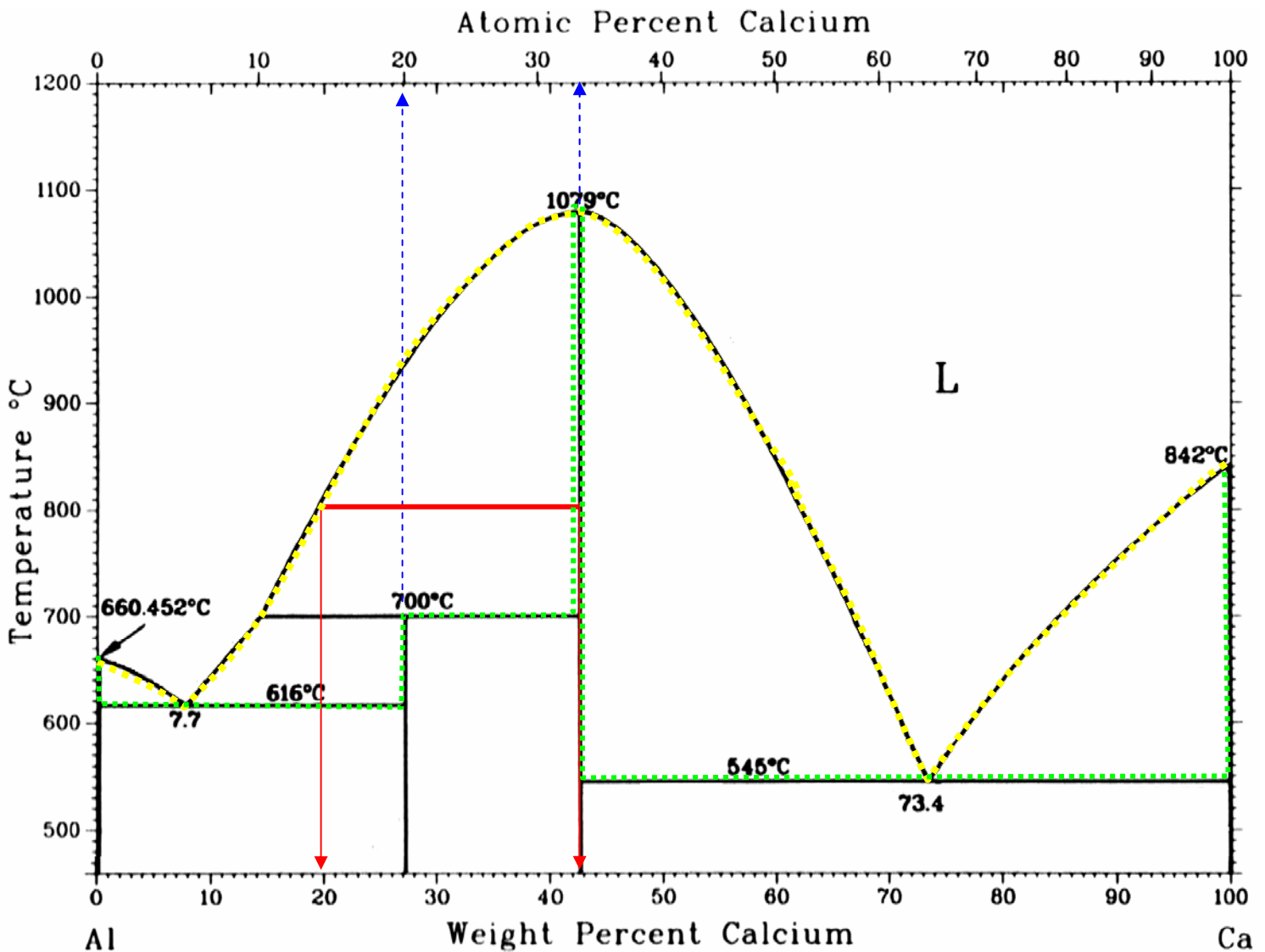


Name \_\_\_\_\_

Student Number: \_\_\_\_\_

Aluminum-calcium alloys are being used in the production of metallic foams for heat dissipation and shock absorbing mechanisms. For the following Al-Ca equilibrium phase diagram respond to the following requests:

- Indicate the liquidus, solidus and -if any- solvus lines
- Identify (indicate which type) and label ALL invariant (isothermal) transformations in the diagram
- Identify all intermediate phases present and provide their chemical formula.
- For the alloy containing 27.3 wt.% Ca – 72.7 wt.% Al (exactly on that vertical line) calculate the relative amounts of phases present and their chemical compositions at 800°C and at 616°C.



- Indicated in the graph: liquidus - - - - - solidus . . . . . There is no visible solvus line.
- Three horizontal lines in the graph are isothermal transformations.  
Peritectic at 700°C  $\text{Al}_2\text{Ca} + \text{Liq.} \leftrightarrow \text{Al}_4\text{Ca}$

Continue your work on the back of the paper

Eutectic at 616°C    Liq.  $\leftrightarrow$  Al<sub>4</sub>Ca +Al  
Eutectic at 545°C    Liq.  $\leftrightarrow$  Al<sub>2</sub>Ca +Ca

c) There are two intermediate phases (line compounds) at 27.3wt.% Ca (20 at.% Ca) and at 42.7 wt.% Ca (33.33 at.% Ca). Their corresponding chemical formulae are: Al<sub>4</sub>Ca (20 at.% Ca, 1/5 moles are Ca) and Al<sub>2</sub>Ca (1/3 moles are Ca).

d) For the alloy containing 27.3 wt.% Ca – 72.7 wt.% Al  
at 800°C:

Chemical composition:    Liq.: 19.5 wt.% Ca, 81.1 wt.% Al  
                                  Al<sub>2</sub>Ca: 42.7 wt.% Ca, 57.3 wt.% Al

Relative amount of phases:    Liq.% =  $\frac{42.7-27.3}{42.7-19.5} \cdot 100 = 66.4\%$   
  Al<sub>2</sub>Ca:% =  $\frac{27.3-19.5}{42.7-19.5} \cdot 100 = 33.6\%$

at 616°C.

Chemical composition:    Al<sub>4</sub>Ca.: 27.3 wt.% Ca – 72.7 wt.% Al

Relative amount of phases:    Al<sub>4</sub>Ca:% = 100 % (everything is Al<sub>4</sub>Ca on that vertical line)

INGE 4001 – Sections 066

Instructor: O. M. Suárez – Graduate Assistants: Hermes Calderón

Phase Diagram Last Quiz – Tuesday May 2, S-303

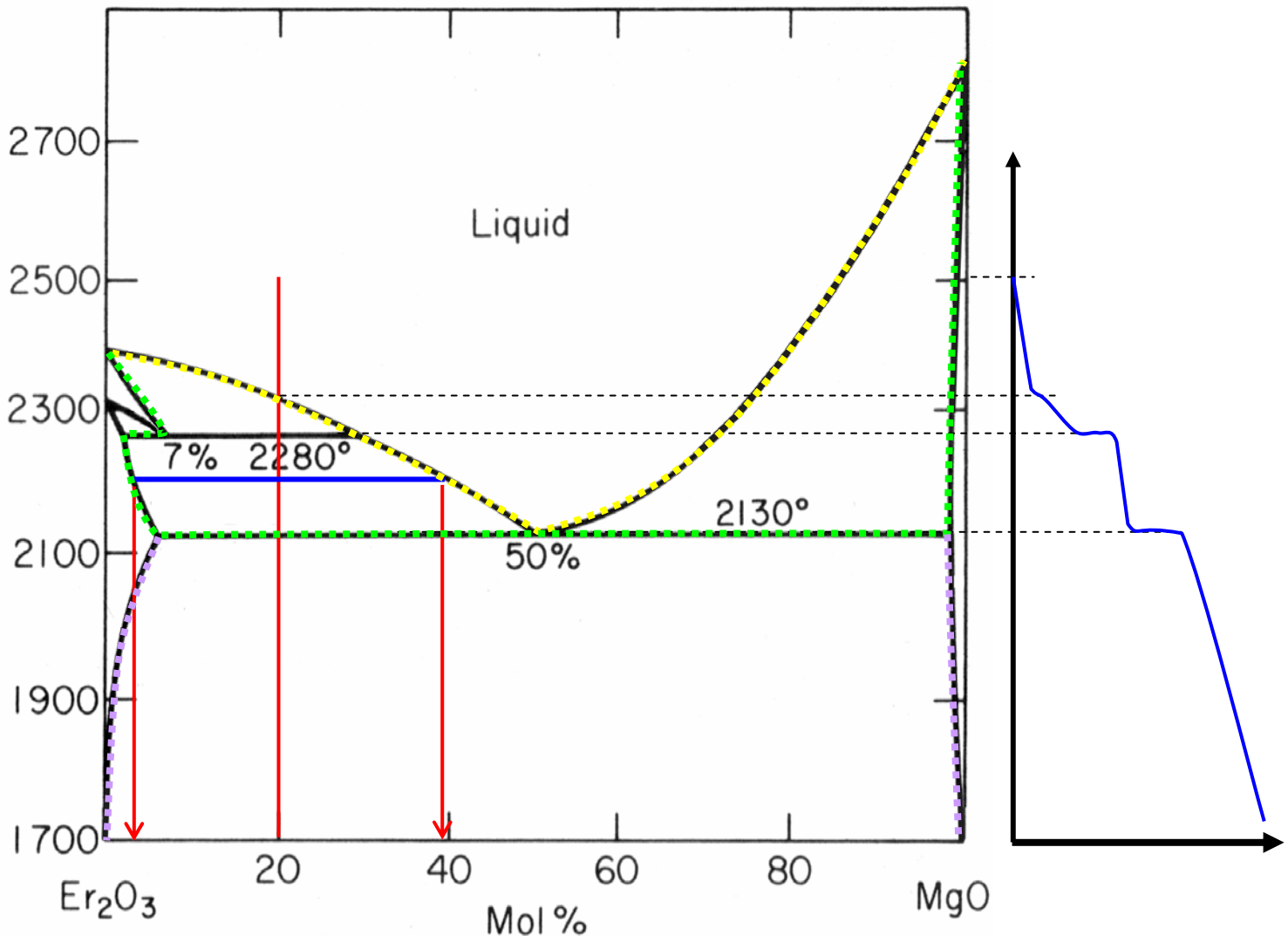
Maximum grade: 15 points - Maximum time: ½ hour

Name \_\_\_\_\_

Student Number: \_\_\_\_\_

Magnesia-doped erbia is being used in multilayered capacitors for their high dielectric constant. For the following  $\text{Er}_2\text{O}_3$ -MgO equilibrium phase diagram respond to the following requests:

- Indicate the liquidus, solidus and -if any- solvus lines
- Is erbia or magnesia polymorphic? Justify your answer.
- Identify (indicate which type) and label ALL invariant (isothermal) transformations in the diagram
- For the ceramic containing 20 mol.% MgO –80 mol.%  $\text{Er}_2\text{O}_3$  calculate the relative amounts of phases present and their chemical compositions at 2200°C. Then sketch the cooling curve for this composition starting at 2500°C (you should do this at the proper temperature scale)



- Indicated in the graph: liquidus - - - - - solidus - - - - - solvus - - - - -
- Erbia is polymorphic: at 2310°C it goes from one crystal structure  $\alpha$  to another one  $\beta$  (upon cooling).
- Two horizontal lines in the graph are isothermal transformations.  
Metatectic at 2280°C  $\alpha \leftrightarrow \beta + \text{Liq}$ .

Continue your work on the back of the paper

Eutectic at 2130°C Liq.  $\leftrightarrow$   $\beta + \gamma$

d) There are two intermediate phases (line compounds) at 27.3wt.% Ca (20 at.% Ca) and at 42.7 wt.% Ca (33.33 at.% Ca). Their corresponding chemical formulae are:  $\text{Al}_4\text{Ca}$  (20 at.% Ca, 1/5 moles are Ca) and  $\text{Al}_2\text{Ca}$  (1/3 moles are Ca).

d) For the ceramic containing 20 mol.% MgO –80 mol.%  $\text{Er}_2\text{O}_3$   
at 2200°C:

Chemical composition:   Liq.: 3 mol.% MgO, 97 mol.%  $\text{Er}_2\text{O}_3$   
                                   $\beta$ : 39 mol.% MgO, 61 mol.%  $\text{Er}_2\text{O}_3$

Relative amount of phases:   Liq.% =  $\frac{20-3}{39-3} \cdot 100 = 47.2\%$   
   $\beta$  % =  $\frac{39-20}{39-3} \cdot 100 = 52.8\%$

The cooling curve is indicated by the phase diagram. For each crossing of an isothermal transformation there is a flat segment (isothermal).

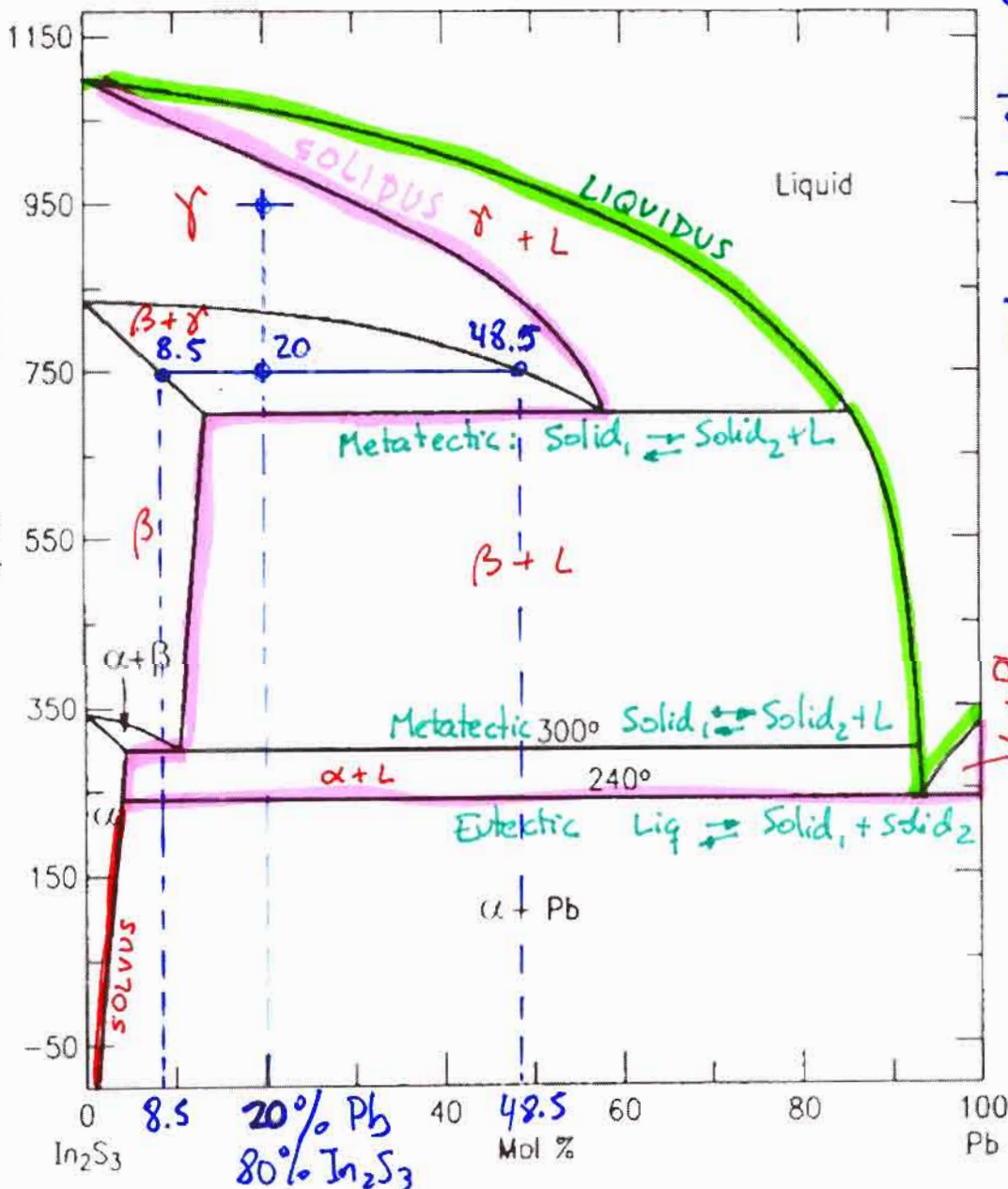
Name:

Student Number:

Solid-state batteries constructed from indium sulfides ( $\text{In}_2\text{S}_3$ ) can be doped with lead for the production of more efficient batteries. For the following  $\text{In}_2\text{S}_3$ -Pb equilibrium phase diagram answer the following questions:

- Are  $\text{In}_2\text{S}_3$  and/or Pb polymorphic?  *$\text{In}_2\text{S}_3$  is polymorphic but not lead.*
- Indicate the liquidus, solidus and -if any- solvus lines
- Identify (indicate which type) and label ALL invariant transformations in the diagram *Metatectics, eutectic*
- Identify all intermediate phases (or compounds) present. *There is no intermediate phase*
- Label ALL regions in the phase diagram with the corresponding phases present (some tips were provided)
- For the composition 20 mol% Pb – 80 mol%  $\text{In}_2\text{S}_3$  calculate the relative amounts of phases present and their chemical compositions at the following temperatures: 750°C and 950°C.

**f) @750°C**  
 Chem. Comp.  $\gamma$  { 48.5% Pb }  
 { 51.5%  $\text{In}_2\text{S}_3$  }  
 $\beta$  { 8.5% Pb }  
 { 91.5%  $\text{In}_2\text{S}_3$  }  
 Rel. amount.  $\% \gamma = \frac{20 - 8.5}{48.5 - 8.5} \cdot 100 = 19.8\%$   
 $\% \beta = \frac{48.5 - 20}{48.5 - 8.5} \cdot 100 = 80.2\%$



**f) @950°C**  
 Chem. Comp.  $\gamma$  { 20% Pb }  
 { 80%  $\text{In}_2\text{S}_3$  }  
 Rel. amount  $\gamma$  100%  
*There's only one phase:  $\gamma$*



Name:

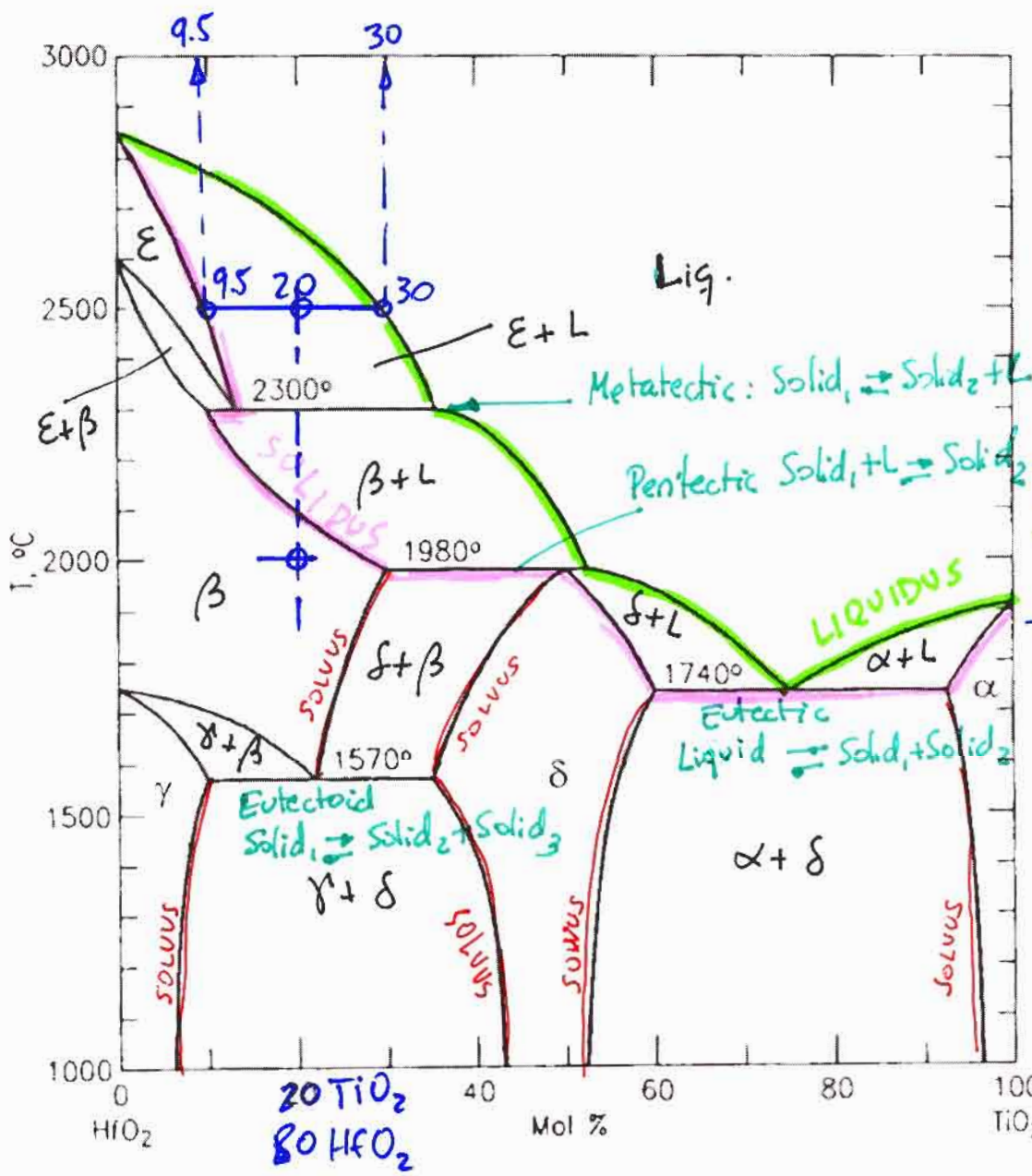
Student Number:

Compounds of hafnia ( $\text{HfO}_2$ ) and rutile or titania ( $\text{TiO}_2$ ) are being used in capacitors for their high  $\kappa$  (dielectric constant). For the following  $\text{HfO}_2 - \text{TiO}_2$  equilibrium phase diagram respond to the following requests:

- g) Are  $\text{HfO}_2$  and/or  $\text{TiO}_2$  polymorphic? *Only hafnia is polymorphic*
- h) Indicate the liquidus, solidus and -if any- solvus lines
- i) Identify (indicate which type) and label ALL invariant transformations in the diagram
- j) Identify all intermediate phases (or compounds) present. *Only one:  $\delta$*
- k) Label ALL regions in the phase diagram with the corresponding phases present (some tips were provided)
- l) For the composition with 20 mol %  $\text{TiO}_2 - 80$  mol%  $\text{HfO}_2$  calculate the relative amounts of phases present and their chemical compositions at the following temperatures: 2000°C and 2500°C.

Metatectric  
Eutectoid  
Peritectic  
Eutectic

f) @ 2000°C there's only one phase  $\beta$  therefore:  
Rel. amount: 100%  $\beta$  with chem. comp.  $\left\{ \begin{array}{l} 20\% \text{TiO}_2 \\ 80\% \text{HfO}_2 \end{array} \right.$



f) @ 2500°C 100 phases present:  $\epsilon + L$   
Chem. Comp:  $\epsilon \left\{ \begin{array}{l} 9.5\% \text{TiO}_2 \\ 81.5\% \text{HfO}_2 \end{array} \right.$   
 $L \left\{ \begin{array}{l} 30\% \text{TiO}_2 \\ 70\% \text{HfO}_2 \end{array} \right.$   
Rel. amount %  $\epsilon = \frac{30-20}{30-9.5} \cdot 100 = 48.7\%$   
 $\% L = \frac{20-9.5}{30-9.5} \cdot 100 = 51.3\%$



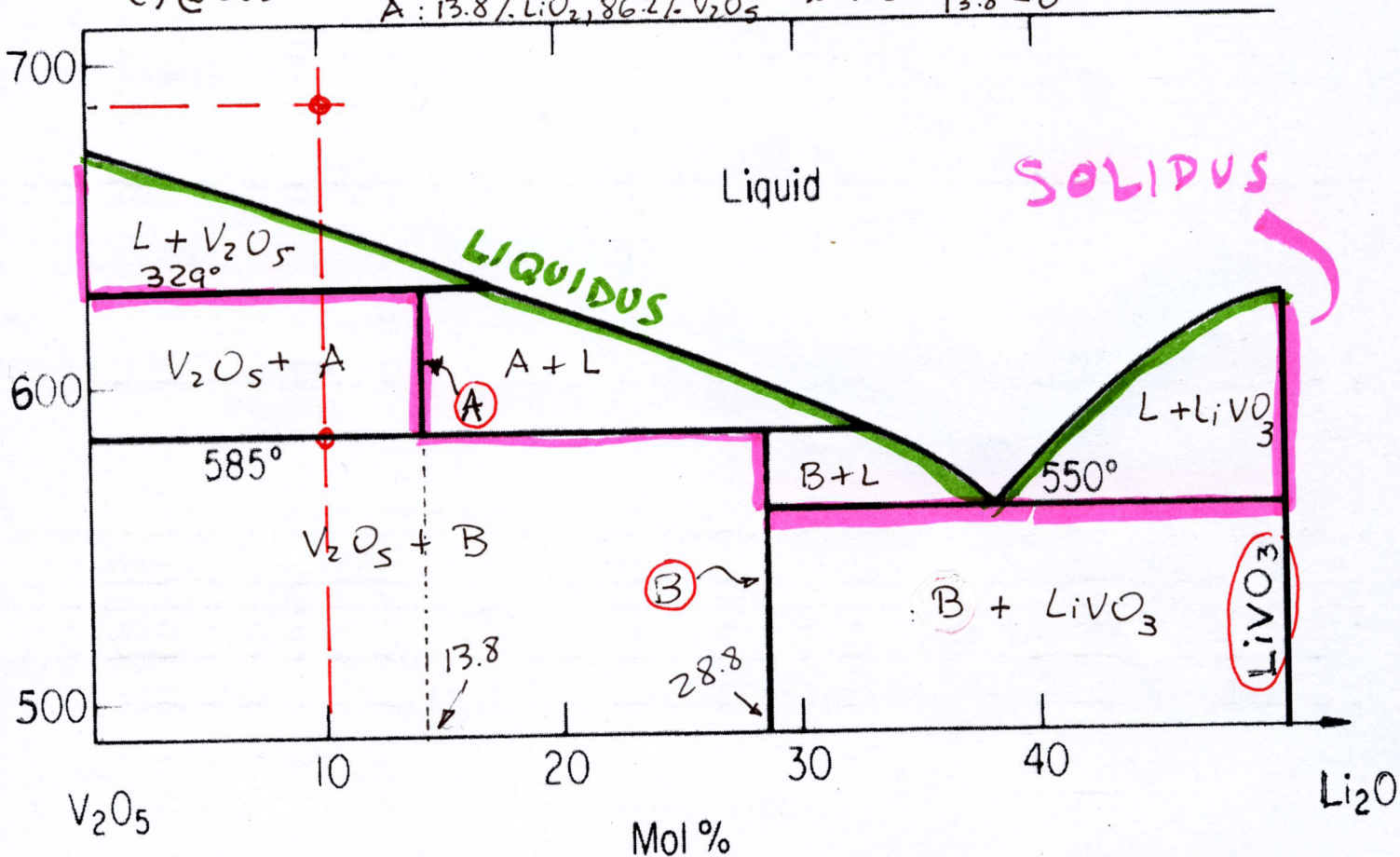
Name:

Vanadia ( $V_2O_5$ ) and lithia ( $Li_2O$ ) are used in the production of advanced glasses. The following is a **partial**  $V_2O_5$ - $Li_2O$  equilibrium phase diagram (limited to 50 mol%  $Li_2O$  where the  $LiVO_3$  line compound is located).

Please respond to the following requests:

- Indicate the liquidus, solidus and -if any- solvus lines
- Identify (indicate which type) and label ALL invariant transformations in the diagram
- Identify all intermediate phases (or compounds) present.
- Label ALL regions in the phase diagram with the corresponding phases present.
- For the composition 10 mol%  $Li_2O$  - 90 mol%  $V_2O_5$  calculate the relative amounts of phases present and their chemical compositions at the following temperatures: 690°C and 585°C.

e) @ 585°C:  $V_2O_5: 100\% V_2O_5$      $A: 13.8\% Li_2O, 86.2\% V_2O_5$      $\%V_2O_5 = \frac{13.8 - 10}{13.8 - 0} \cdot 100 = 27.5\%$      $\%Li_2O = 72.5\%$



a) Liquidus ——— Solidus ——— There are no solvus lines

b) There are 3 isothermal transformations:

@ 329°C:  $L + V_2O_5 \rightleftharpoons A$  peritectic

@ 585°C:  $A \rightleftharpoons V_2O_5 + B$  eutectoid

@ 550°C:  $L \rightleftharpoons B + LiVO_3$  eutectic

c) There are 3 intermediate phases:

$A$ ,  $B$  and  $LiVO_3$

e) @ 690°C: 100% Lig  
Lig: 10%  $Li_2O$ , 90%  $V_2O_5$

@ 585°C - Δ  
 $V_2O_5: 100\% V_2O_5$      $\%V_2O_5 = \frac{28.8 - 10}{28.8 - 0} \cdot 100 = 65.3\%$   
 $B \left\{ \begin{array}{l} 28.8\% Li_2O \\ 71.2\% V_2O_5 \end{array} \right.$      $\%Li_2O = 34.7\%$



INGE 4001-Section 036

Instructor: O. Marcelo Suárez

Grad Student Assist.: Hermes Calderón

Phase Diagrams - Quiz #3 - 12 Points -Maximum time: 20 minutes

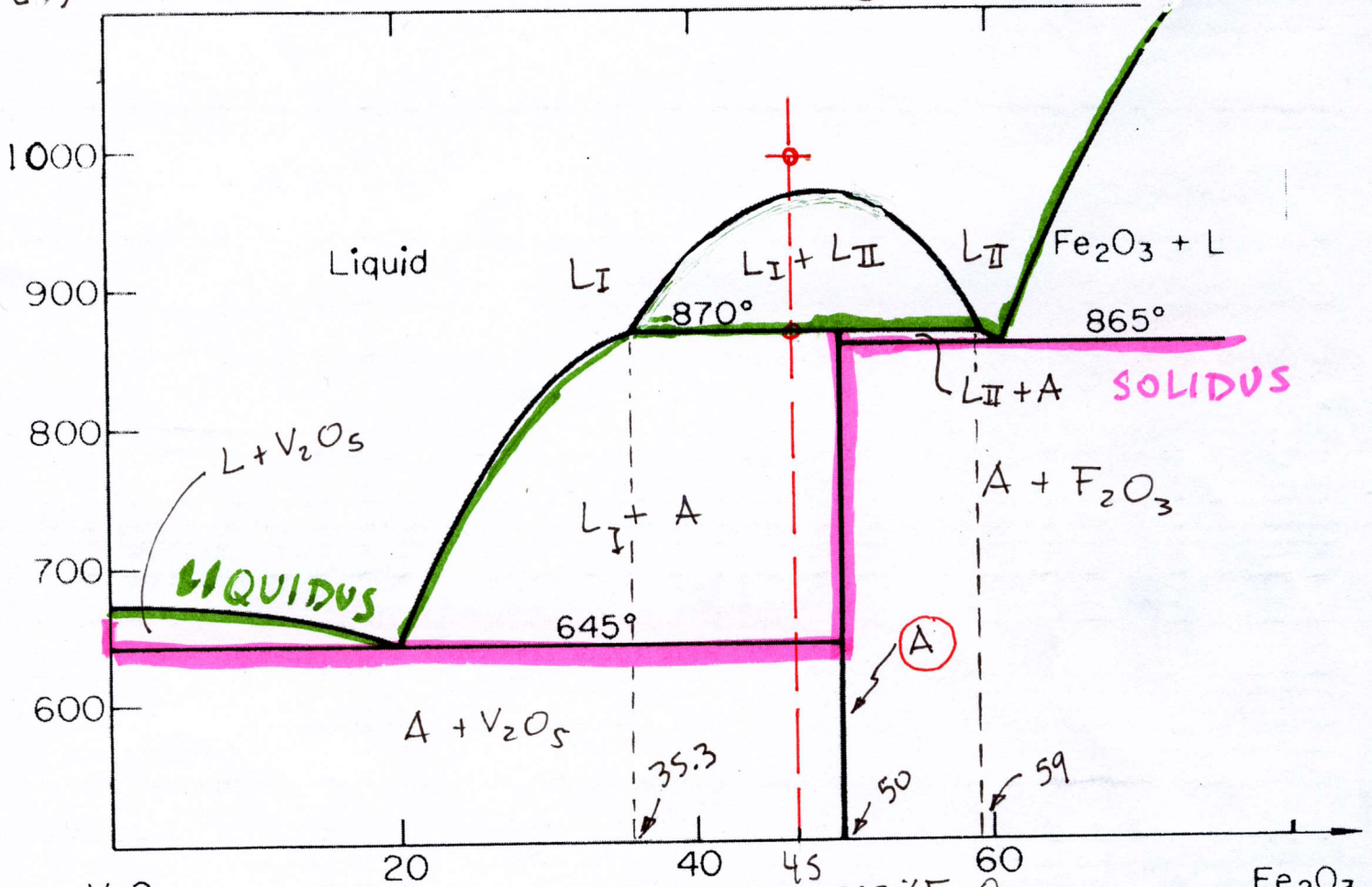
Name:

Student Number:

Vanadia ( $V_2O_5$ ) and hematite ( $\alpha Fe_2O_3$ ) are being used in ceramic glazes. The following is a **partial**  $V_2O_5 - Fe_2O_3$  equilibrium phase diagram **limited to ~ 80 mol%  $Fe_2O_3$** . Please respond to the following requests:

- Is there any intermediate compound? If there is one, does it melt congruently or not?
- Indicate the liquidus, solidus and -if any- solvus lines
- Identify (indicate which type) and label ALL invariant transformations in the diagram
- Label ALL regions in the phase diagram with the corresponding phases present (some tips were provided)
- For the composition with 45 mol %  $Fe_2O_3 - 55$  mol%  $V_2O_5$  calculate the relative amounts of phases present and their chemical compositions at the following temperatures: 870°C and 1000°C.

a) Yes **(A)** melts congruently.  $@ 865^\circ L_{II} \rightleftharpoons A + Fe_2O_3$  eutectic  
 c) There are 3:  $@ 870^\circ L_I + L_{II} \rightleftharpoons$  Syntectic  $@ 645^\circ L \rightleftharpoons A + V_2O_5$  eutectic



e) @ 1000°C 100% Liq  
 L { 45%  $Fe_2O_3$   
 { 55%  $V_2O_5$

@ 870°C +Δ:  $L_I$  { 35.3%  $Fe_2O_3$   
 { 64.7%  $V_2O_5$   
 $L_{II}$  { 59%  $Fe_2O_3$   
 { 41%  $V_2O_5$

@ 870°C -Δ:  $L_I$  { 35.3%  $Fe_2O_3$   
 { 64.7%  $V_2O_5$   
 A { 50%  $Fe_2O_3$   
 { 50%  $V_2O_5$

$\% L_I = \frac{59 - 45}{59 - 35.3} \times 100 = 59\%$   
 $\% L_{II} = 41\%$   
 $\% L_I = \frac{50 - 45}{50 - 35.3} \times 100 = 34\%$   
 $\% A = 66\%$