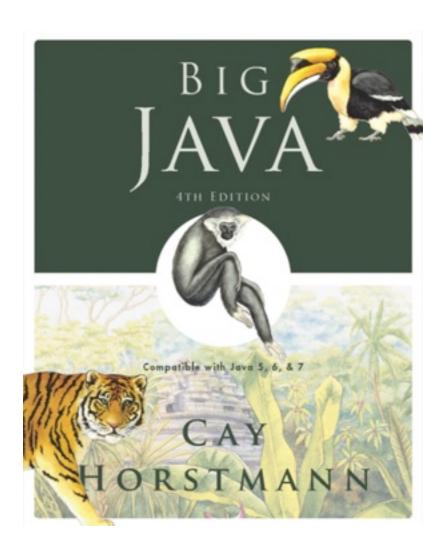
ICOM 4015: Advanced Programming

Lecture 14

Reading: Chapter 14 – Sorting and Searching

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Chapter 14 – Sorting and Searching

Chapter Goals

- To study several sorting and searching algorithms
- To appreciate that algorithms for the same task can differ widely in performance
- To understand the big-Oh notation
- To learn how to estimate and compare the performance of algorithms
- To learn how to measure the running time of a program

Selection Sort

- Sorts an array by repeatedly finding the smallest element of the unsorted tail region and moving it to the front
- Slow when run on large data sets
- Example: sorting an array of integers

11	9	17	5	12
----	---	----	---	----

Sorting an Array of Integers

Find the smallest and swap it with the first element



Find the next smallest. It is already in the correct place



Find the next smallest and swap it with first element of unsorted portion



Repeat



When the unsorted portion is of length 1, we are done



ch14/selsort/SelectionSorter.java

```
/**
    This class sorts an array, using the selection sort
    algorithm

*/
public class SelectionSorter
{
    private int[] a;

    /**
        Constructs a selection sorter.
        @param anArray the array to sort
    */
    public SelectionSorter(int[] anArray)
    {
        a = anArray;
    }
}
```

Continued

ch14/selsort/SelectionSorter.java (cont.)

```
/**
    Sorts the array managed by this selection sorter.
*/
public void sort()
{
    for (int i = 0; i < a.length - 1; i++)
    {
        int minPos = minimumPosition(i);
        swap(minPos, i);
    }
}</pre>
```

Continued

ch14/selsort/SelectionSorter.java (cont.)

```
/**
   Finds the smallest element in a tail range of the array.
   Oparam from the first position in a to compare
   Oreturn the position of the smallest element in the
   range a[from] . . . a[a.length - 1]
private int minimumPosition(int from)
   int minPos = from;
   for (int i = from + 1; i < a.length; i++)
       if (a[i] < a[minPos]) minPos = i;</pre>
   return minPos;
/**
   Swaps two entries of the array.
   @param i the first position to swap
   @param j the second position to swap
* /
private void swap(int i, int j)
   int temp = a[i];
   a[i] = a[j];
   a[j] = temp;
```

ch14/selsort/SelectionSortDemo.java

```
import java.util.Arrays;
/**
   This program demonstrates the selection sort algorithm by
   sorting an array that is filled with random numbers.
* /
public class SelectionSortDemo
   public static void main(String[] args)
      int[] a = ArrayUtil.randomIntArray(20, 100);
      System.out.println(Arrays.toString(a));
      SelectionSorter sorter = new SelectionSorter(a);
      sorter.sort();
      System.out.println(Arrays.toString(a));
```

How Can We Compare Algorithms?

 Option #1: Use a stop watch to measure elapsed time

ch14/selsort/ArrayUtil.java

```
import java.util.Random;
/**
   This class contains utility methods for array manipulation.
* /
public class ArrayUtil
   private static Random generator = new Random();
   /**
       Creates an array filled with random values.
       Oparam length the length of the array
       Oparam n the number of possible random values
       Oreturn an array filled with length numbers between
       0 and n - 1
   * /
   public static int[] randomIntArray(int length, int n)
       int[] a = new int[length];
       for (int i = 0; i < a.length; i++)
          a[i] = generator.nextInt(n);
       return a;
```

ch14/selsort/ArrayUtil.java (cont.)

Typical Program Run:

[65, 46, 14, 52, 38, 2, 96, 39, 14, 33, 13, 4, 24, 99, 89, 77, 73, 87, 36, 81] [2, 4, 13, 14, 14, 24, 33, 36, 38, 39, 46, 52, 65, 73, 77, 81, 87, 89, 96, 99]

Self Check 14.1

Why do we need the temp variable in the swap method? What would happen if you simply assigned a [i] to a [j] and a [j] to a [i]?

Answer: Dropping the temp variable would not work. Then a [i] and a [j] would end up being the same value.

Self Check 14.2

What steps does the selection sort algorithm go through to sort the sequence 6 5 4 3 2 1?

Answer:



Profiling the Selection Sort Algorithm

- We want to measure the time the algorithm takes to execute
 - Exclude the time the program takes to load
 - Exclude output time
- Create a StopWatch class to measure execution time of an algorithm
 - It can start, stop and give elapsed time
 - Use System.currentTimeMillis method
- Create a StopWatch object
 - Start the stopwatch just before the sort
 - Stop the stopwatch just after the sort
 - Read the elapsed time

ch14/selsort/StopWatch.java

```
/**
   A stopwatch accumulates time when it is running. You can
   repeatedly start and stop the stopwatch. You can use a
   stopwatch to measure the running time of a program.
*/
public class StopWatch
   private long elapsedTime;
   private long startTime;
   private boolean isRunning;
    /**
       Constructs a stopwatch that is in the stopped state
       and has no time accumulated.
   * /
   public StopWatch()
       reset();
```

Continued

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ch14/selsort/StopWatch.java (cont.)

```
/**
   Starts the stopwatch. Time starts accumulating now.
* /
public void start()
   if (isRunning) return;
   isRunning = true;
   startTime = System.currentTimeMillis();
/**
   Stops the stopwatch. Time stops accumulating and is
   is added to the elapsed time.
* /
public void stop()
   if (!isRunning) return;
   isRunning = false;
   long endTime = System.currentTimeMillis();
   elapsedTime = elapsedTime + endTime - startTime;
```

Continued

ch14/selsort/StopWatch.java (cont.)

```
/**
   Returns the total elapsed time.
   @return the total elapsed time
* /
public long getElapsedTime()
   if (isRunning)
       long endTime = System.currentTimeMillis();
       return elapsedTime + endTime - startTime;
   else
       return elapsedTime;
/**
   Stops the watch and resets the elapsed time to 0.
* /
public void reset()
   elapsedTime = 0;
   isRunning = false;
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```

ch14/selsort/SelectionSortTimer.java

```
import java.util.Scanner;
/**
   This program measures how long it takes to sort an
   array of a user-specified size with the selection
   sort algorithm.
* /
public class SelectionSortTimer
   public static void main(String[] args)
      Scanner in = new Scanner (System.in);
      System.out.print("Enter array size: ");
      int n = in.nextInt();
      // Construct random array
      int[] a = ArrayUtil.randomIntArray(n, 100);
      SelectionSorter sorter = new SelectionSorter(a);
```

Continued

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ch14/selsort/SelectionSortTimer.java (cont.)

Program Run:

```
Enter array size: 100000
Elapsed time: 27880 milliseconds
```

Selection Sort on Various Size Arrays*

n	Milliseconds	
10,000	786	
20,000	2,148	
30,000	4,796	
40,000	9,192	
50,000	13,321	
60,000	19,299	

^{*} Obtained with a Pentium processor, 2 GHz, Java 6, Linux

Selection Sort on Various Size Arrays

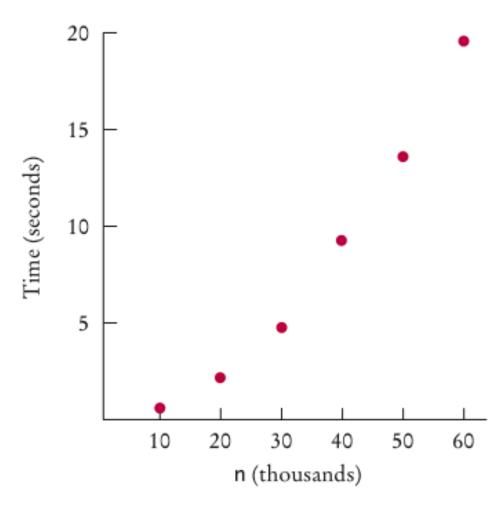


Figure 1 Time Taken by Selection Sort

How Can We Compare Algorithms?

- Option #1: Use a stop watch to measure elapsed time
 - Dependent on factors foreign to algorithm behavior: machine speed, programming skill, OS efficiency, etc.

Selection Sort on Various Size Arrays

 Doubling the size of the array more than doubles the time needed to sort it

Self Check 14.3

Approximately how many seconds would it take to sort a data set of 80,000 values?

Answer: Four times as long as 40,000 values, or about 36 seconds.

Self Check 14.4

Look at the graph in Figure 1. What mathematical shape does it resemble?

Answer: A parabola.

How Can We Compare Algorithms?

- Option #2: Use analysis to count "steps" as a mathematical function of "input size"
- Problems:
 - What is a step?
 - How do we measure input size?
- Solutions:
 - Define then consistently across algorithms being compared

Analyzing the Performance of the Selection Sort Algorithm

- A <u>step</u> is a visit to an array element
- The size of the input is the length of the array
- In an array of size n, count how many times an array element is visited
 - To find the smallest, visit n elements + 2 visits for the swap
 - To find the next smallest, visit (n 1) elements + 2 visits for the swap
 - The last term is 2 elements visited to find the smallest + 2 visits for the swap

Analyzing the Performance of the Selection Sort Algorithm

- The number of visits:
 - n + 2 + (n 1) + 2 + (n 2) + 2 + ... + 2 + 2
 - This can be simplified to $n^2/2 + 5n/2 3$
 - 5n/2 3 is small compared to $n^2/2$ so let's ignore it
 - Also ignore the 1/2 it cancels out when comparing ratios

Analyzing the Performance of the Selection Sort Algorithm

- The number of visits is of the order n²
- Using big-Oh notation: The number of visits is $O(n^2)$
- Multiplying the number of elements in an array by 2 multiplies the processing time by 4
- Big-Oh notation "f(n) = O(g(n))" expresses that f grows no faster than g
- To convert to big-Oh notation: Locate fastest-growing term, and ignore constant coefficient

Self Check 14.5

If you increase the size of a data set tenfold, how much longer does it take to sort it with the selection sort algorithm?

Answer: It takes about 100 times longer.

Self Check 14.6

How large does n need to be so that $n^2/2$ is bigger than 5n/2 - 3?

Answer: If *n* is 4, then $n^2/2$ is 8 and 5n/2 - 3 is 7.

Insertion Sort

• Assume initial sequence a [0] ... a [k] is sorted (k = 0):



Add a [1]; element needs to be inserted before 11



• Add a [2]



• Add a [3]

• Finally, add a [4]

ch14/insertionsort/InsertionSorter.java

```
/**
    This class sorts an array, using the insertion sort
    algorithm

*/
public class InsertionSorter
{
    private int[] a;

    /**
        Constructs an insertion sorter.
        @param anArray the array to sort
    */
    public InsertionSorter(int[] anArray)
    {
        a = anArray;
    }
}
```

Continued

ch14/insertionsort/InsertionSorter.java (cont.)

```
/**
   Sorts the array managed by this insertion sorter
* /
public void sort()
   for (int i = 1; i < a.length; i++)</pre>
       int next = a[i];
       // Move all larger elements up
       int j = i;
       while (j > 0 \&\& a[j - 1] > next)
           a[j] = a[j - 1];
           i −−;
       // Insert the element
       a[j] = next;
```

How Can We Compare Algorithms?

- Option #2: Use analysis to count "steps" as a mathematical function of "input size"
- Another Problem:
 - What if the Algorithm may work faster on particular inputs?
- Solutions:
 - Easy: Consider worst, best cases
 - Harder: Make simplifying probabilistic
 assumptions and calculate averageruntime
 - Hardest: Consider realistic probabilistic model of inputs and calculate average runtime

Analyzing the Performance of the Insertion Sort Algorithm

- The number of visits to insert ith element can go from 1 to n-i
- Assume any case equally likely (BIG ASSUMPTION)
- The worst-case number of visits to insert ith element is (n-i)
- The average number of visits to insert ith element is (n-i)/2
- Total visits is roughly: $n + (n 1) + (n 2) \dots + 1 = n*(n+1)/2$
- Using big-Oh notation: The number of visits is then $O(n^2)$ in both the worst and average cases

Merge Sort

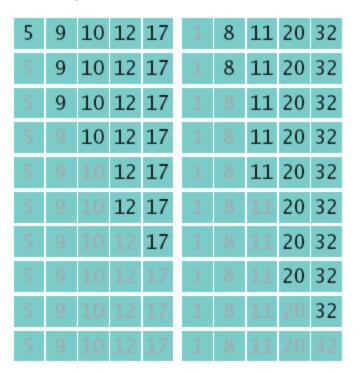
- Sorts an array by
 - Cutting the array in half
 - Recursively sorting each half
 - Merging the sorted halves
- Dramatically faster than the selection sort

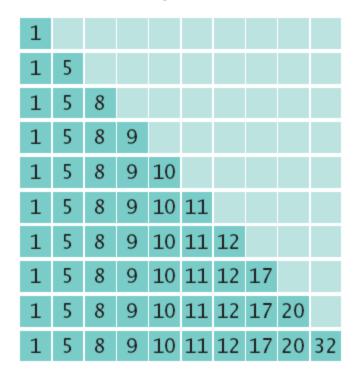
Merge Sort Example

Divide an array in half and sort each half



Merge the two sorted arrays into a single sorted array





Merge Sort

```
public void sort()
   if (a.length <= 1) return;</pre>
   int [] first = new int[a.length / 2];
   int[] second = new int[a.length - first.length];
   // Copy the first half of a into first, the second half
   // into second
   MergeSorter firstSorter = new MergeSorter(first);
   MergeSorter secondSorter = new MergeSorter (second);
   firstSorter.sort();
   secondSorter.sort();
   merge(first, second);
```

ch14/mergesort/MergeSorter.java

```
/**
    This class sorts an array, using the merge sort algorithm.
*/
public class MergeSorter
{
    private int[] a;

    /**
        Constructs a merge sorter.
        @param anArray the array to sort
    */
    public MergeSorter(int[] anArray)
    {
        a = anArray;
    }
}
```

Continued

ch14/mergesort/MergeSorter.java (cont.)

```
/**
   Sorts the array managed by this merge sorter.
* /
public void sort()
   if (a.length <= 1) return;</pre>
   int[] first = new int[a.length / 2];
   int[] second = new int[a.length - first.length];
   // Copy the first half of a into first, the second half into second
   for (int i = 0; i < first.length; i++) { first[i] = a[i]; }</pre>
   for (int i = 0; i < second.length; i++)</pre>
       second[i] = a[first.length + i];
   MergeSorter firstSorter = new MergeSorter(first);
   MergeSorter secondSorter = new MergeSorter(second);
   firstSorter.sort();
   secondSorter.sort();
   merge(first, second);
```

Continued

ch14/mergesort/MergeSorter.java (cont.)

```
/**
   Merges two sorted arrays into the array managed by this merge sorter.
   @param first the first sorted array
   Oparam second the second sorted array
* /
private void merge(int[] first, int[] second)
   int iFirst = 0; // Next element to consider in the first array
    int iSecond = 0; // Next element to consider in the second array
    int j = 0; // Next open position in a
    // As long as neither iFirst nor iSecond is past the end, move
    // the smaller element into a
    while (iFirst < first.length && iSecond < second.length)</pre>
       if (first[iFirst] < second[iSecond])</pre>
           a[j] = first[iFirst];
           iFirst++;
       else
           a[j] = second[iSecond];
                                                                                Continued
           iSecond++;
       j++;
                                                                             Big Java by Cay Horstmann
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```

ch14/mergesort/MergeSorter.java (cont.)

```
// Note that only one of the two loops below copies entries
// Copy any remaining entries of the first array
while (iFirst < first.length)
{
    a[j] = first[iFirst];
    iFirst++; j++;
}
// Copy any remaining entries of the second half
while (iSecond < second.length)
{
    a[j] = second[iSecond];
    iSecond++; j++;
}
}</pre>
```

ch14/mergesort/MergeSortDemo.java

```
import java.util.Arrays;
/ * *
   This program demonstrates the merge sort algorithm by
   sorting an array that is filled with random numbers.
* /
public class MergeSortDemo
   public static void main(String[] args)
      int[] a = ArrayUtil.randomIntArray(20, 100);
      System.out.println(Arrays.toString(a));
      MergeSorter sorter = new MergeSorter(a);
      sorter.sort();
      System.out.println(Arrays.toString(a));
```

Continued

ch14/mergesort/MergeSortDemo.java (cont.)

Typical Program Run:

```
[8, 81, 48, 53, 46, 70, 98, 42, 27, 76, 33, 24, 2, 76, 62, 89, 90, 5, 13, 21]
[2, 5, 8, 13, 21, 24, 27, 33, 42, 46, 48, 53, 62, 70, 76, 76, 81, 89, 90, 98]
```

Self Check 14.7

Why does only one of the two while loops at the end of the merge method do any work?

Answer: When the preceding while loop ends, the loop condition must be false, that is,

iFirst >= first.length or iSecond >= second.length (De Morgan's Law).

Self Check 14.8

Manually run the merge sort algorithm on the array 8 7 6 5 4 3 2 1.

Answer:

First sort 8 7 6 5.

Recursively, first sort 87.

Recursively, first sort 8. It's sorted.

Sort 7. It's sorted.

Merge them: 7 8.

Do the same with 6 5 to get 5 6.

Merge them to 5 6 7 8.

Do the same with 4 3 2 1: Sort 4 3 by sorting 4 and 3 and merging them to 3 4.

Sort 2 1 by sorting 2 and 1 and merging them to 1 2.

Merge 3 4 and 1 2 to 1 2 3 4.

Finally, merge 5 6 7 8 and 1 2 3 4 to 1 2 3 4 5 6 7 8.

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Analyzing the Merge Sort Algorithm

n	Merge Sort (milliseconds)	Selection Sort (milliseconds)
10,000	40	786
20,000	73	2,148
30,000	134	4,796
40,000	170	9,192
50,000	192	13,321
60,000	205	19,299

Merge Sort Timing vs. Selection Sort

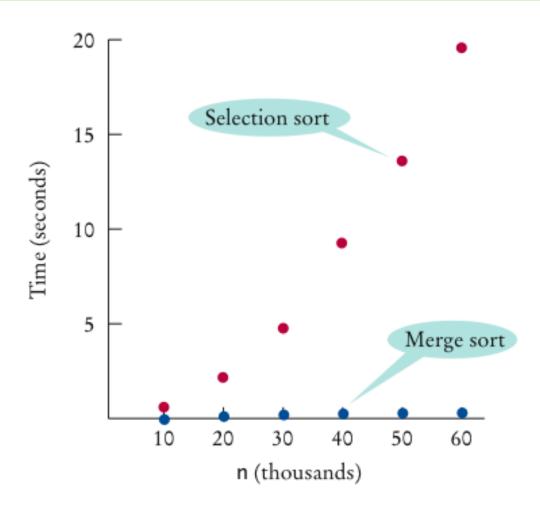


Figure 2 Merge Sort Timing versus Selection Sort

Analyzing the Merge Sort Algorithm

- In an array of size n, count how many times an array element is visited
- Assume *n* is a power of 2: $n = 2^m$
- Calculate the number of visits to create the two sub-arrays and then merge the two sorted arrays
 - 3 visits to merge each element or 3n visits
 - 2n visits to create the two sub-arrays
 - total of 5n visits

Analyzing the Merge Sort Algorithm

- Let T(n) denote the number of visits to sort an array of n elements then
 - T(n) = T(n/2) + T(n/2) + 5n or
 - T(n) = 2T(n/2) + 5n
- The visits for an array of size *n*/2 is:
 - T(n/2) = 2T(n/4) + 5n/2
 - So $T(n) = 2 \times 2T(n/4) + 5n + 5n$
- The visits for an array of size *n*/4 is:
 - T(n/4) = 2T(n/8) + 5n/4
 - So $T(n) = 2 \times 2 \times 2T(n/8) + 5n + 5n + 5n$

Analyzing Merge Sort Algorithm

- Repeating the process k times:
 - $T(n) = 2 {}^{k}T(n/2^{k}) + 5nk$
 - Since $n = 2^m$, when k=m: $T(n) = 2^m T(n/2^m) + 5nm$
 - T(n) = nT(1) + 5nm
 - $T(n) = n + 5n\log_2(n)$

Analyzing Merge Sort Algorithm

- To establish growth order
 - Drop the lower-order term n
 - Drop the constant factor 5
 - Drop the base of the logarithm since all logarithms are related by a constant factor
 - We are left with n log(n)
- Using big-Oh notation: Number of visits is $O(n\log(n))$

Merge Sort Vs Selection Sort

- Selection sort is an $O(n^2)$ algorithm
- Merge sort is an O(nlog(n)) algorithm
- The $n\log(n)$ function grows much more slowly than n^2

Self Check 14.9

Given the timing data for the merge sort algorithm in the table at the beginning of this section, how long would it take to sort an array of 100,000 values?

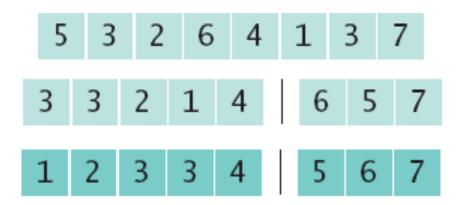
Answer: Approximately $100,000 \times \log(100,000) / 50,000 \times \log(50,000) = 2 \times 5 / 4.7 = 2.13$ times the time required for 50,000 values. That's 2.13×97 milliseconds or approximately 207 milliseconds.

Self Check 14.10

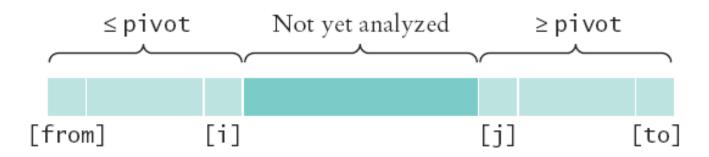
If you double the size of an array, how much longer will the merge sort algorithm take to sort the new array?

Answer: $(2n \log(2n)/n \log(n)) = 2(1 + \log(2)/\log(n))$. For n > 2, that is a value < 3.

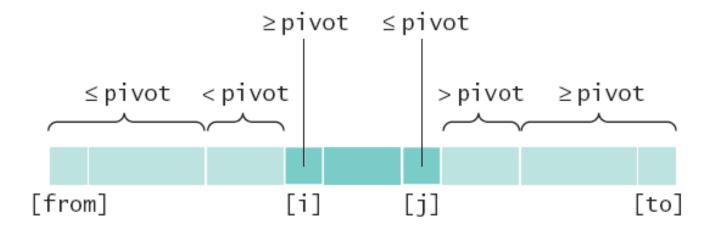
- Divide and conquer
 - 1.Partition the range
 - 2. Sort each partition



```
public void sort(int from, int to)
{
   if (from >= to)
   return; int p =
   partition(from, to);
   sort(from, p);
   sort(p + 1, to);
}
```



Partitioning a Range



Extending the Partitions

```
private int partition(int from, int to)
   int pivot = a[from];
   int i = from - 1;
   int j = to + 1;
   while (i < j)
      <u>i++;</u>
      while (a[i] < pivot) i++;
      j--;
      while (a[j] > pivot) j--;
      if (i < j) swap(i, j);
   return j;
```

Analyzing the Quick Sort Algorithm

- In an array of size n, count how many times an array element is visited
- Assume n is a power of 2: $n = 2^m$
- Calculate the number of visits to find the pivot and create the two sub-arrays

The First Programmer



Babbage's Difference Engine

Searching

- Linear search: also called sequential search
- Examines all values in an array until it finds a match or reaches the end
- Number of visits for a linear search of an array of n elements:
 - The average search visits n/2 elements
 - The maximum visits is n
- A linear search locates a value in an array in O(n) steps

ch14/linsearch/LinearSearcher.java

```
/**
    A class for executing linear searches through an array.
*/
public class LinearSearcher
{
    private int[] a;

    /**
        Constructs the LinearSearcher.
        @param anArray an array of integers
        */
    public LinearSearcher(int[] anArray)
        {
            a = anArray;
        }
}
```

Continued

ch14/linsearch/LinearSearcher.java (cont.)

```
/**
   Finds a value in an array, using the linear search
   algorithm.
    @param v the value to search
    @return the index at which the value occurs, or -1
   if it does not occur in the array
* /
public int search(int v)
   for (int i = 0; i < a.length; i++)</pre>
        if (a[i] == v)
           return i;
   return -1;
```

ch14/linsearch/LinearSearchDemo.java

```
import java.util.Arrays;
import java.util.Scanner;

/**
    This program demonstrates the linear search algorithm.

*/
public class LinearSearchDemo
{
    public static void main(String[] args)
    {
        int[] a = ArrayUtil.randomIntArray(20, 100);
        System.out.println(Arrays.toString(a));
        LinearSearcher searcher = new LinearSearcher(a);

        Scanner in = new Scanner(System.in);
```

Continued

ch14/linsearch/LinearSearchDemo.java (cont.)

```
boolean done = false;
while (!done)
{
    System.out.print("Enter number to search for, -1 to quit: ");
    int n = in.nextInt();
    if (n == -1)
        done = true;
    else
    {
        int pos = searcher.search(n);
        System.out.println("Found in position " + pos);
    }
}
```

Typical Program Run:

```
[46, 99, 45, 57, 64, 95, 81, 69, 11, 97, 6, 85, 61, 88, 29, 65, 83, 88, 45, 88] Enter number to search for, -1 to quit: 11 Found in position 8
```

Self Check 14.11

Suppose you need to look through 1,000,000 records to find a telephone number. How many records do you expect to search before finding the number?

Answer: On average, you'd make 500,000 comparisons.

Self Check 14.12

Why can't you use a "for each" loop for (intelement: a) in the search method?

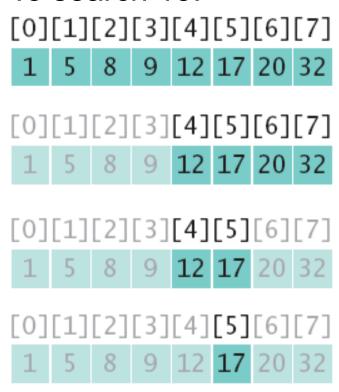
Answer: The search method returns the index at which the match occurs, not the data stored at that location.

Binary Search

- Locates a value in a sorted array by
 - Determining whether the value occurs in the first or second half
 - Then repeating the search in one of the halves

Binary Search

• To search 15:



• 15 ≠ 17: We don't have a match

ch14/binsearch/BinarySearcher.java

```
/**
    A class for executing binary searches through an array.
*/
public class BinarySearcher
{
    private int[] a;

    /**
        Constructs a BinarySearcher.
        @param anArray a sorted array of integers
        */
    public BinarySearcher(int[] anArray)
        {
            a = anArray;
        }
}
```

Continued

ch14/binsearch/BinarySearcher.java (cont.)

```
/**
   Finds a value in a sorted array, using the binary
   search algorithm.
   @param v the value to search
   @return the index at which the value occurs, or -1
   if it does not occur in the array
* /
public int search(int v)
   int low = 0;
   int high = a.length - 1;
   while (low <= high)</pre>
       int mid = (low + high) / 2;
       int diff = a[mid] - v;
       if (diff == 0) // a[mid] == v
           return mid;
       else if (diff < 0) // a[mid] < v
           low = mid + 1;
       else
          high = mid - 1;
   return -1;
```

Binary Search

- Count the number of visits to search a sorted array of size n
 - We visit one element (the middle element) then search either the left or right subarray
 - Thus: T(n) = T(n/2) + 1
- If n is n/2, then T(n/2) = T(n/4) + 1
- Substituting into the original equation: T(n) = T(n/4) + 2
- This generalizes to: $T(n) = T(n/2^k) + k$

Binary Search

- Assume n is a power of 2, n = 2mwhere $m = \log_2(n)$
- Then: $T(n) = 1 + \log_2(n)$
- Binary search is an O(log(n)) algorithm

Searching a Sorted Array in a Program

- The Arrays class contains a static binarySearch method
- The method returns either
 - The index of the element, if element is found
 - Or -k 1 where k is the position before which the element should be inserted:

```
int[] a = { 1, 4, 9 };
int v = 7;
int pos = Arrays.binarySearch(a, v);
    // Returns -3; v should be inserted before
    // position 2
```

Suppose you need to look through a sorted array with 1,000,000 elements to find a value. Using the binary search algorithm, how many records do you expect to search before finding the value?

Answer: You would search about 20. (The binary log of 1,024 is 10.)

Why is it useful that the Arrays.binarySearch method indicates the position where a missing element should be inserted?

Answer: Then you know where to insert it so that the array stays sorted, and you can keep using binary search.

Why does Arrays.binarySearch return -k - 1 and not -k to indicate that a value is not present and should be inserted before position k?

Answer: Otherwise, you would not know whether a value is present when the method returns 0.

- The Arrays class contains static sort methods
- To sort an array of integers:

```
int[] a = \dots;
Arrays.sort(a);
```

 That sort method uses the Quicksort algorithm (see Special Topic 14.3)

• Arrays.sort sorts objects of classes that implement Comparable interface:

```
public interface Comparable
{
   int compareTo(Object otherObject);
}
```

- The call a.compareTo(b) returns
 - A negative number if a should come before b
 - 0 if a and b are the same
 - A positive number otherwise

- Several classes in Java (e.g. String and Date) implement Comparable
- You can implement Comparable interface for your own classes:

```
public class Coin implements Comparable
{
    ...
    public int compareTo(Object otherObject)
    {
        Coin other = (Coin)otherObject;
        if (value < other.value) return -1;
        if (value == other.value) return 0;
        return 1;
    }
    ...
}</pre>
```

compareTo Method

- The implementation must define a total ordering relationship
 - Antisymmetric

If a.compare To(b)
$$\leq 0$$
, then b.compare To(a) ≥ 0

Reflexive

```
a.compareTo(a) = 0
```

Transitive

If a.compareTo(b)
$$\leq$$
 0 and b.compareTo(c) \leq 0, then a.compareTo(c) \leq 0

• Once your class implements Comparable, simply use the Arrays.sort method:

```
Coin[] coins = new Coin[n];
// Add coins
...
Arrays.sort(coins);
```

• If the objects are stored in an ArrayList, use

```
Collections.sort:
ArrayList<Coin> coins = new ArrayList<Coin>();
// Add coins
...
Collections.sort(coins);
```

Collections.sort uses the merge sort algorithm

Why can't the Arrays.sort method sort an array of Rectangle objects?

Answer: The Rectangle class does not implement the Comparable interface.

What steps would you need to take to sort an array of BankAccount objects by increasing balance?

Answer: The BankAccount class needs to implement the Comparable interface. Its compareTo method must compare the bank balances.