# Last Lecture → Impedance

The ratio of the phasor voltage V to the phasor current I.

$$Z = \frac{V}{I} [Ohms]$$

$$= \frac{V_M \langle \theta_v}{I_M \langle \theta_i} = \frac{V_M}{I_M} \langle (\theta_v - \theta_i) = Z \langle \theta_z \rangle$$

Reactance

Resistance

$$Z\langle\theta_z=R+jX$$

#### **KVL & KCL** are valid in the frequency domain!

PASSIVE ELEMENT	IMPEDANCE
R	$\mathbf{Z} = R$
L	$\mathbf{Z} = j\omega L = jX_L, X_L = \omega L$
C	$\mathbf{Z} = \frac{1}{j\omega C} = -\frac{j}{\omega C} = -jX_C, X_C = \frac{1}{\omega C}$

**Series** → **Equivalent Impedance** 

$$Z_s = Z_1 + Z_2 + \dots + Z_n$$

**Parallel** → **Equivalent Impedance** 

$$\frac{1}{Z_p} = \frac{1}{Z_1} + \frac{1}{Z_2} + \dots + \frac{1}{Z_n}$$

### Last Lecture → Admitance

The ratio of the phasor current I to the phasor voltage V.

$$Y = \frac{I}{V} = \frac{1}{Z}$$
 [Siemens]

#### **Conductance**

$$Y \left< \theta_y = G + jB \right>$$
Susceptance

### **KVL & KCL** are valid in the frequency domain!

PASSIVE ELEMENT	IMPEDANCE
R	$\mathbf{Z} = R$
L	$\mathbf{Z} = j\omega L = jX_L, X_L = \omega L$
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### **Parallel** → **Equivalent Admittance**

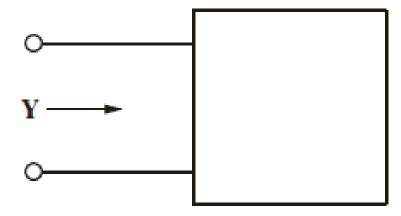
$$Y_p = Y_1 + Y_2 + \dots + Y_n$$

**Series** → **Equivalent Admittance** 

$$\frac{1}{Y_s} = \frac{1}{Y_1} + \frac{1}{Y_2} + \dots + \frac{1}{Y_n}$$

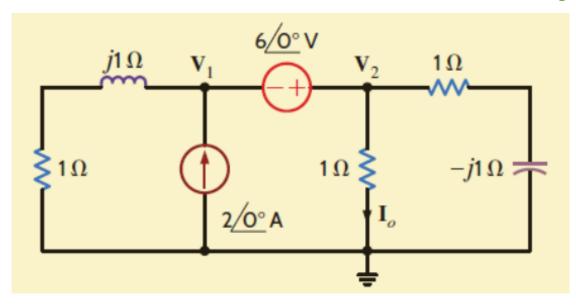
### Problem 8.25

The admittance of the box in the figure provided is 0.1 + j0.2 S at 500 rad/s. What is the impedance at 300 rad/s?



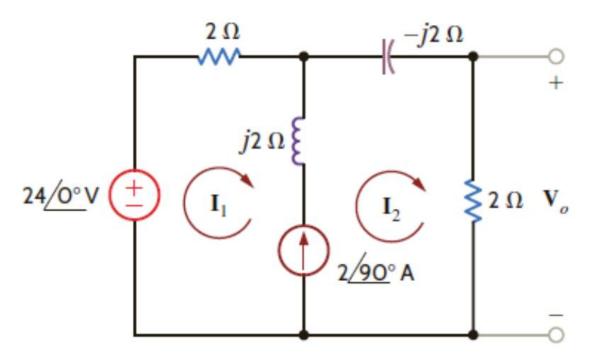
# Example 8.15

For the given network determine I<sub>0</sub> using nodal analysis.



## Learning Assessment E8.20

For the given network use (a) mesh equations and (b) Thevenin's theorem to find  $V_0$ .



## Learning Assessment E8.23

For the given network use (a) superposition and (b) source transformation to find  $V_0$ .

