

# Exam #2 → Thursday, October 17

10/4/2019

## Concepts Chapter #5:

- 1) Superposition
- 2) Thevenin's & Norton's Theorem
- 3) Source Transformation
- 4) Maximum Power Transfer

## Concepts Chapter #6:

- 1) Capacitors
- 2) Inductors

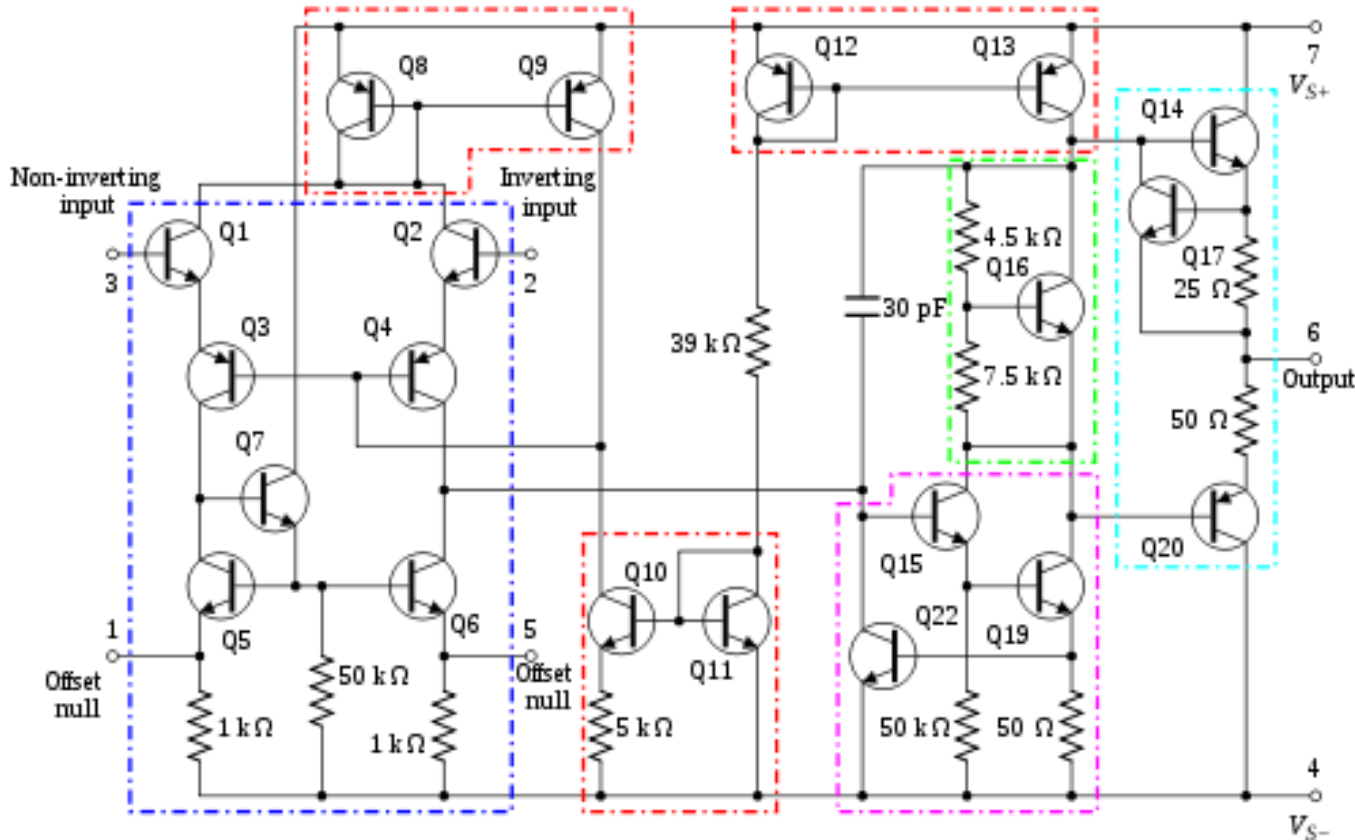
## Concepts Chapter #4:

- 1) Op-Amps – Model
- 2) Op-Amps - Analysis

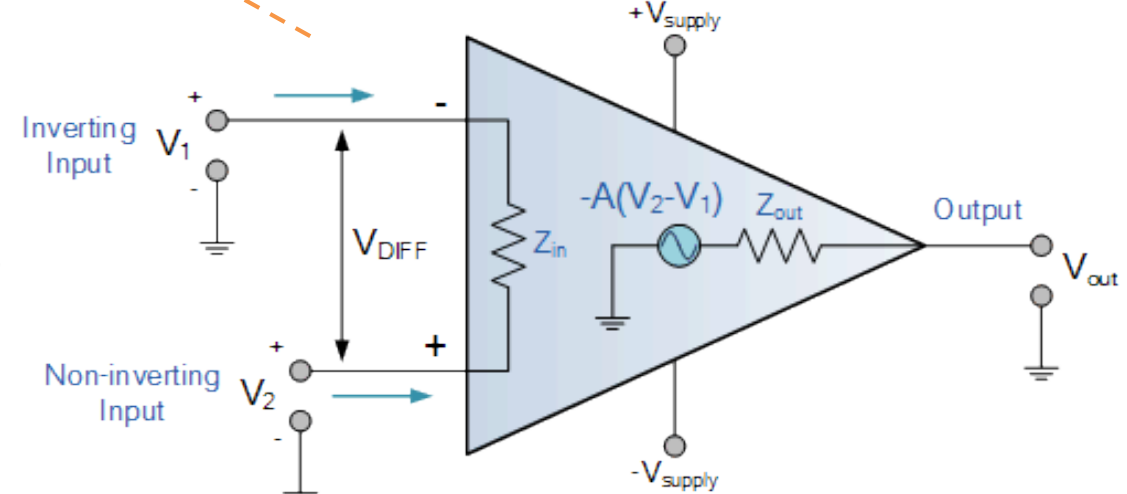
# Last Lecture → Operational Amplifier

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- Internal Circuit Diagram



- Symbol / Equivalent Circuit

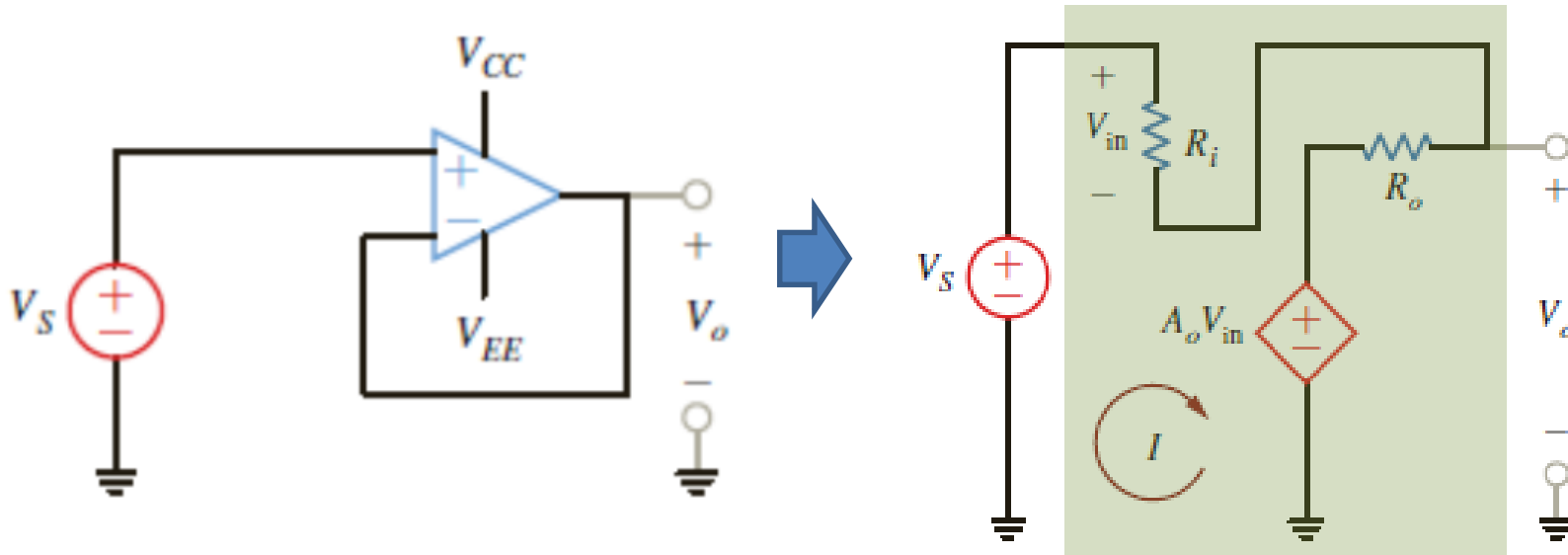


$$V_0 = A_0(IN_+ - IN_-)$$

# Last Lecture → Non-Ideal Analysis

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Using the op-amp model find the expression for the transfer function  $V_o/V_s$ .



## Op-Amp Ideal Behavior

- $R_i = \infty$
- $A_0 = \infty$
- $R_o = 0$

$$i_{R_i} = \frac{V_{in}}{R_i} = 0$$

$$\therefore i_+ = i_- = 0$$

$$\frac{V_o}{V_s} = \frac{1}{1 + \frac{1}{A_0 + \frac{R_o}{R_i}}} \approx \frac{1}{1 + \frac{1}{A_0}} \approx 1$$

$R_i = \infty, R_o = 0$        $A_0 = \infty$

$$V_o = A_0(V_+ - V_-)$$

$$\hookrightarrow (V_+ - V_-) = \frac{V_o}{A_0} = 0 \quad \therefore V_+ = V_-$$

# Last Lecture → Ideal Analysis

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- Establish ideal op-amp conditions on the circuit schematic
- Write nodal equations at the op-amp input terminals
- Solve for the input/output relationship

MODEL ASSUMPTION

$A_o \rightarrow \infty$

$R_f \rightarrow \infty$

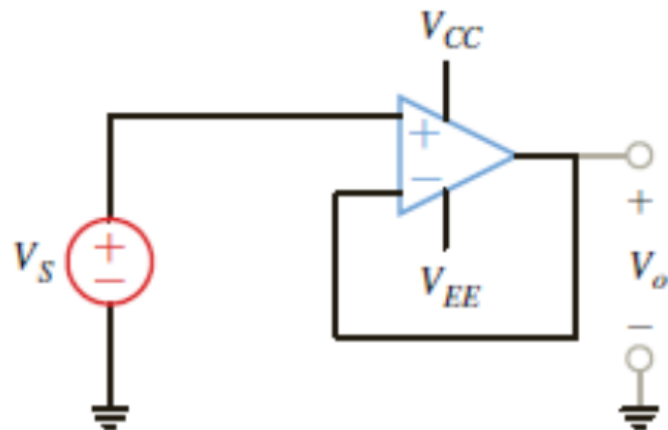
TERMINAL RESULT

input voltage  $\rightarrow 0$  Vinput current  $\rightarrow 0$  A

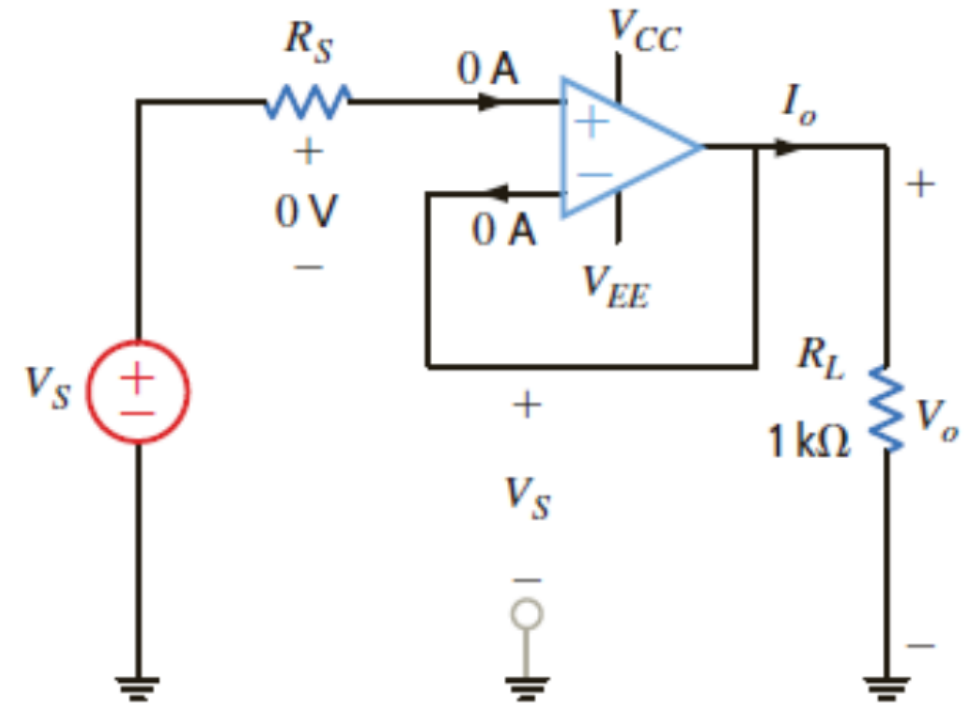
$V_+ = V_-$

$i_+ = i_- = 0$

## Unity Gain Buffer - Revisited



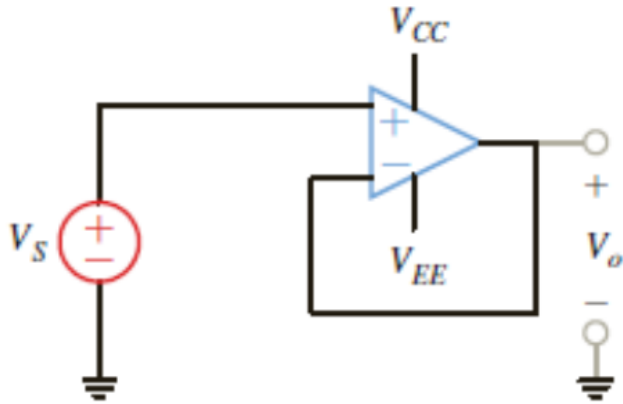
$$\therefore V_o = V_S$$



# Last Lecture → Basic Circuits

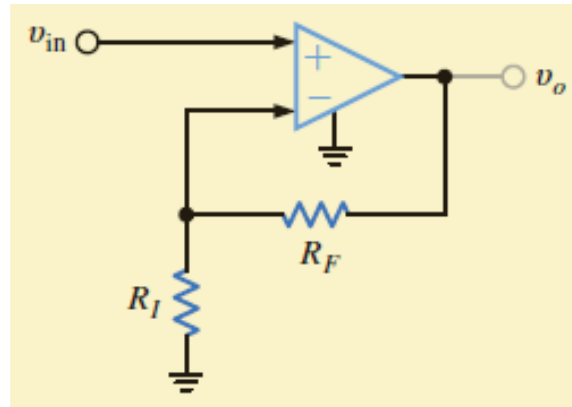
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- Unity – Gain Amp.



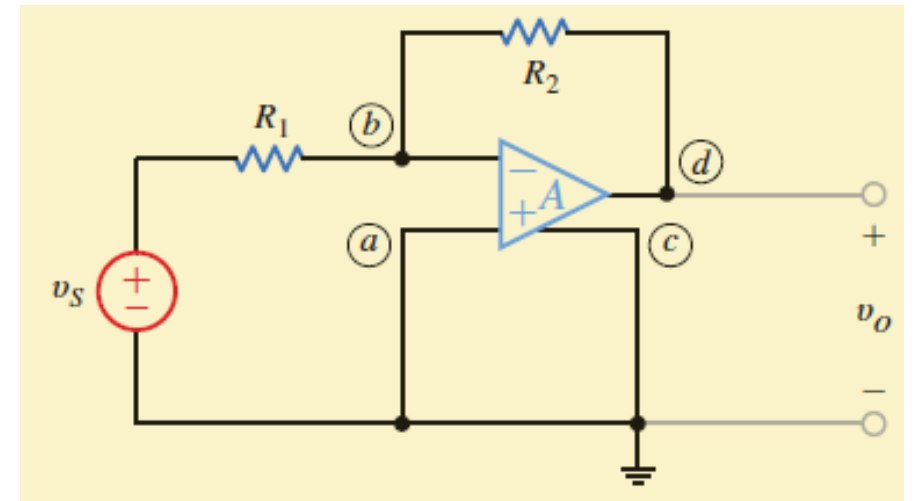
$$\frac{V_o}{V_s} \approx 1$$

- Non-Inverting Amp.



$$\frac{V_o}{V_s} \approx 1 + \frac{R_F}{R_I}$$

- Inverting Amp

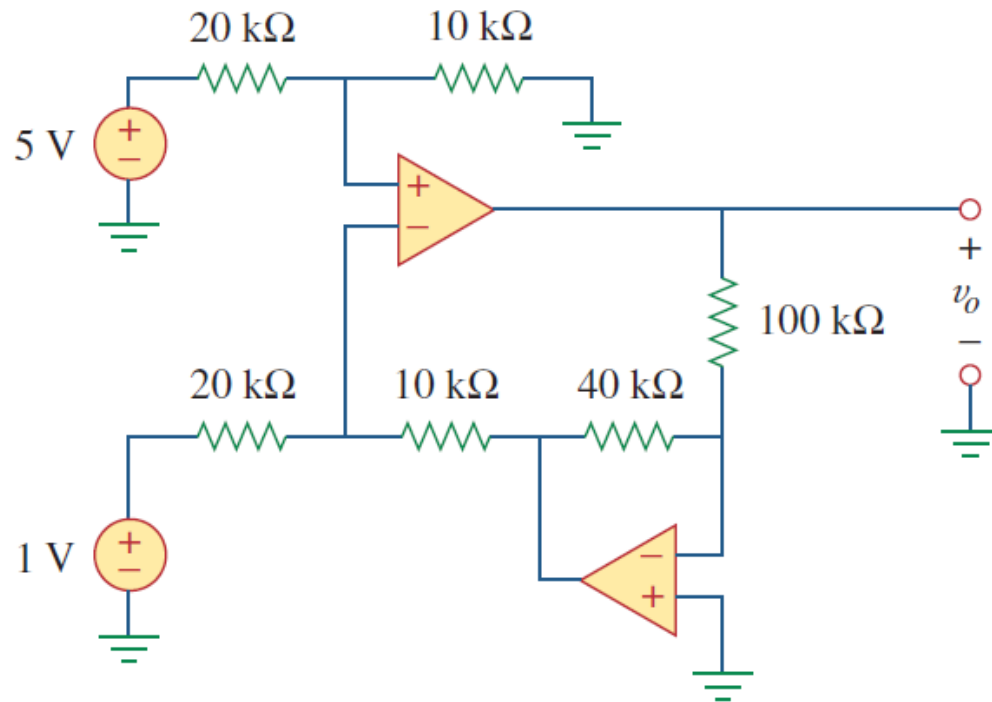


$$\frac{V_o}{V_s} \approx -\frac{R_2}{R_1}$$

# Problem

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Determine  $v_o$  in the circuit provided.



# Capacitance and Inductance → Chapter #5

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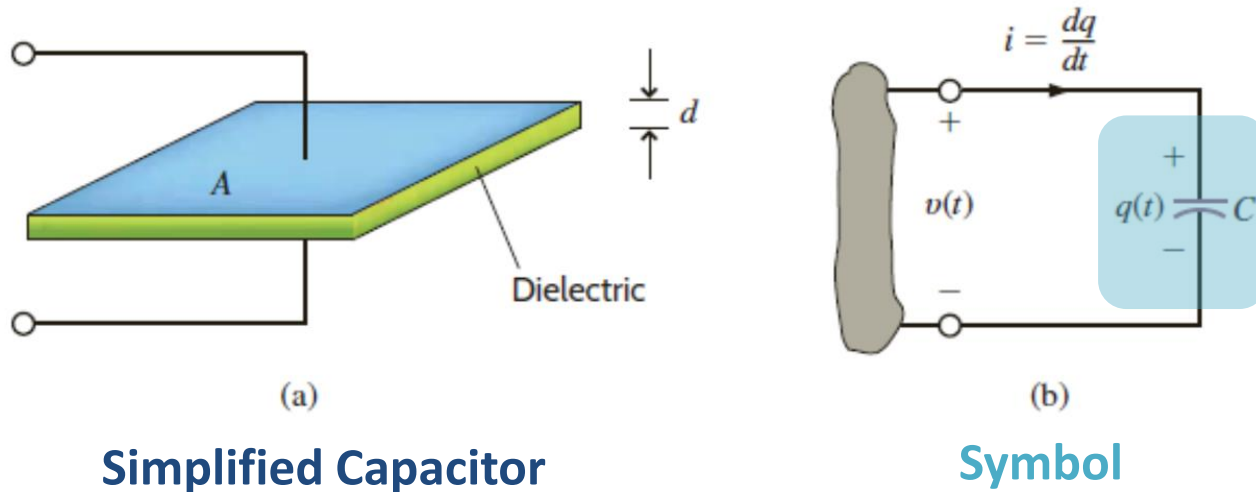
- Inductor / Capacitor Model → voltages, currents, powers, stored energy
- Concept of Continuity → inductor: current, capacitor: voltage
- Circuit Analysis with DC Sources
- Equivalent Inductance /Capacitance → series & parallel

# Capacitor

Typical  
Capacitors



... a circuit element that consists of two conducting surfaces separated by dielectric material



Capacitance (C)  $\rightarrow C = \frac{\epsilon_0 A}{d}$

$\epsilon_0$  ← permittivity of free space



Unit  $\rightarrow$  farads (F) = coulombs per volts

$$q = C \cdot v \quad i = C \cdot \frac{dv}{dt}$$

$$v(t) = v(t_0) + \frac{1}{C} \cdot \int_{t_0}^t i(x) dx$$

$$p(t) = C \cdot v(t) \frac{dv(t)}{dt}$$

$$w_c(t) = \frac{1}{2} C \cdot v(t)^2$$



# Example 6.1

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If the charge accumulated on two parallel conductors charge to 12V is 600 pC, what is the capacitance of the parallel conductors?

$$v = 12V \quad q = 600 \text{ pC}$$

$$q = C \cdot v \quad \underbrace{\hspace{1.5cm}}_{\rightarrow} \quad C = \frac{q}{v} = \frac{600\text{p}}{12} = 50\text{pF}$$

# Example 6.2

10/4/2019

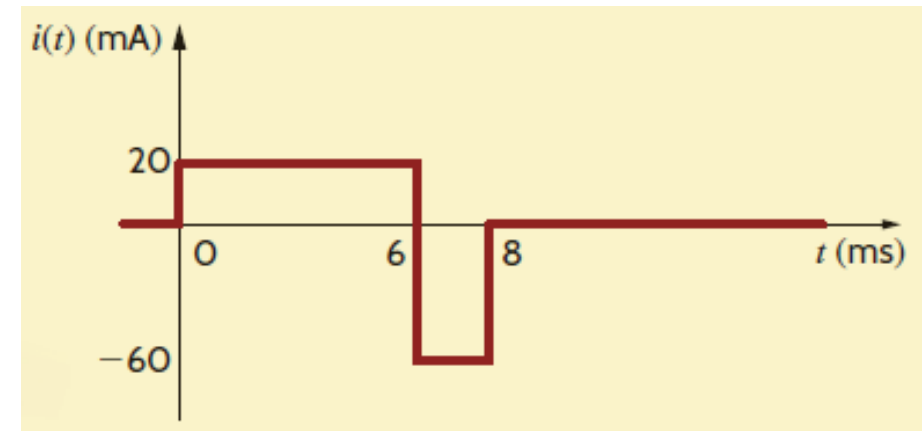
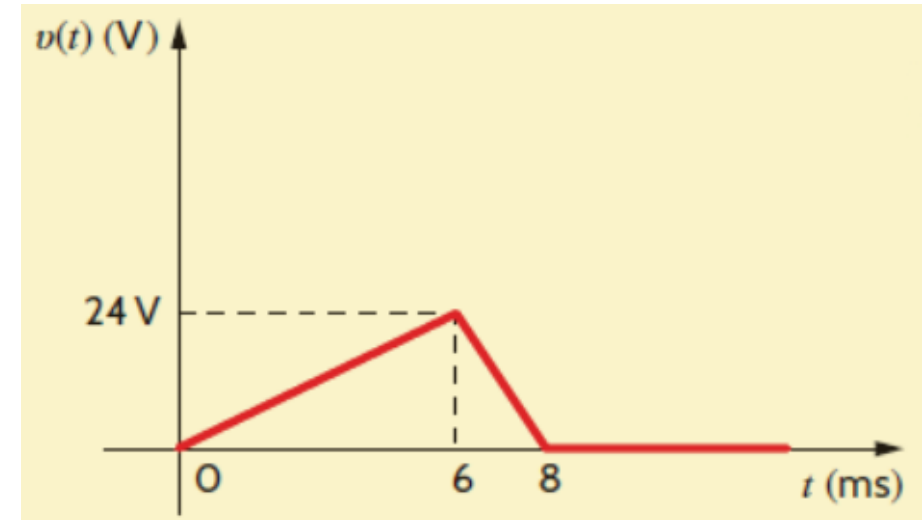
If voltage across a 5- $\mu\text{F}$  capacitor has the waveform shown below, determine the current waveform?

$$v(t) = 4k \cdot t \rightarrow t = [0: 6]$$

$$24 - 12k \cdot (t - 6m) \rightarrow t = [6: 8]$$

$$0 \rightarrow t = [8: \infty]$$

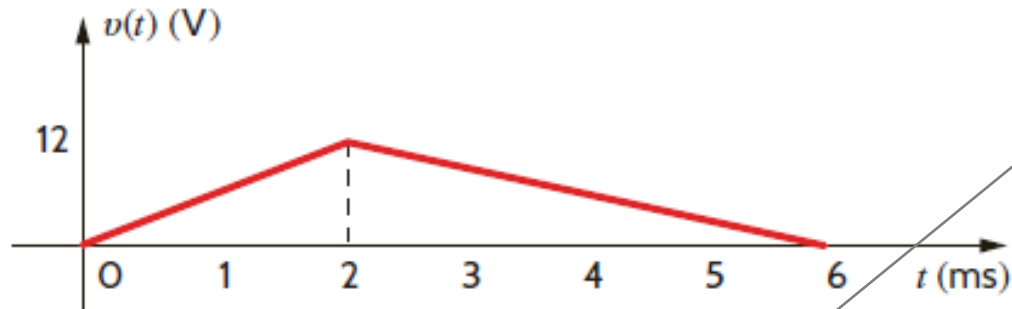
$$i = C \cdot \frac{dv}{dt} = ?$$



# Learning Assessment E6.2-E6.3

10/4/2019

The voltage across a 2- $\mu\text{F}$  capacitor is provided below. Determine the waveforms for the current, power, and energy and compute the energy stored in the electric field of the capacitor at  $t=2\text{ms}$ .



$$v(t) =$$

$$i = C \cdot \frac{dv}{dt} =$$

$$p(t) = C \cdot v(t) \frac{dv(t)}{dt} =$$

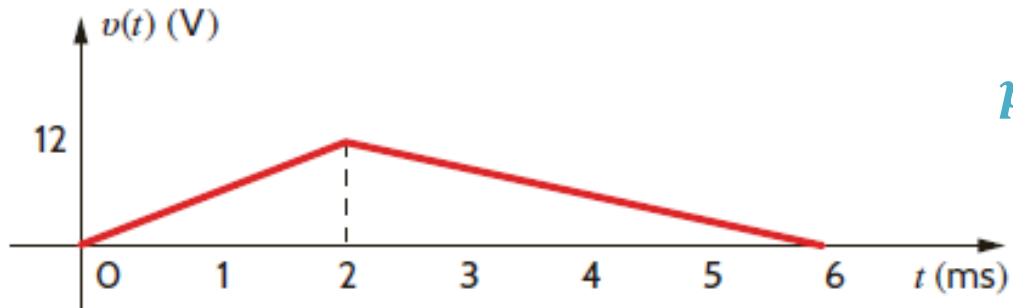
$$w_c(t) = \frac{1}{2} C \cdot v(t)^2 =$$

$$w_c(t = 2\text{m}) =$$

# Learning Assessment E6.2-E6.3

10/4/2019

The voltage across a 2- $\mu\text{F}$  capacitor is provided below. Determine the waveforms for the current, power, and energy and compute the energy stored in the electric field of the capacitor at  $t=2\text{ms}$ .



$$p(t) = C \cdot v(t) \frac{dv(t)}{dt} = 72 \cdot t \text{ W} \rightarrow t = [0:2]$$

$$-72 + 18 \cdot (t - 2\text{m}) \text{ W} \rightarrow t = [2:6]$$

$$v(t) = 6k \cdot t \rightarrow t = [0:2]$$

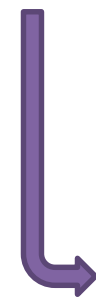
$$12 - 3k \cdot (t - 2\text{m}) \rightarrow t = [2:6]$$

$$i = C \cdot \frac{dv}{dt} = 12 \text{ mA} \rightarrow t = [0:2]$$

$$-6 \text{ mA} \rightarrow t = [2:6]$$

$$w_c(t) = \frac{1}{2} C \cdot v(t)^2 = 36 \cdot t^2 \text{ J} \rightarrow t = [0:2]$$

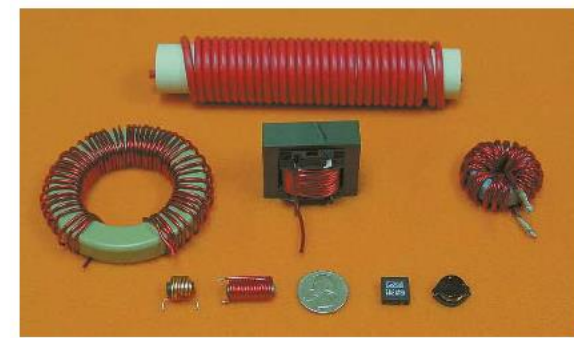
$$[17 - 3k \cdot t]^2 \text{ uJ} \rightarrow t = [2:6]$$



$$w_c(t = 2\text{m}) = 144 \text{ uJ}$$

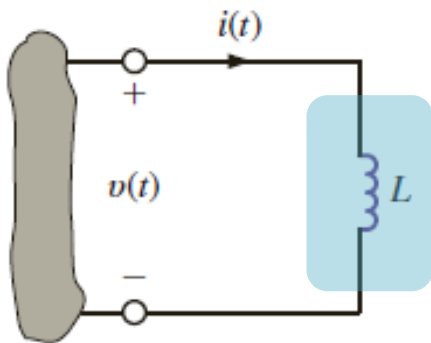
# Inductor

Typical  
Inductors

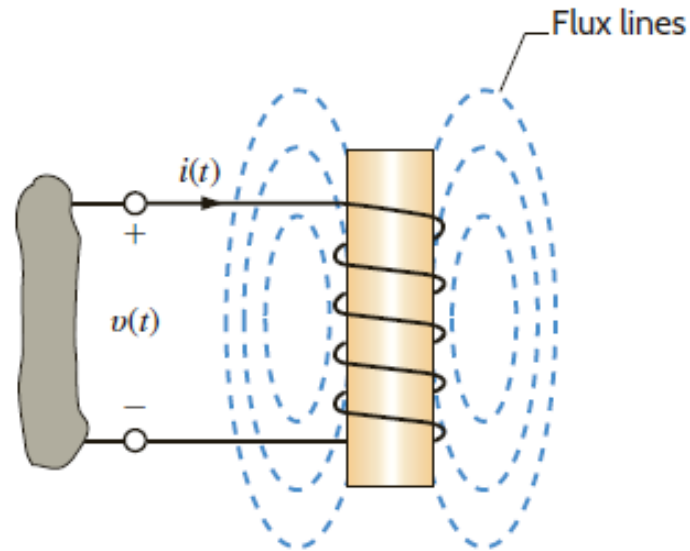


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... a circuit element that consists of a conducting wire usually in the form of a coil.



Symbol



Simplified Inductor

Inductance (L)



Unit → Henry (H) = 1 volt-second per ampere

$$v = L \cdot \frac{di}{dt}$$

$$i(t) = i(t_0) + \frac{1}{L} \cdot \int_{t_0}^t v(x) dx$$

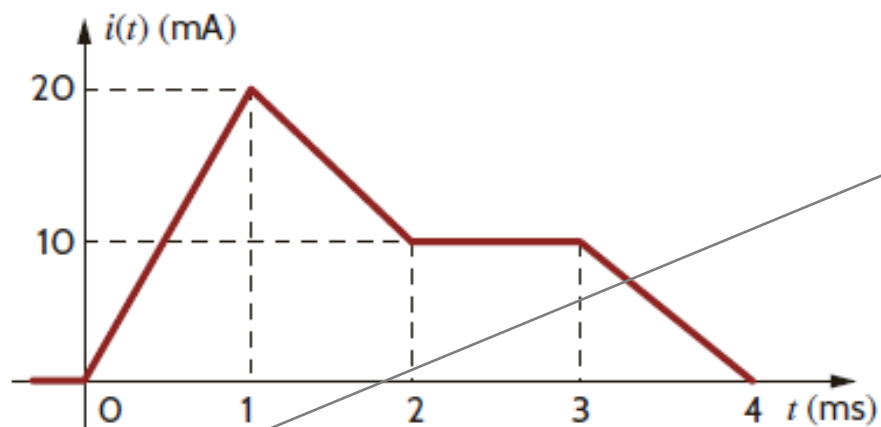
$$p(t) = L \cdot i(t) \frac{di(t)}{dt}$$

$$w_L(t) = \frac{1}{2} L \cdot i(t)^2$$

# Learning Assessment E6.6-E6.7

10/4/2019

The current across a 5-mH inductor is provided below. Determine the waveforms for the voltage, power, and energy and compute the energy stored in the magnetic field of the inductor at  $t=1.5\text{ms}$ .



$i(t) =$

$$v = L \cdot \frac{di}{dt} =$$

$$p(t) = L \cdot i(t) \frac{di(t)}{dt} =$$

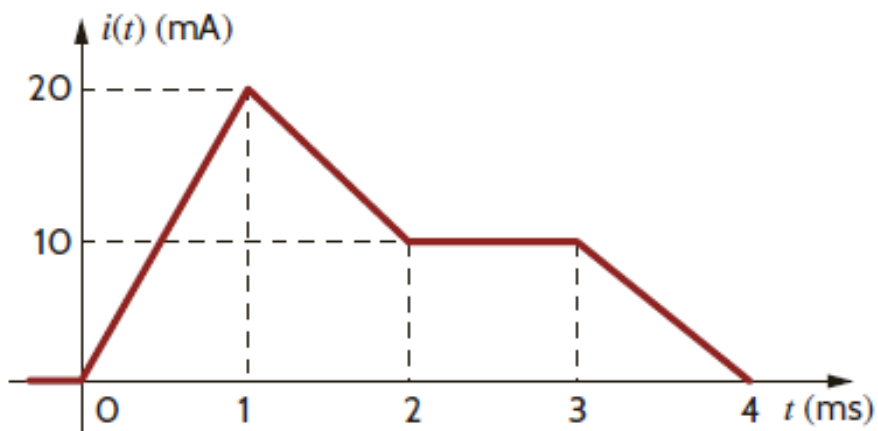
$$w_L(t) = \frac{1}{2} L \cdot i(t)^2 =$$

$$w_L(t = 1.5\text{m}) =$$

# Learning Assessment E6.6-E6.7

10/4/2019

The current across a 5-mH inductor is provided below. Determine the waveforms for the voltage, power, and energy and compute the energy stored in the magnetic field of the inductor at  $t=1.5\text{ms}$ .



$$i(t) = \begin{aligned} & 20 \cdot t \text{ A} \rightarrow t = [0:1] \\ & 20\text{m} - 10 \cdot (t - 1\text{m}) \text{ A} \rightarrow t = [1:2] \\ & 10 \text{ mA} \rightarrow t = [2:3] \\ & 10\text{m} - 10 \cdot (t - 3\text{m}) \text{ A} \rightarrow t = [3:4] \end{aligned}$$

$$v = L \cdot \frac{di}{dt} = \begin{aligned} & 100 \text{ mV} \rightarrow t = [0:1] \\ & -50 \text{ mV} \rightarrow t = [1:2] \\ & 0 \rightarrow t = [2:3] \\ & -50 \text{ mV} \rightarrow t = [3:4] \end{aligned}$$

$$p(t) = L \cdot i(t) \frac{di(t)}{dt} = \begin{aligned} & 2 \cdot t \text{ W} \rightarrow t = [0:1] \\ & -1\text{m} + 0.5 \cdot (t - 1\text{m}) \text{ W} \rightarrow t = [1:2] \\ & 0 \rightarrow t = [2:3] \\ & -0.5\text{m} + 0.5 \cdot (t - 3\text{m}) \text{ W} \rightarrow t = [3:4] \end{aligned}$$

$$w_L(t) = \frac{1}{2} L \cdot i(t)^2 = \begin{aligned} & t^2 \text{ J} \rightarrow t = [0:1] \\ & 2.5 \cdot [30\text{m} - 10 \cdot t]^2 \text{ mJ} \rightarrow t = [1:2] \\ & 250 \text{ nJ} \rightarrow t = [2:3] \\ & 2.5 \cdot [40\text{m} - 10 \cdot t]^2 \text{ mJ} \rightarrow t = [3:4] \end{aligned}$$

$\downarrow$   
 $w_L(t = 1.5\text{m}) = 562 \text{ nJ}$