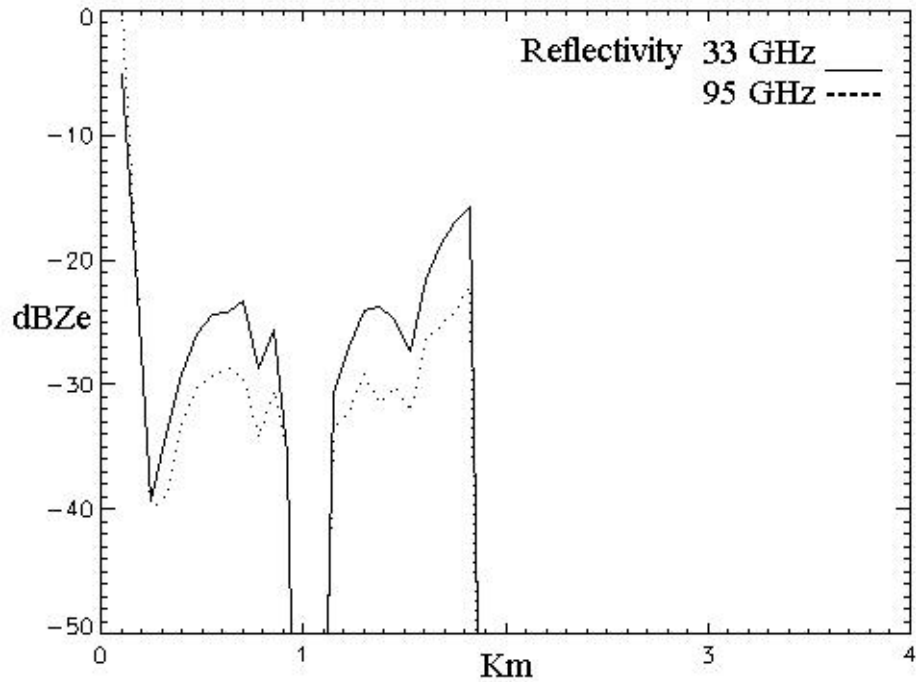
# Range Correction

To reduce the mismatch, reflectivity data was convolved with the range weighting function of the other frequency.

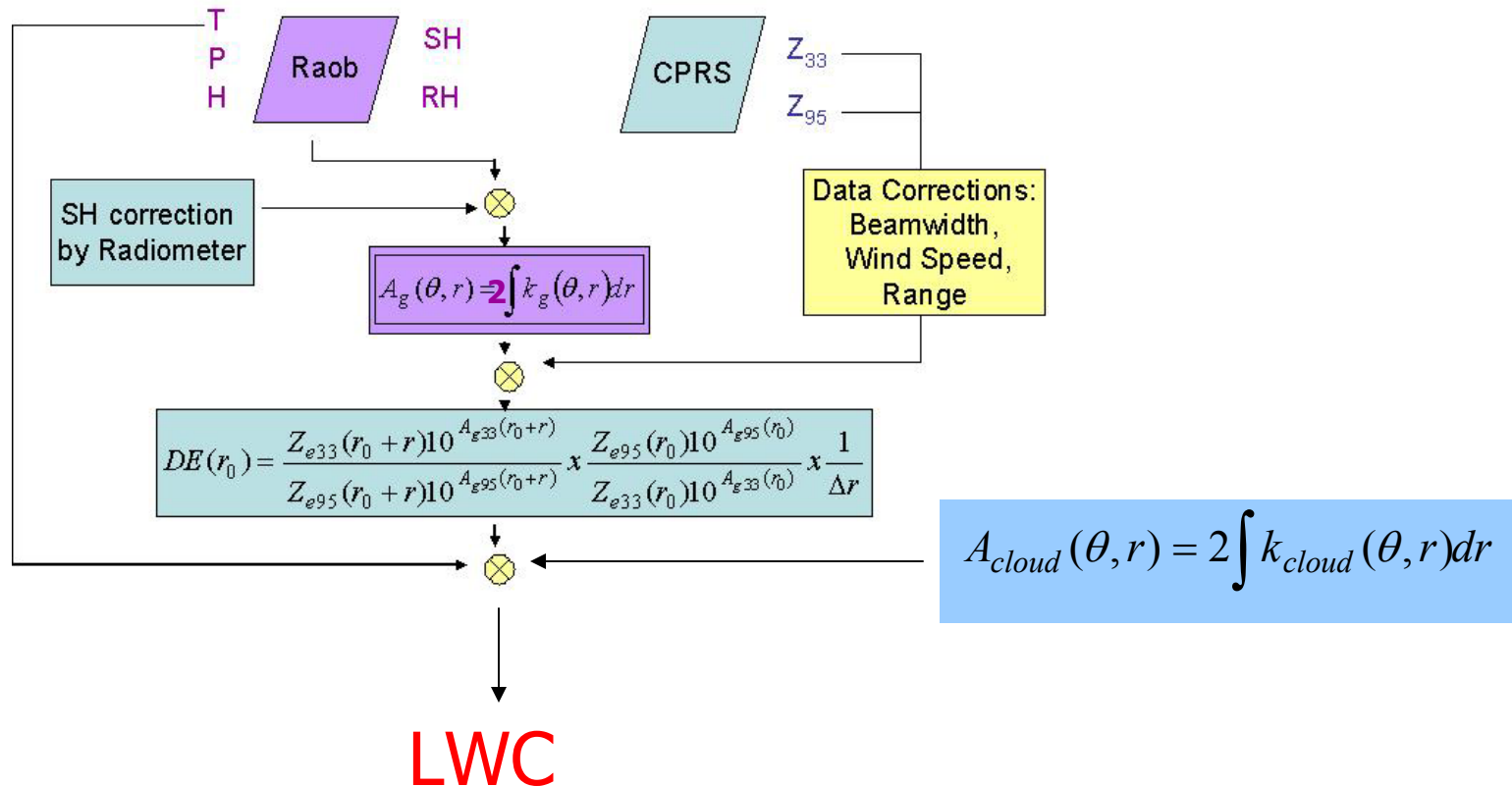
$$W(r) = \frac{1}{2} \left\{ \operatorname{erf} \left[ \left( \frac{2aB_6}{c} \right) \left( r_0 - r + \frac{c\tau}{4} \right) \right] - \operatorname{erf} \left[ \left( \frac{2aB_6}{c} \right) \left( r_0 - r - \frac{c\tau}{4} \right) \right] \right\}$$

$\frac{\pi}{2\sqrt{\ln 2}}$  Pulse Width  
 Bandwidth within 6 dB  
 Speed of Light  
 Scatterer's Maximum Weight Received at

# After Data Correction ...



# Flow Diagram



# Look Up Table To Find LWC

Cloud Attenuation  
From Liebe's  
Model  
For Suspended  
Water Droplets  
at Both  
Frequencies

T

	LWC	LWC	LWC	
DE	LWC	LWC		

# Cloud Characterization Parameters

Newton's Method for Solving Non-Linear Equations Systems

Drop Size Distribution

Effective Diameter

$$N(D) = N_0 D^\mu e^{-3.67 D / D_0}$$

Reflectivity [dBZe]

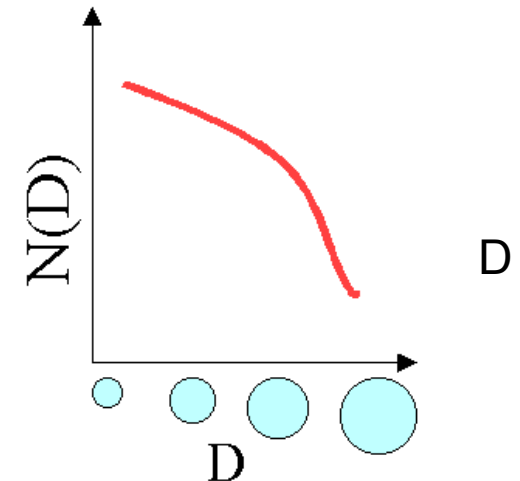
$$Z = \int_0^{\infty} N(D) D^6 dD$$

Peak Number Concentration

Liquid Water Content [g/m<sup>3</sup>]

$$LWC = \frac{\pi \rho_w}{6} \int_0^{\infty} D^3 N(D) dD$$

Exponential Distribution



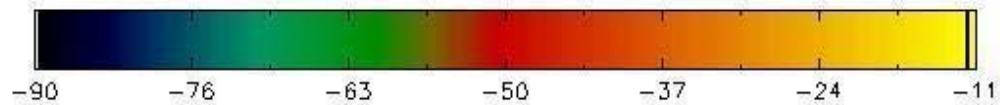
Effective Drop Diameter



# Newton Method for Solving Non Linear System Equations

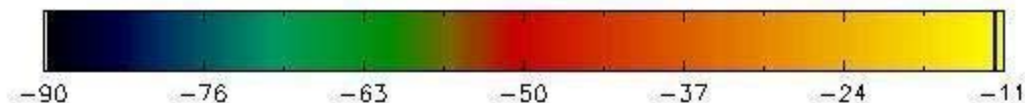
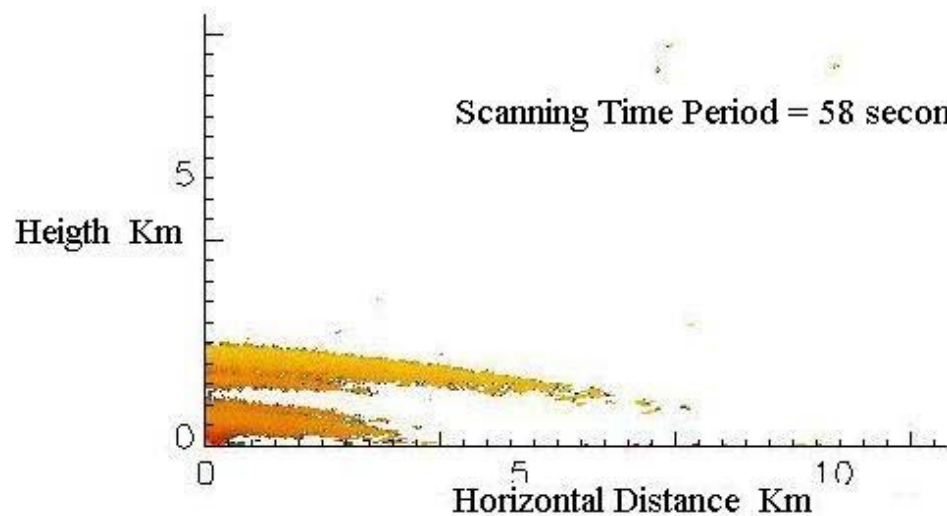
$$\begin{pmatrix} \left( \frac{\partial Z(N_0, D_0)}{\partial N_0} \right) & \left( \frac{\partial Z(N_0, D_0)}{\partial D_0} \right) \\ \left( \frac{\partial LWC(N_0, D_0)}{\partial N_0} \right) & \left( \frac{\partial LWC(N_0, D_0)}{\partial D_0} \right) \end{pmatrix} \begin{pmatrix} \Delta N_0 \\ \Delta D_0 \end{pmatrix} = - \begin{pmatrix} Z(N_0, D_0) \\ LWC(N_0, D_0) \end{pmatrix}$$

Minimizing the Error

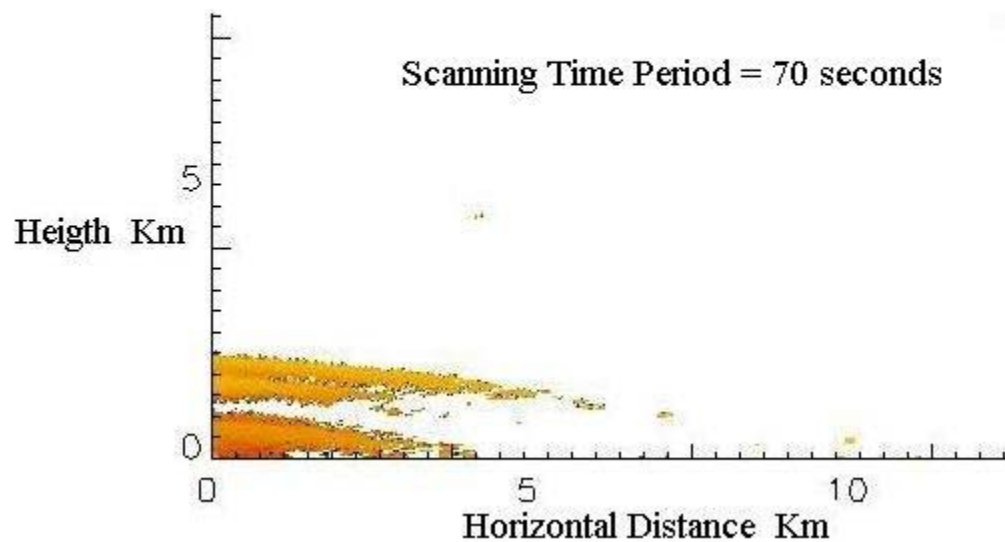


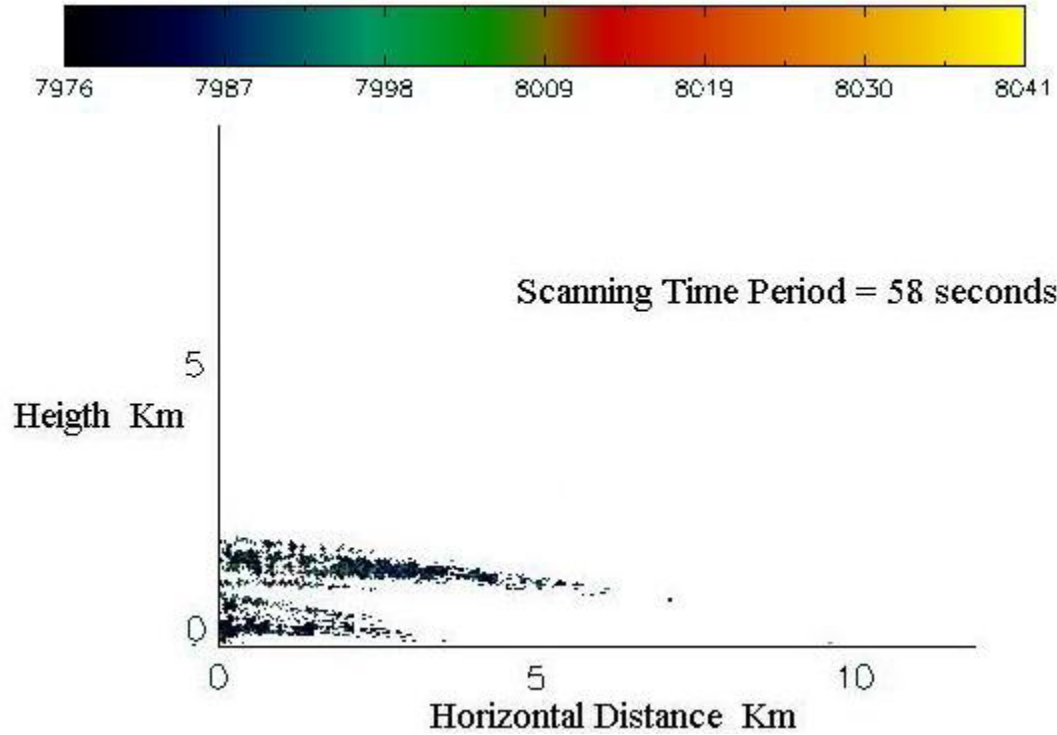
Scanning Time Period = 58 seconds

Z<sub>33</sub> [dBZ]

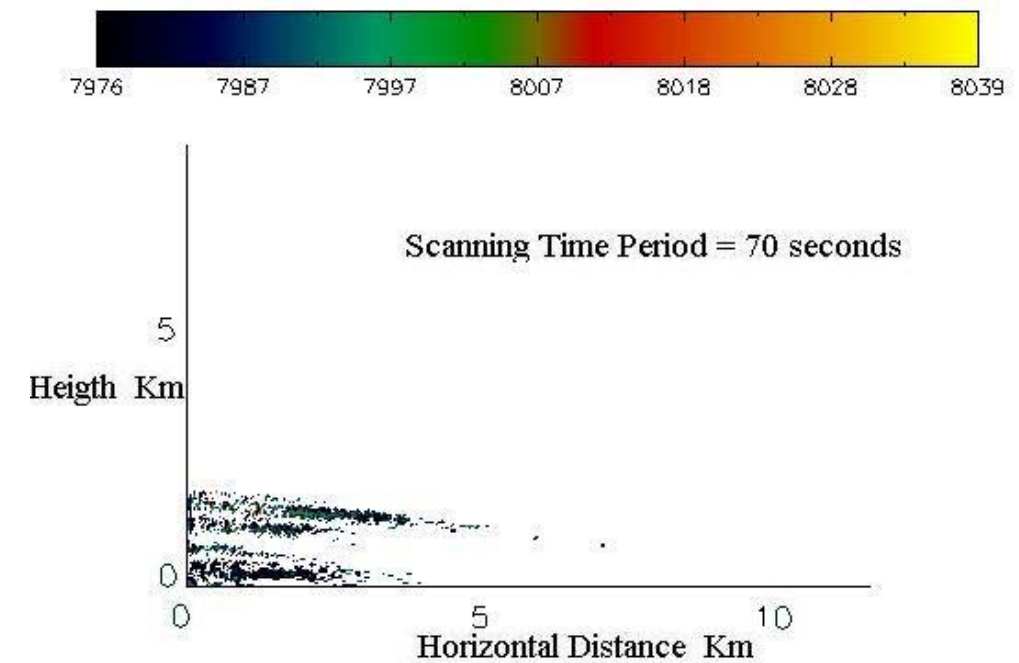


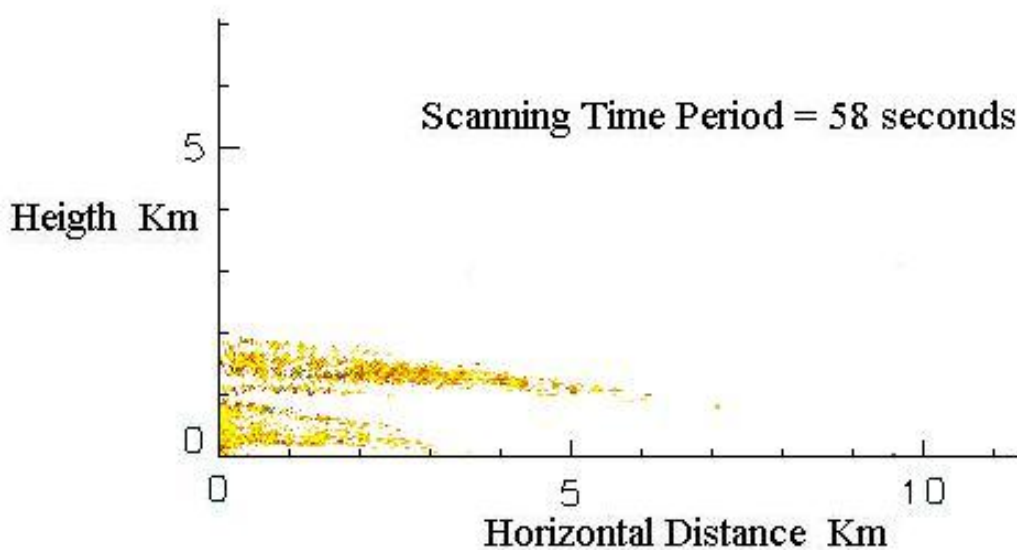
Scanning Time Period = 70 seconds



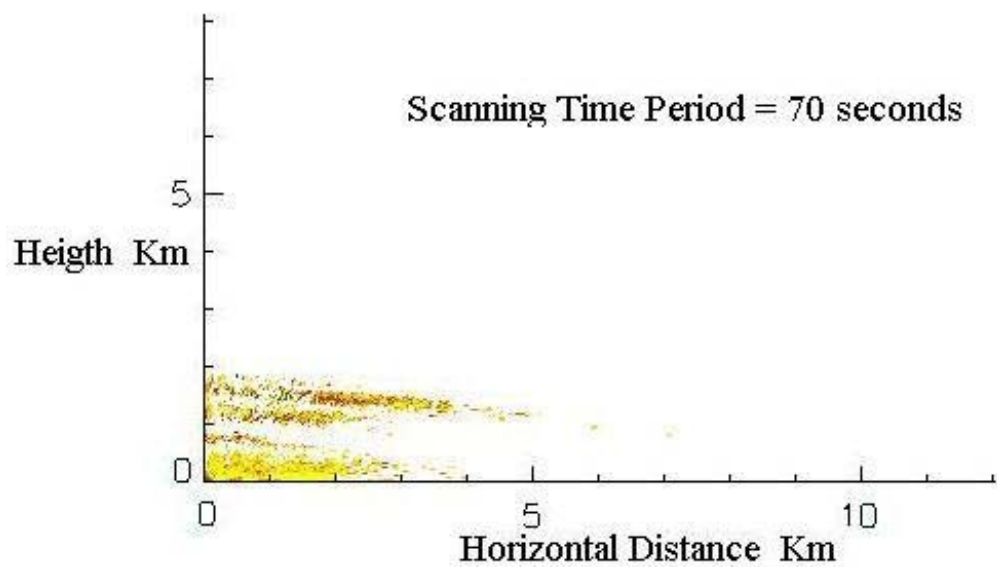
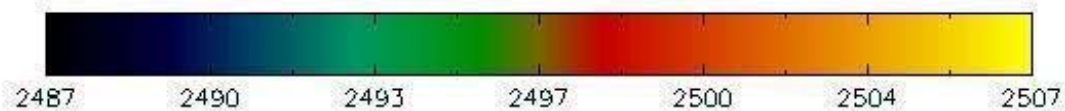


$$N_o \approx 8,000$$





$$D_o \approx 2.5 \mu\text{m}$$



# Conclusions

- Radar reflectivity was used to retrieve cloud's microphysical properties,  $N(D)$ .
- A clear improvement in the W-band and  $K_a$ -band reflectivity after correcting
- The drop size distribution as well as the peak number concentration was estimated using Newton's method for non-linear system of equations.
- $N_0$  and  $D_0$ , were in excellent agreement with the model by Marshall and Palmer





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