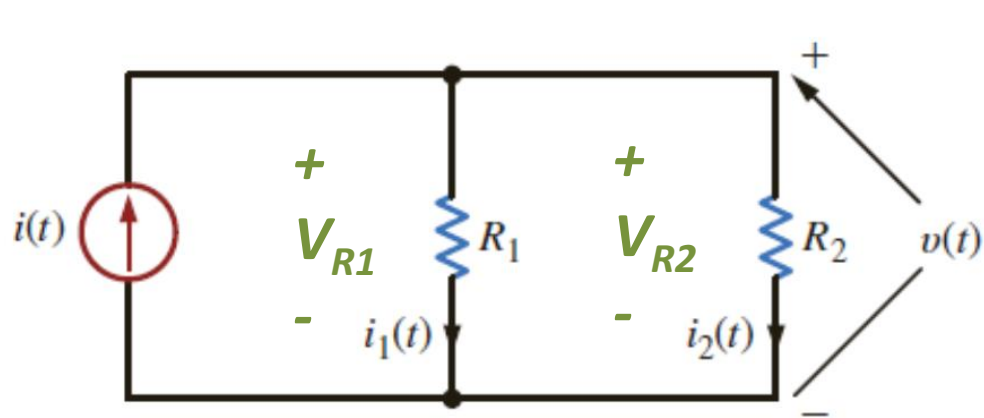


Last Lecture → Current / Voltage Division

8/21/2019



* $V_{R1} = V_{R2} = v(t)$
 $\therefore R_1$ and R_2 are in parallel

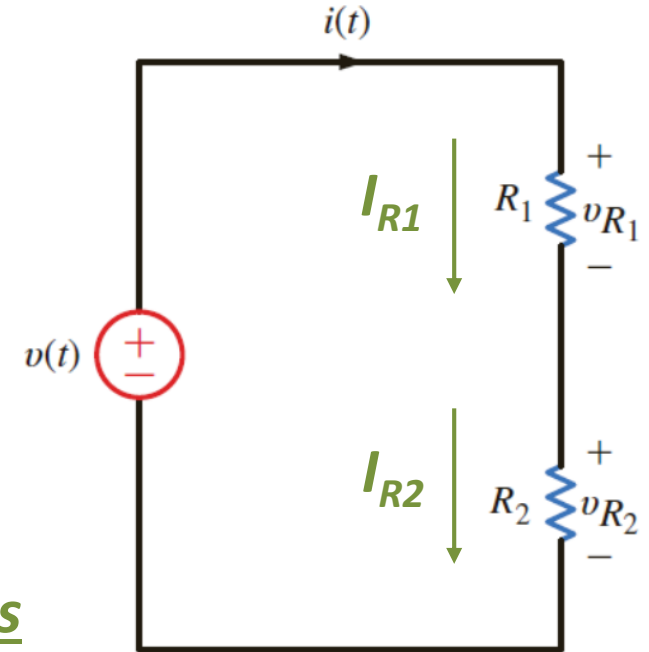
$$\therefore i_1(t) = \frac{R_2}{R_1 + R_2} \cdot i(t)$$

$$i_2(t) = \frac{R_1}{R_1 + R_2} \cdot i(t)$$

* $I_{R1} = I_{R2} = i(t)$
 $\therefore R_1$ and R_2 are in series

$$\therefore v_{R1} = \frac{R_1}{R_1 + R_2} \cdot v(t)$$

$$v_{R2} = \frac{R_2}{R_1 + R_2} \cdot v(t)$$



Last Lecture → Multiple Source/Resistor Networks

8/21/2019

- Series

The sum of several voltage source in series can be replaced by one source whose value is the algebraic sum of the individual source

The equivalent resistance of N resistors in series is simply the sum of the individual resistances.

$$R_s = R_1 + R_2 + \dots + R_N$$

- Parallel

The sum of several current source in series can be replaced by one source whose value is the algebraic sum of the individual source

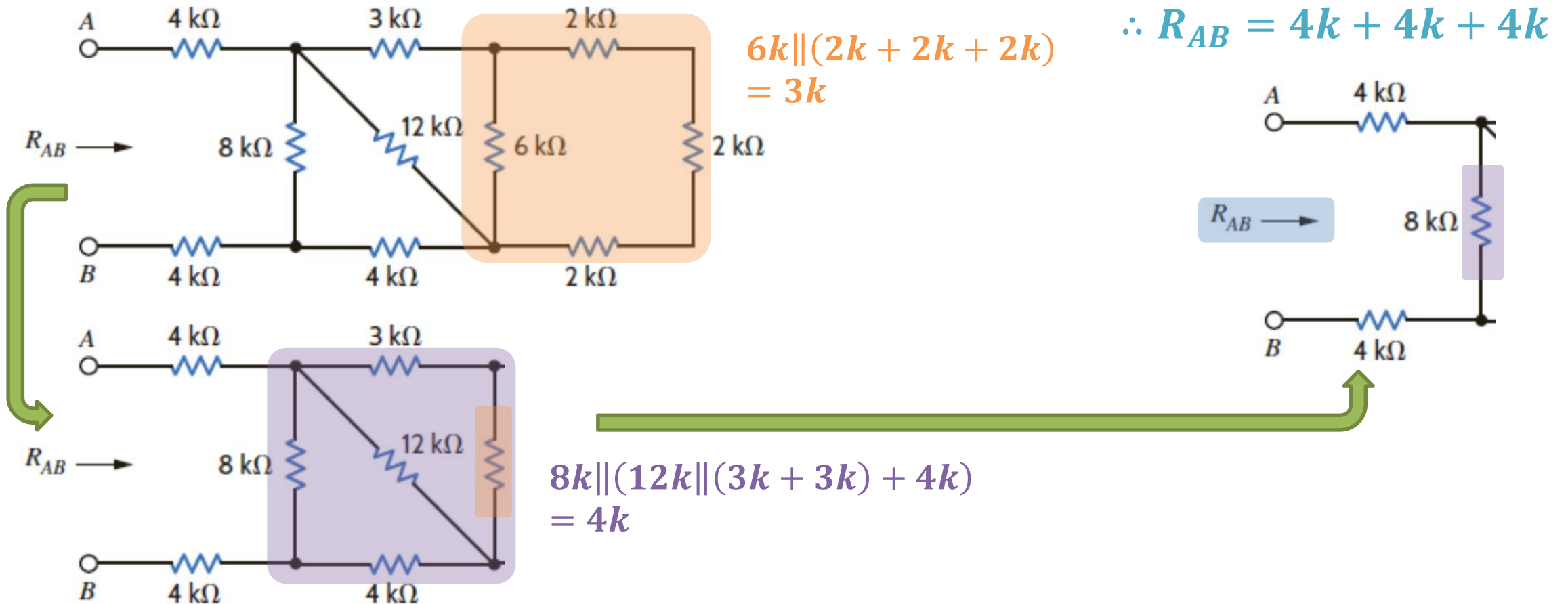
The reciprocal of the equivalent resistance of N resistors in parallel is equal to the sum of the reciprocal of the individual resistances.

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N}$$

Series/Parallel Resistor Combinations

8/21/2019

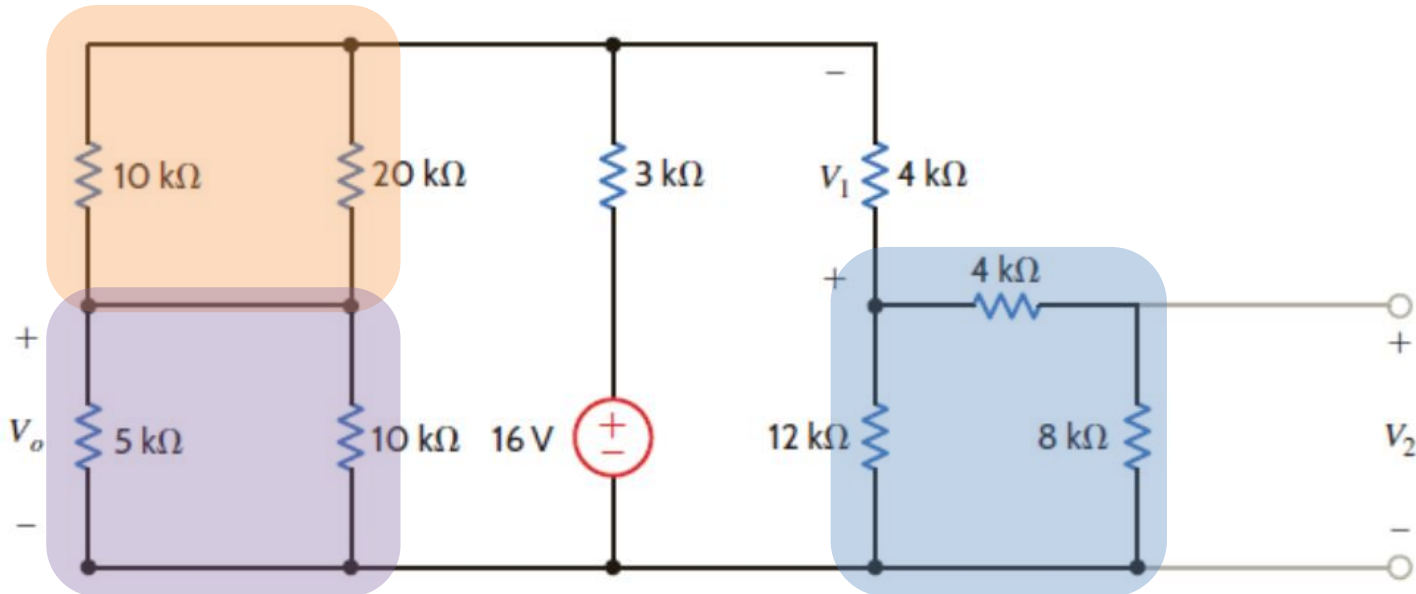
E2.16: Find R_{AB} in the provided network.



Learning Assessment E2.22

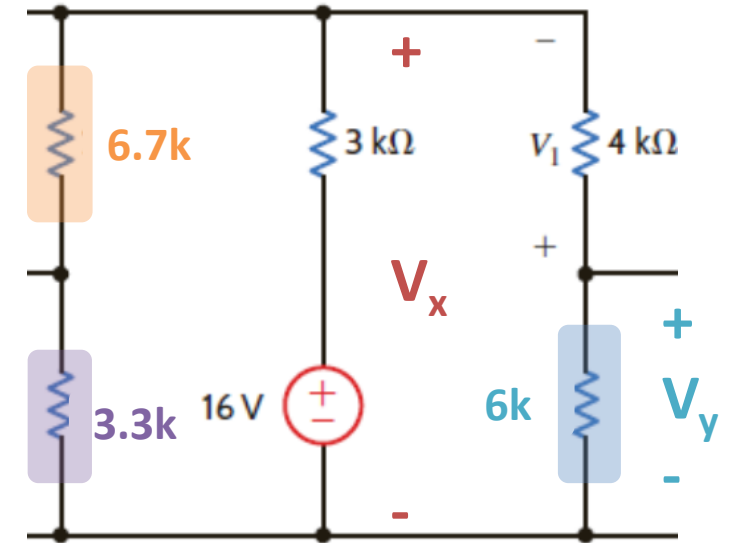
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Find V_0 , V_1 , and V_2 in the network provided.



$$V_0 = V_x \left[\frac{3.3k}{6.7k + 3.3k} \right] = 3.3V$$

$$V_2 = 6 \left[\frac{8k}{4k + 8k} \right] = 4V$$



$$V_x = 16 \left[\frac{10k \parallel 10k}{3k + 10k \parallel 10k} \right] = 10V$$

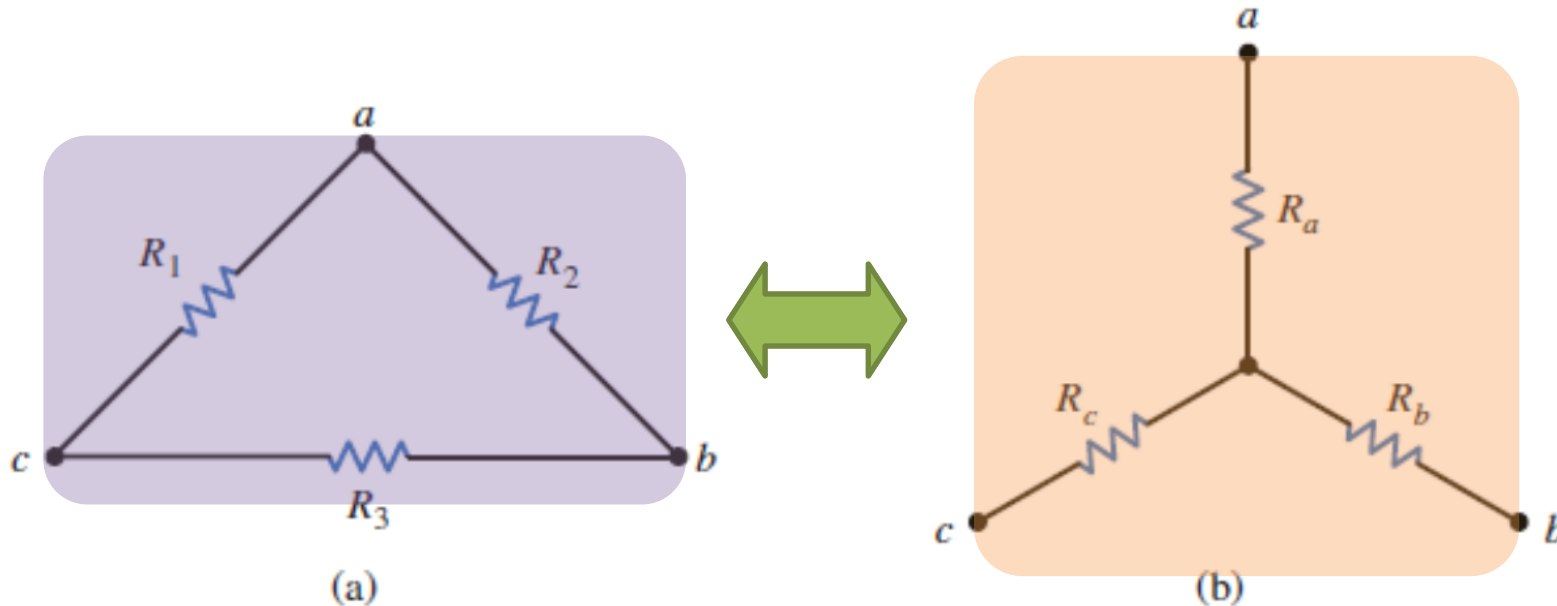
$$V_1 = -V_x \left[\frac{4k}{6k + 4k} \right] = -4V$$

$$V_y = V_x + V_1 = 10 - 4 = 6V$$

Wye \Leftrightarrow Delta Transformations

8/21/2019

For the two networks to be equivalent at each corresponding pair of terminals, it is necessary that the resistance at the corresponding terminals be equal (e.g., the resistance at terminals a and b with c open-circuited must be the same for both networks).


 $\Delta \leftarrow Y$

$$\left\{ \begin{array}{l} R_1 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_b} \\ R_2 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_c} \\ R_3 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_a} \end{array} \right.$$

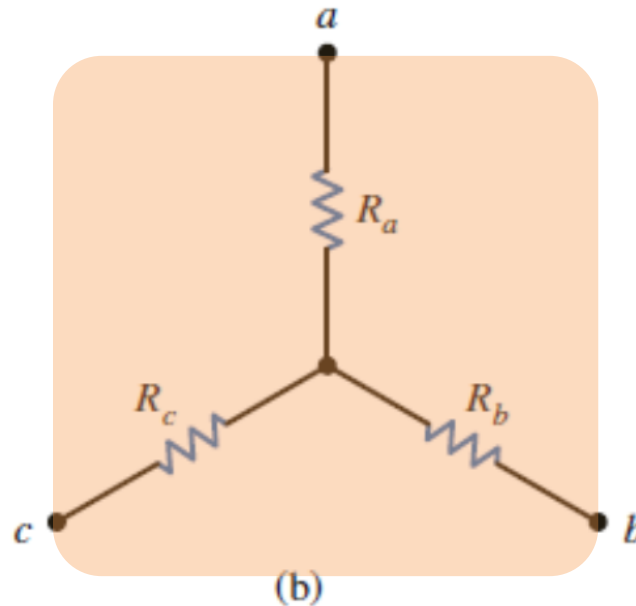
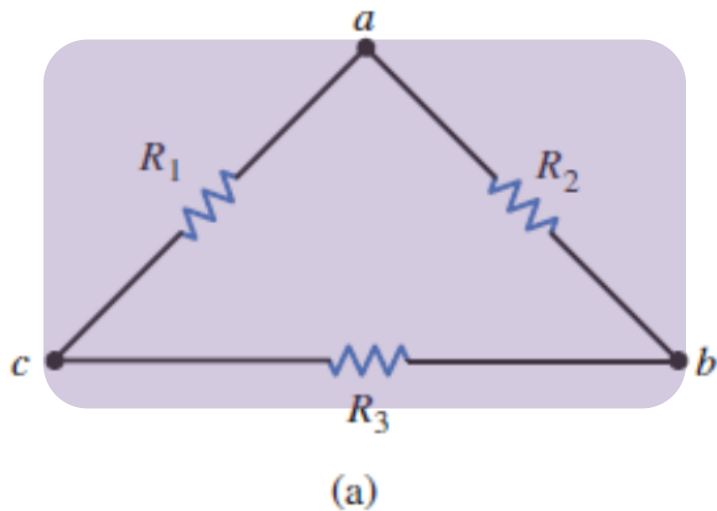
 $Y \leftarrow \Delta$

$$\left\{ \begin{array}{l} R_a = \frac{R_1 R_2}{R_1 + R_2 + R_3} \\ R_b = \frac{R_2 R_3}{R_1 + R_2 + R_3} \\ R_c = \frac{R_1 R_3}{R_1 + R_2 + R_3} \end{array} \right.$$

Wye \Leftrightarrow Delta Transformations

8/21/2019

For the two networks to be equivalent at each corresponding pair of terminals, it is necessary that the resistance at the corresponding terminals be equal (e.g., the resistance at terminals a and b with c open-circuited must be the same for both networks).



... for $R_a = R_b = R_c = R_Y$
 $R_1 = R_2 = R_3 = R_\Delta$

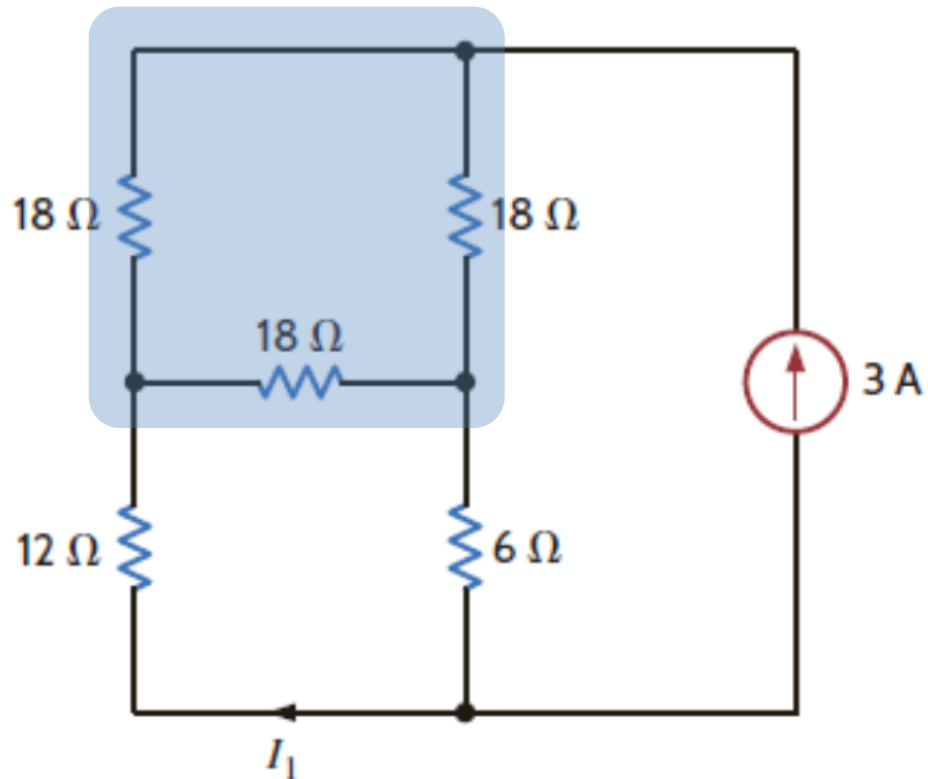
$\Delta \leftarrow Y$ $\left\{ R_\Delta = 3R_Y$

$Y \leftarrow \Delta$ $\left\{ R_Y = \frac{1}{3}R_\Delta$

Learning Assessment E2.26

8/21/2019

Find I_1 in the network provided.



Circuits with Dependent Sources

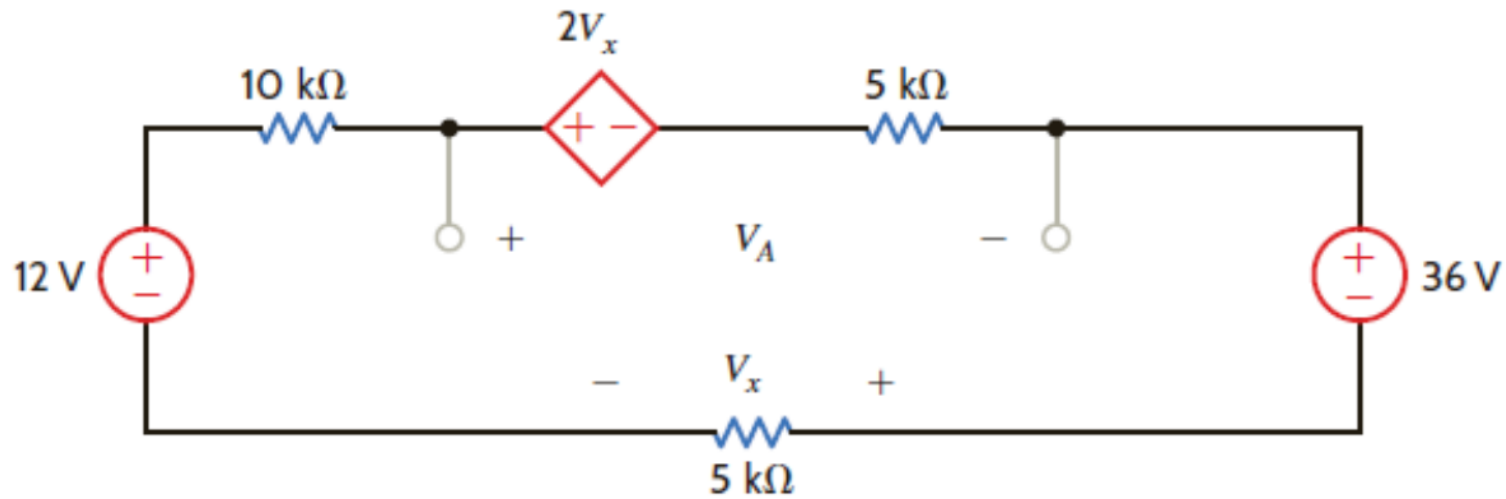
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- 1) Write KVL and/or KCL equations for the network
→ treat the dependent CS as an independent CS
- 2) Write the equation that specifies the relationship of the dependent source to the controlling parameter.
- 3) Solve the equations for the unknowns.
→ Be sure the number of linearly independent equations matches the number of unknowns.

Learning Assessment E2.29

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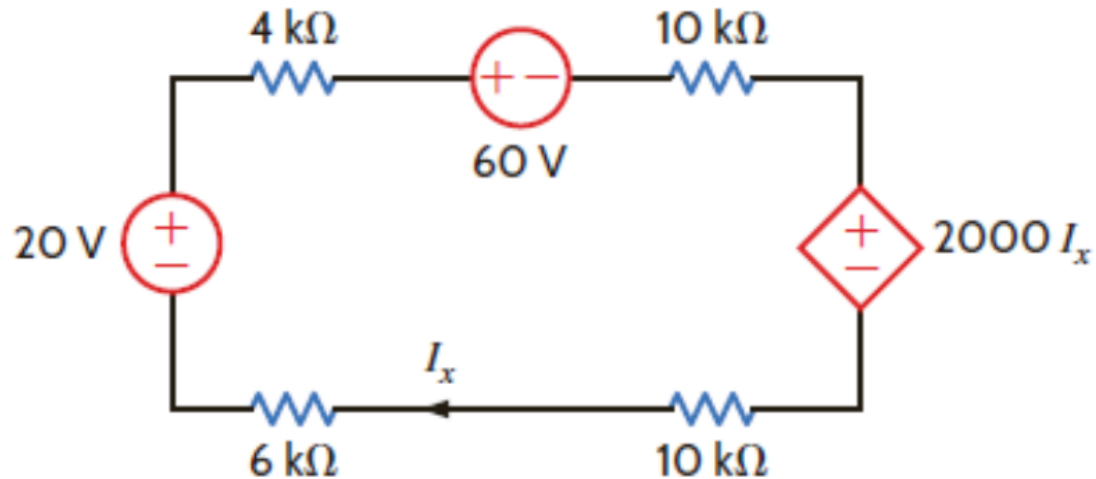
Find V_A in the network provided.



Problem 2.35

8/21/2019

Find the power absorbed by the dependent source in the circuit provided.



Nodal and Loop Analysis → Chapter #3

8/21/2019

- Solve circuits with multiple nodes using nodal analysis
- Solve circuits with multiple loops using loop analysis
- Identify the most appropriate analysis technique that should be utilized to solve a particular problem

Nodal Analysis

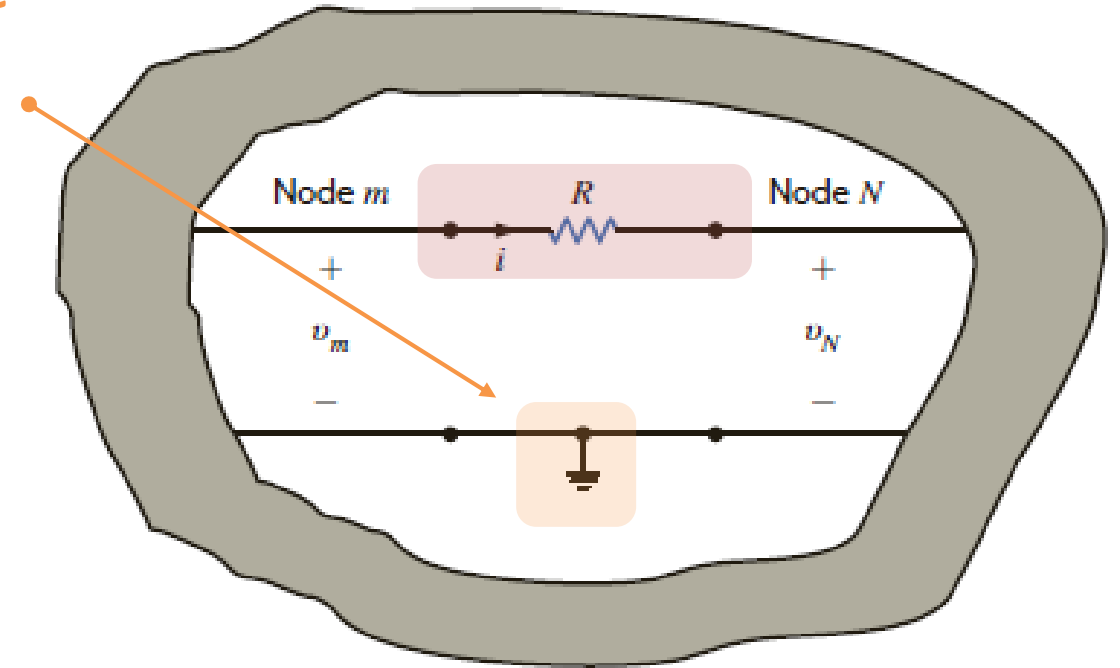
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- One node is selected as the reference node
- KCL is applied to the remaining $N-1$ nodes

Ohm's Law:

$$i = \frac{v_m - v_n}{R}$$

- Current defined by Ohm's law
- Variables are node voltages
- Voltages are defined with respect to a common point (the reference)

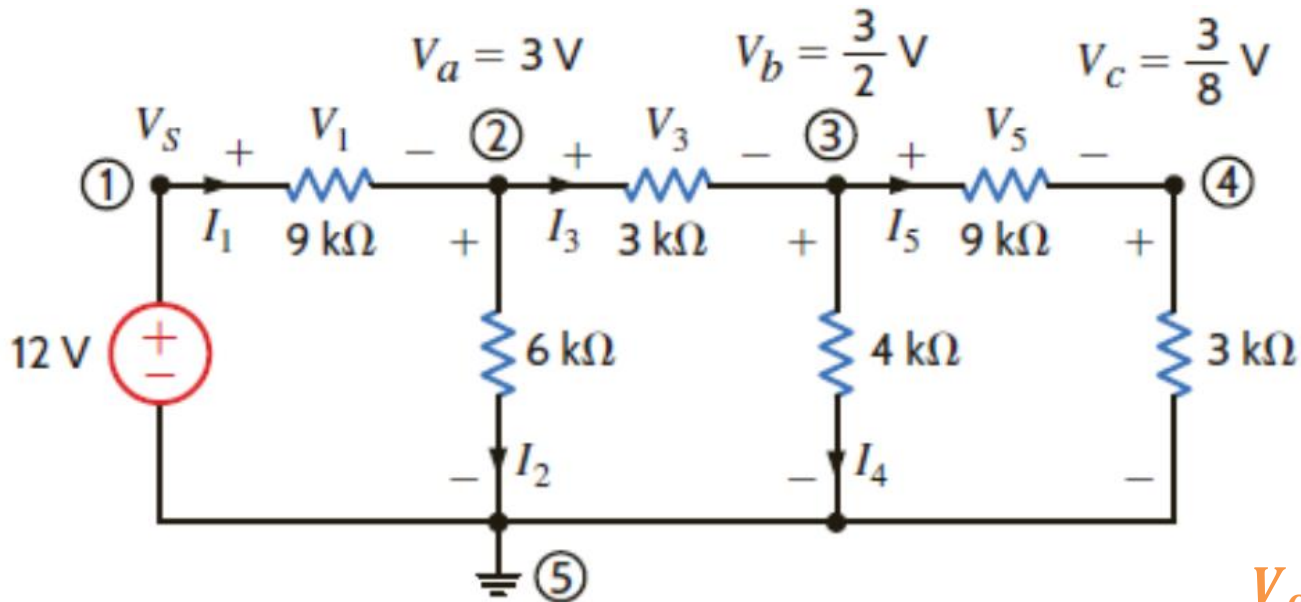


N-1 independent simultaneous equations!

Nodal Analysis → Known Node Voltages

8/21/2019

- Define node voltages to be positive with respect to the reference node
- Define currents with respect to node voltages



- Voltage across resistors

$$V_1 = V_S - V_a = 9\text{ V}$$

$$V_3 = V_a - V_b = \frac{3}{2}\text{ V}$$

$$V_5 = V_b - V_c = \frac{9}{8}\text{ V}$$

- Current in resistors

$$I_1 = \frac{V_1}{9k} = \frac{V_S - V_a}{9k} = 1\text{ mA}$$

$$I_3 = \frac{V_3}{3k} = \frac{V_a - V_b}{3k} = \frac{1}{2}\text{ mA}$$

$$I_5 = \frac{V_5}{9k} = \frac{V_b - V_c}{9k} = \frac{1}{8}\text{ mA}$$

$$I_2 = \frac{V_a - 0}{6k} = \frac{1}{2}\text{ mA}$$

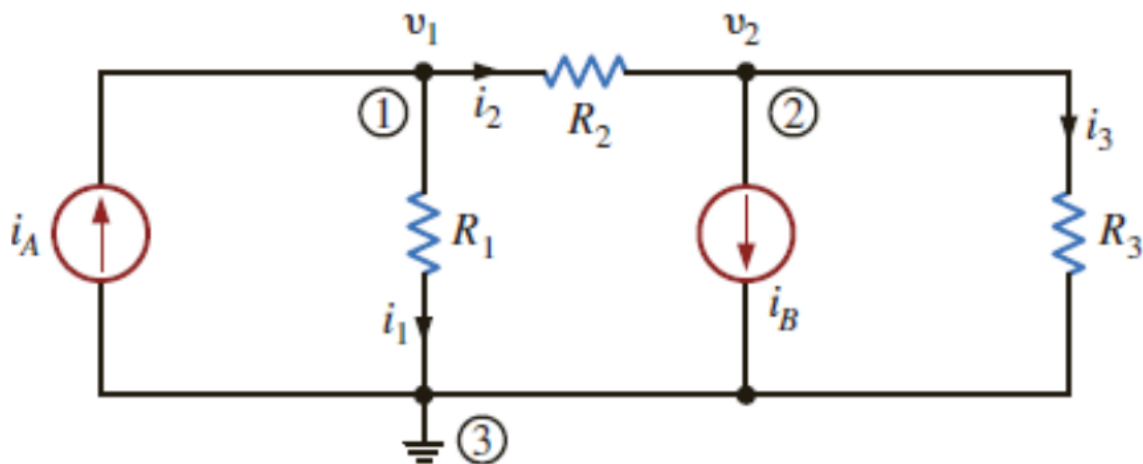
$$I_4 = \frac{V_b - 0}{4k} = \frac{3}{8}\text{ mA}$$

Nodal Analysis → with Independent CS

8/21/2019

- 1) Identify #of nodes: **3 node circuit**
- 2) Select reference node: **bottom node, 3**
- 3) Label other node voltages: v_1, v_2
- 4) Identify branch currents: i_1, i_2, i_3
- 5) Apply KCL to nodes: **1, 2** → **2 independent equations**

assume: $I_A = 1mA$ $R_1 = 12k\Omega$
 $I_B = 4mA$ $R_2 = 6k\Omega$
 $R_3 = 6k\Omega$



KCLs: $I_A = I_1 + I_2 = \frac{V_1}{R_1} + \frac{V_1 - V_2}{R_2} = V_1 \left[\frac{1}{R_1} + \frac{1}{R_2} \right] - V_2 \left[\frac{1}{R_2} \right]$

$I_B = I_2 + I_3 = \frac{V_1 - V_2}{R_2} - \frac{V_2}{R_3} = V_1 \left[\frac{1}{R_2} \right] - V_2 \left[\frac{1}{R_2} + \frac{1}{R_3} \right]$

matrix eq.

$$\begin{bmatrix} I_A \\ I_B \end{bmatrix} = \begin{bmatrix} \frac{1}{R_1 \parallel R_2} & -\frac{1}{R_2} \\ \frac{1}{R_2} & -\frac{1}{R_2 \parallel R_3} \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$