## Last Lecture $\rightarrow$ Chapter \#1

## System of Units

$\checkmark$ Basic Electrical Quantities
$\checkmark$ Independent Sources
Circuit Analysis

- Independent Sources


$$
\begin{aligned}
& \begin{array}{l}
\text { apter \#1 } \\
\text { its } \\
\text { al Quantities } \\
\text { Sources } \\
\text { is }
\end{array} \\
& \boldsymbol{i}(t)=\frac{d q(t)}{d t} \quad[\mathrm{~A}=\mathrm{C} / \mathrm{s}] \\
& v(t)=\frac{d w(t)}{d q} \quad[\mathrm{~N}=\mathrm{m}] \\
& p=\frac{d w}{d t}=v \cdot i \quad[\mathrm{~W}=\mathrm{J} / \mathrm{s}] \\
& \text { s passive sign convention: positive power is defined as the current }
\end{aligned}
$$

$i(t)$ entering the positive reference $v(t)$ of the element

- Power positive - power being absorbed
- Power negative - power being supplied


## Dependent Source

Generate a voltage or current that is determined by another voltage or current at specified location in the circuit.

(c)

Voltage Controlled Current Source (VCCS)

Current Controlled Voltage Source (CCVS)

(b)

(d)

Current Controlled
Current Source (CCCS)

## Example 1.7

Use Tellegen's theorem to find the current $I_{0}$ in the network provided.

$$
\begin{aligned}
& \text { - } P_{1}=6 \cdot I_{0} \\
& \text { - } P_{2}=12 \cdot(-9)=-108 \mathrm{~W} \\
& \text { - } P_{3}=10 \cdot(-3)=-30 W \\
& \text { - } P_{V S}=4 \cdot(-8)=-32 W \\
& \text { - } P_{C S}=6 \cdot(-2)=-12 \mathrm{~W} \\
& \text { - } P_{C C V S}=8 I_{x} \cdot 11=176 \mathrm{~W} \\
& \sum_{i}^{N} P_{i}=0 \\
& \Rightarrow P_{1}=6 \cdot I_{0}=6 \mathrm{~W} \\
& \therefore I_{0}=1 A
\end{aligned}
$$



## Resistive Circuits $\rightarrow$ Chapter \#2

- Ohm's Law
- Kirchhoff's Current and Voltage Law
- Basic Circuit Analysis
- Equivalent Resistance
- Voltage and Current Division
- Wye and Delta Resistor Networks
- Circuit Analysis with Dependent Sources
- Basic Electrical Quantities
- Independent \& Dependent Sources
- Circuit Analysis


## Ohm's Law

States that the voltage across a resistance is directly proportional to the current flowing through it.


A circuit element whose electrical characteristic is primarily resistive is called a resistor ( $R$ ) .

## Ohm's Law

- Resistance [ $\Omega=\mathrm{V} / \mathrm{A}$ ]

$$
R=\frac{v(t)}{i(t)}
$$

- Conductance [S = A/V]

$$
G=\frac{1}{R}=\frac{i(t)}{v(t)}
$$



- Power Dissipation [W]

$$
\boldsymbol{p}(\boldsymbol{t})=\boldsymbol{v}(\boldsymbol{t}) \cdot \boldsymbol{i}(\boldsymbol{t})=\boldsymbol{R} \cdot i(t)^{2}=\frac{v(t)^{2}}{R}
$$

Resistor Types

## Ohm's Law

## Short-Circuit \& Open-Circuit Description



$$
v(t)=R \cdot i(t)
$$


(b)

$$
\text { for } \boldsymbol{R} \rightarrow \mathbf{0}
$$

$$
v(t)=R \cdot i(t)=0
$$

$\therefore$ short circuit!

(c)

$$
\text { for } R \rightarrow \infty
$$

$$
i(t)=\frac{v(t)}{R}=0
$$

$\therefore$ open circuit!

## Example 2.1

Determine the current and the power absorbed by the resistor.


## Example 2.2

Determine the voltage and the current in the circuit.


## Example 2.3

Find the value of the voltage source and the power absorbed by the resistance.


## Example 2.4

Find the value of the resistance and the voltage across the current source


Kirchhoff's Laws $\rightarrow$ Chapter \#2.2

- Kirchhoff's Current Law (KCL)
- Kirchhoff's Voltage Law (KVL)
- Node: a point of connection of two or more circuit elements
- Loop: any closed path through the circuit in which no node is encountered more than once
- Branch: a portion of the circuit containing a single element and the node at each end of the elements



## Kirchhoff's Current Law

... the algebraic sum of the all the currents entering any node is zero


$$
\sum_{j=1}^{N} i_{j}^{i n}(t)=\sum_{i=1}^{M} i_{i}^{\text {out }}
$$

$$
\begin{aligned}
& \operatorname{KCL}(1): i_{1}(t)-i_{2}(t)-i_{3}(t)=\mathbf{0} \\
& \operatorname{KCL}(2): i_{4}(t)-i_{1}(t)-\boldsymbol{i}_{6}(t)=0 \\
& \operatorname{KCL}(3): i_{2}(t)+i_{5}(t)-i_{4}(t)-i_{7}(t)=\mathbf{0} \\
& \operatorname{KCL}(4): i_{3}(t)+i_{8}(t)-i_{5}(t)=\mathbf{0} \\
& \operatorname{KCL}(5): \boldsymbol{i}_{6}(t)+i_{7}(t)-i_{8}(t)=\mathbf{0}
\end{aligned}
$$


(5)

## Learning Assessments $\rightarrow$ E2.5b

... find $\mathrm{I}_{1}$, and $\mathrm{I}_{2}$ in the circuit provided.


Learning Assessments $\rightarrow$ E2.6b
... find $\mathrm{I}_{\mathrm{x}}$ in the circuit provided.


## Kirchhoff's Voltage Law

... the algebraic sum of the voltages around any loop is zero

$$
\begin{aligned}
& \quad \sum_{h=1}^{K} v_{h}(t)=0 \quad \text { KVL: } 30-V_{R 1}+5-V_{R 2}+15-V_{R 3}=0 \\
& \text { *Adopt a sign convention for the voltages } \\
& \text { across the elements: } \\
& \text { - Increase in energy level } \rightarrow \text { positive }
\end{aligned}
$$

- Decrease in energy level $\rightarrow$ negative


## Example 2.12

... write the KVL equation for:

1) abda
2) dbcd
3) dabcd


Learning Assessment $\rightarrow$ E2.9
... find $V_{b d}$.


