



Chapter 2: Machines, Machine Languages, and Digital Logic

Instruction sets, SRC, RTN, and the mapping of register transfers to digital logic circuits

Some modifications by Tom Noack, 2010

Chapter 2 Topics

- 2.1 Classification of Computers and Instructions
- 2.2 Kinds and Classes of Instruction Sets
- 2.3 Informal Description of the Simple RISC Computer, SRC
 - Students may wish to consult Appendix C, Assembly and Assemblers for information about assemblers and assembly.
- 2.4 Formal Description of SRC using Register Transfer Notation (RTN)
- 2.5 RTN Description of Addressing Modes
- 2.6 Register Transfers and Logic Circuits: from Behavior to Hardware
 - Students may wish to consult Appendix A, Digital Logic for additional information about Digital Logic circuits.

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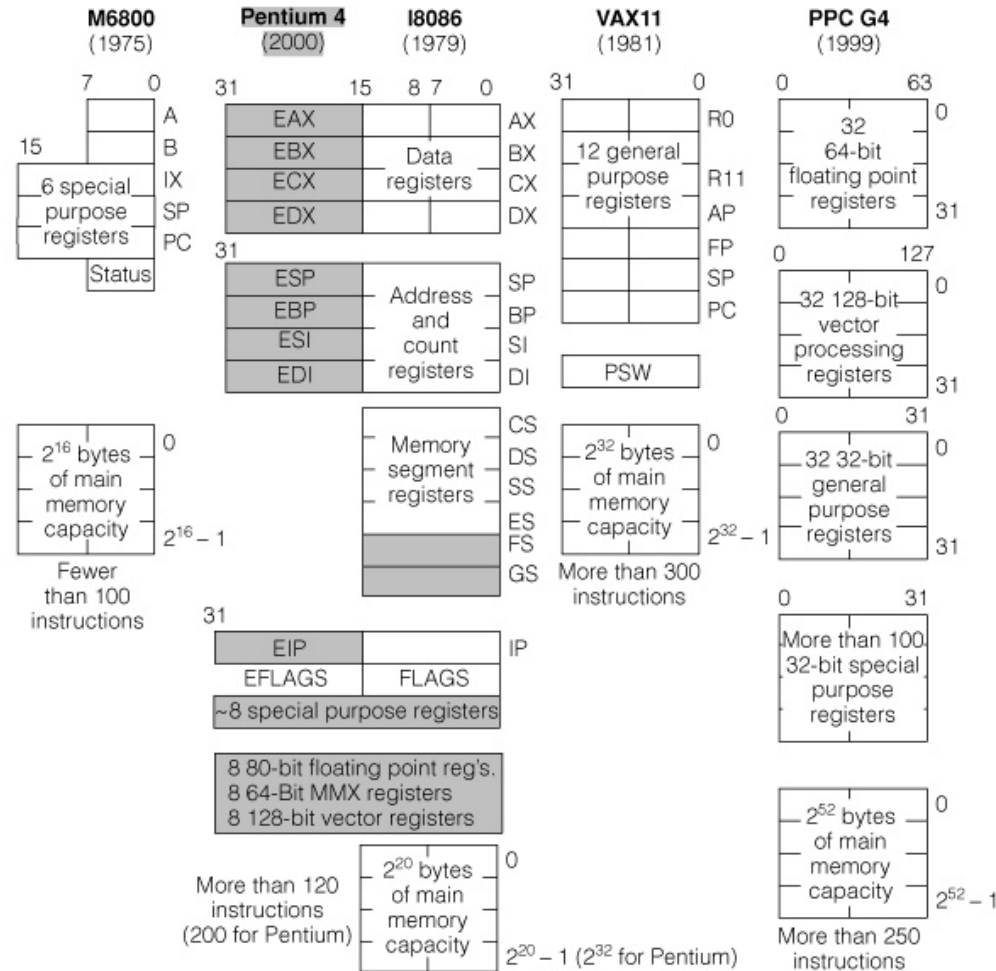
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What are the components of an ISA?

- Sometimes known as *The Programmers Model* of the machine
- Storage cells
 - General and special purpose registers in the CPU
 - Many general purpose cells of same size in memory
 - Storage associated with I/O devices
- The Machine Instruction Set
 - The instruction set is the entire repertoire of machine operations
 - Makes use of storage cells, formats, and results of the fetch/execute cycle
 - i. e. Register Transfers
- The Instruction Format
 - Size and meaning of fields within the instruction
- The nature of the Fetch/Execute cycle
 - Things that are done before the operation code is known

Fig. 2.1 Programmer's Models of Various Machines

We saw in Chap. 1 a variation in number and type of storage cells




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What Must an Instruction Specify?

Data Flow

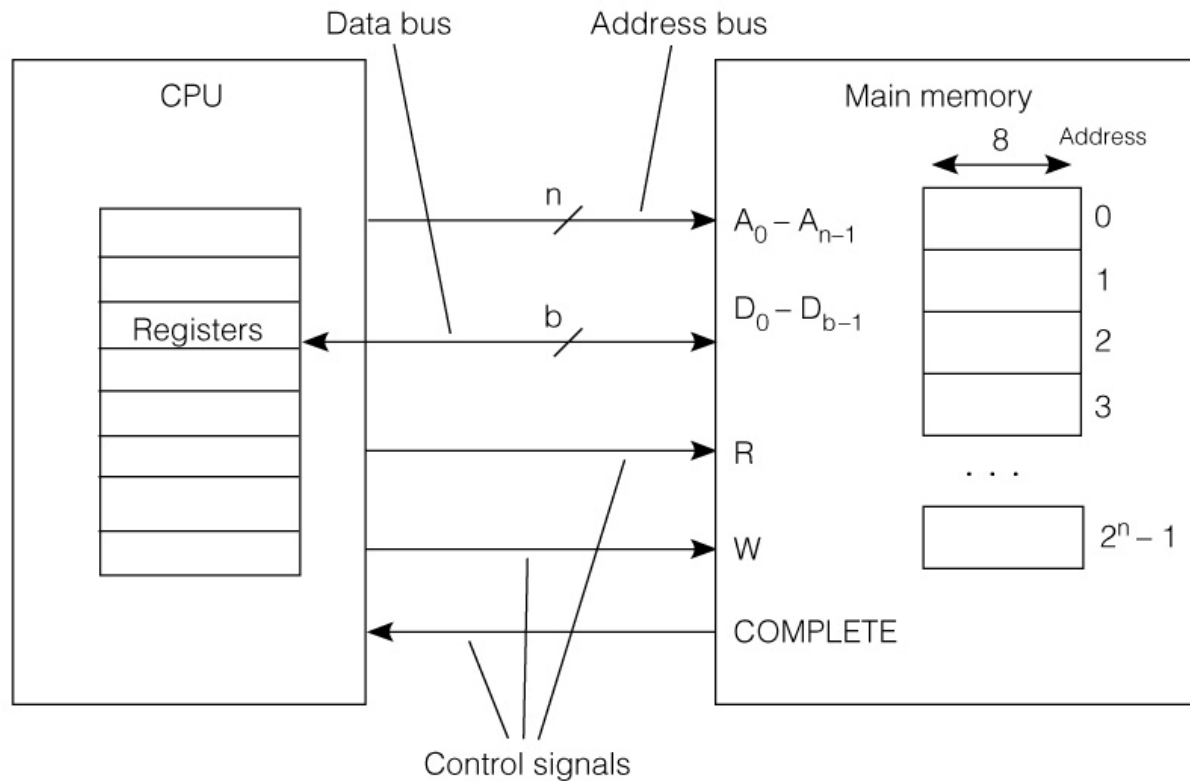


- Which operation to perform: add r0, r1, r3
- Ans: Op code: add, load, branch, etc.
- Where to find the operand or operands add r0, r1, r3
 - In CPU registers, memory cells, I/O locations, or part of instruction
- Place to store result add r0, r1, r3
 - Again CPU register or memory cell
- Location of next instruction add r0, r1, r3 br endloop

- The default is usually memory cell pointed to by program counter—PC: the next instruction in sequence
- Sometimes there *is* no operand, or no result, or no next instruction. Can you think of examples?

The Bus idea

- A bus is a system for transferring data
 - Components
 - Data – what is being transferred
 - Address – where from/to
 - Control – describes and synchronizes the transfer, R/W, etc.
 - Mechanization
 - Parallel traces on a parentboard or inside a chip
 - Serial – USB, Ethernet, SCSI
 - Interfacing circuits to a bus on a chip
 - Gate – places data on a bus – usually tri-state
 - Strobe – captures data from the bus
 - Transfer is
 - gate (one source at a time, signal is Y_{out})
 - Strobe (can be several destinations, signal is Y_{in})
 - One transfer per bus per clock cycle

Fig. 2.2 Accessing Memory—Reading from Memory



Typical bus transaction
Note data, address, control

For a Memory Read:

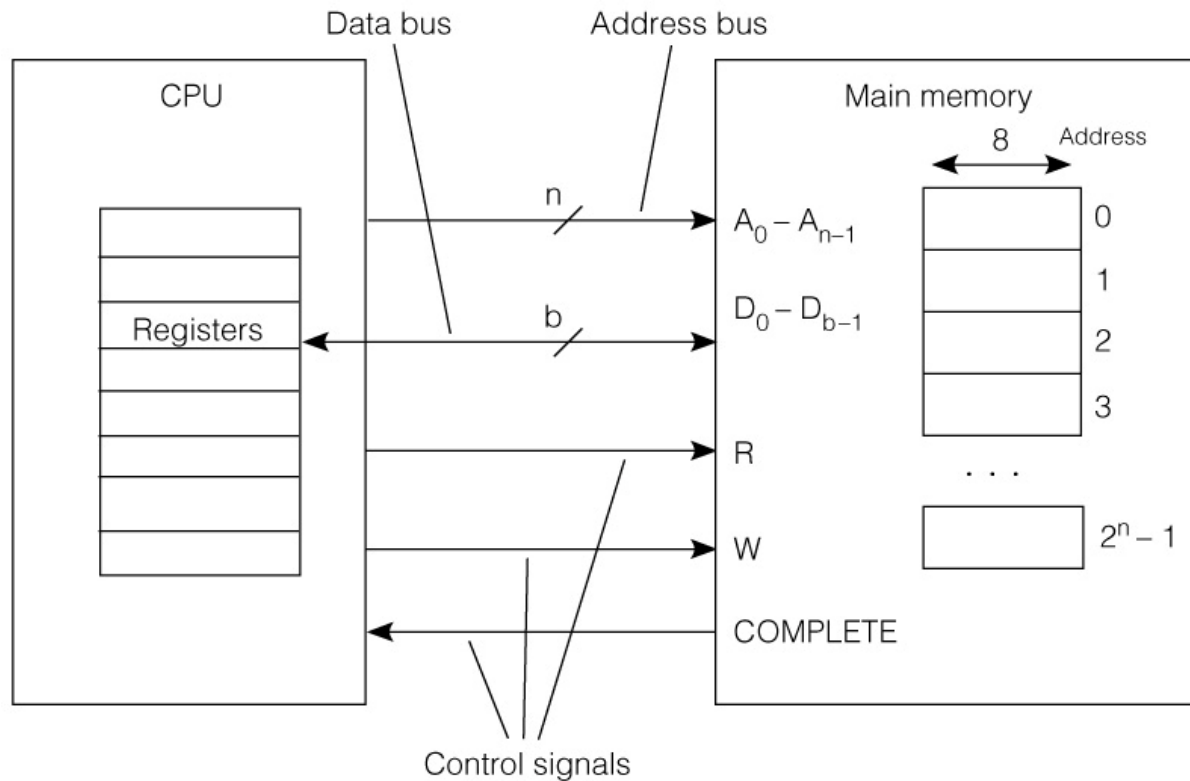
CPU applies desired address to Address lines $A_0 - A_{n-1}$

CPU issues Read command, R

Memory returns the value at that address on Data lines $D_0 - D_{b-1}$ and asserts the COMPLETE signal

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Figure 2.2 Accessing Memory—Writing to Memory



For a Memory Write:

CPU applies desired address to Address lines $A_0 - A_{n-1}$ and data to be written on

Data lines $D_0 - D_{b-1}$

CPU issues Write command, W

Memory asserts the COMPLETE signal when the data has been written to memory.

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Instructions Can Be Divided into 3 Classes

Data movement instructions

- Move data from a memory location or register to another memory location or register without changing its form
- **Load**—source is memory and destination is register
- **Store**—source is register and destination is memory


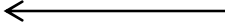
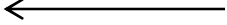
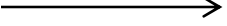

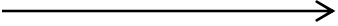
Arithmetic and logic (ALU) instructions

- Changes the form of one or more operands to produce a result stored in another location
- **Add, Sub, Shift**, etc.

Branch instructions (control flow instructions)

- Any instruction that alters the normal flow of control from executing the next instruction in sequence
- **Br Loc, Brz Loc2**,—unconditional or conditional branches

Tbl. 2.1 Examples of Data Movement Instructions

Inst ruct.	Meaning	Machine
 MOV A, B	Move 16 bits from mem. loc. A to loc. B	VAX11
 lwz R3, A	Move 32 bits from mem. loc. A to reg. R3	PPC601
 li \$3, 455	Load the 32 bit integer 455 into reg. 3	MIPS R3000
 mov R4, dout	Move 16 bits from R4 to out port dout	DEC PDP11
 IN, AL, KBD	Load a byte from in port KBD to accum.	Intel Pentium
 LEA.L (A0), A2	Load address pointed to by A0 into A2	M68000

- Lots of variation, even with one instruction type
- Notice differences in direction of data flow left-to-right or right-to-left

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Assembler and machine differences

- Assembler differences
 - One processor may be supported by several different assemblers
 - Destination-first
 - INTEL/Microsoft
 - Source-first
 - GNU, Motorola, VAX
 - Processor-independent
 - GNU – free software foundation – used in most Linux distributions
 - Register names and opcodes can't be reserved words, so prefixes are used to indicate registers and immediates
 - Table-driven – one assembler skeleton
 - Processor-dependent
 - Specialized, such as INTEL, Microsoft, Motorola
 - Register names and opcodes are reserved words

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Tbl 2.2 Examples of ALU (Arithmetic and Logic Unit) Instructions

Instruction	Meaning	Machine
MULF A, B, C	multiply the 32-bit floating point values at mem loc'ns. A and B, store at C	VAX11
nabs r3, r1	Store abs value of r1 in r3	PPC601
ori \$2, \$1, 255	Store logical OR of reg \$ 1 with 255 into reg \$2	MIPS R3000
DEC R2	Decrement the 16-bit value stored in reg R2	DEC PDP11
SHL AX, 4	Shift the 16-bit value in reg AX left by 4 bits	Intel 8086

- Notice again the complete dissimilarity of both syntax and semantics

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ALU instruction and assembler conventions

- Instruction varieties
 - Zero- to four-address code
 - Combined memory and computation
 - Either-or (RISC/CISC) load-store or operate in registers
 - Operand sizes (byte/half/word/double)
 - Can be specified by opcode (add.w, sub.h)
 - Or by operand attribute (register size or defined name)
 - Or by keyword (word/byte ptr)
- Assembler varieties
 - Processor-independent
 - Processor-dependent

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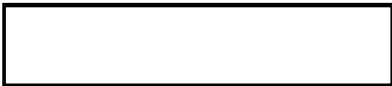
Tbl 2.3 Examples of Branch Instructions

Instruction	Meaning	Machine
BLSS A, Tgt	Branch to address Tgt if the least significant bit of mem loc'n. A is set (i.e. = 1)	VAX11
bun r2	Branch to location in R2 if result of previous floating point computation was Not a Number (NAN)	PPC601
beq \$2, \$1, 32	Branch to location (PC + 4 + 32) if contents of \$1 and \$2 are equal	MIPS R3000
SOB R4, Loop	Decrement R4 and branch to Loop if R4 \neq 0	DEC PDP11
JCXZ Addr	Jump to Addr if contents of register CX = 0.	Intel 8086

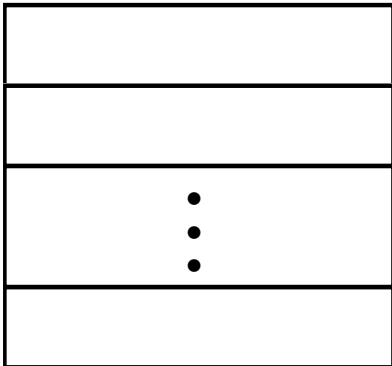
CPU Registers Associated with Flow of Control—Branch Insts.

- Program counter usually contains the address of, or "points to" the next instruction
- Condition codes may control branch
- Branch targets may be contained in separate registers

Processor State



Program Counter



Branch Targets



Condition Codes

HLL Conditionals Implemented by Control Flow Change

- Conditions are computed by arithmetic instructions
- Program counter is changed to execute only instructions associated with true conditions

C language

```
if NUM==5 then SET=7
```

Assembly language

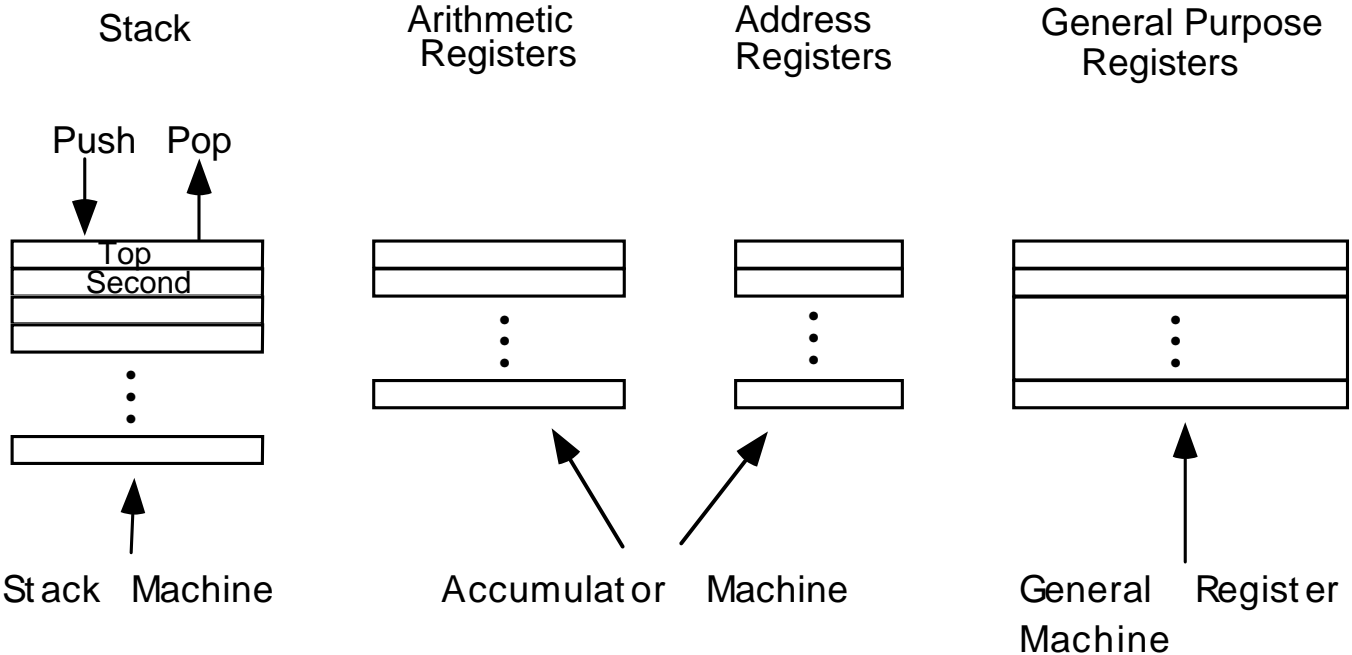
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CMP.W #5, NUM ;the comparison
BNE L1 ;conditional branch
MOV.W #7, SET ;action if true
L1 ... ;action if false

```


CPU Registers may have a “personality”

- Architecture classes are often based on how where the operands and result are located and how they are specified by the instruction.
- They can be in CPU registers or main memory



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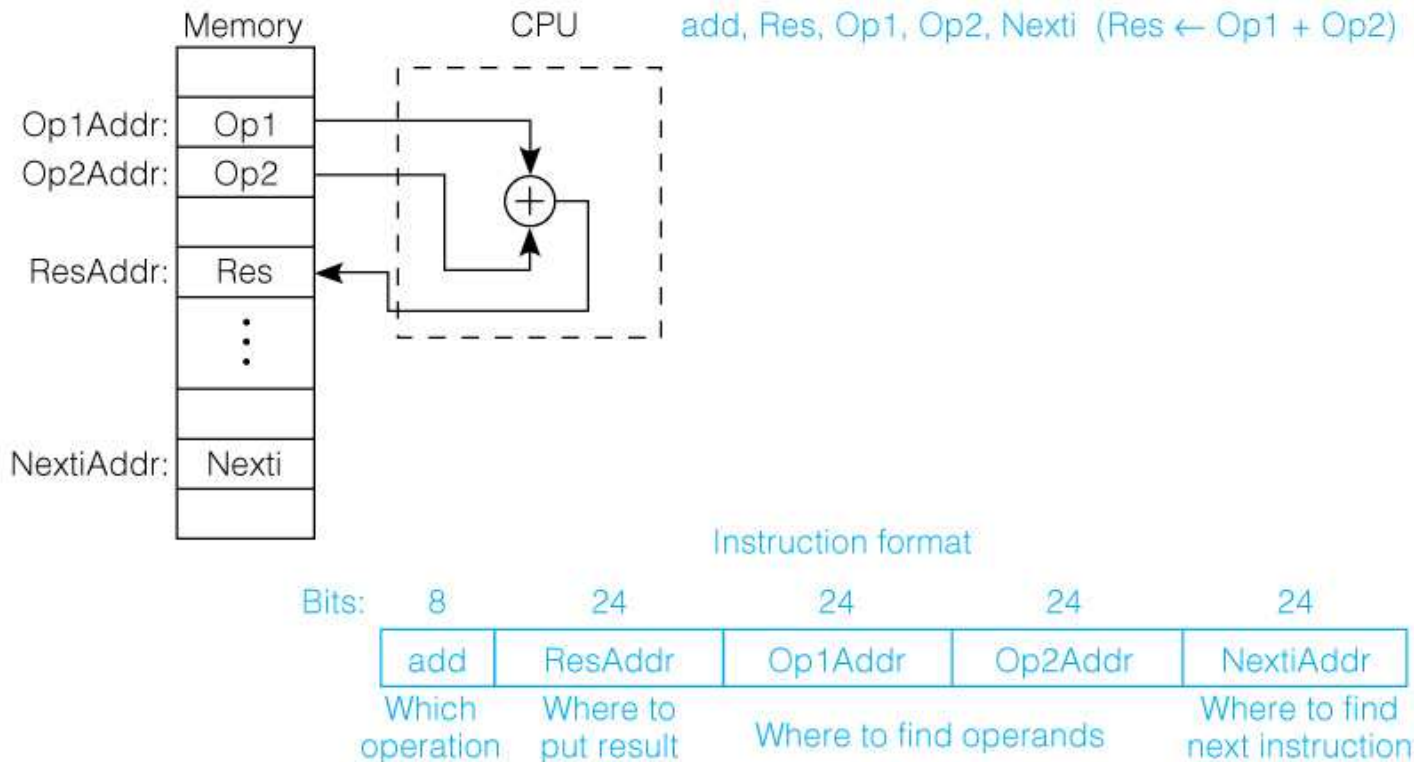
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3, 2, 1, & 0 Address Instructions

The classification is based on arithmetic instructions that have two operands and one result

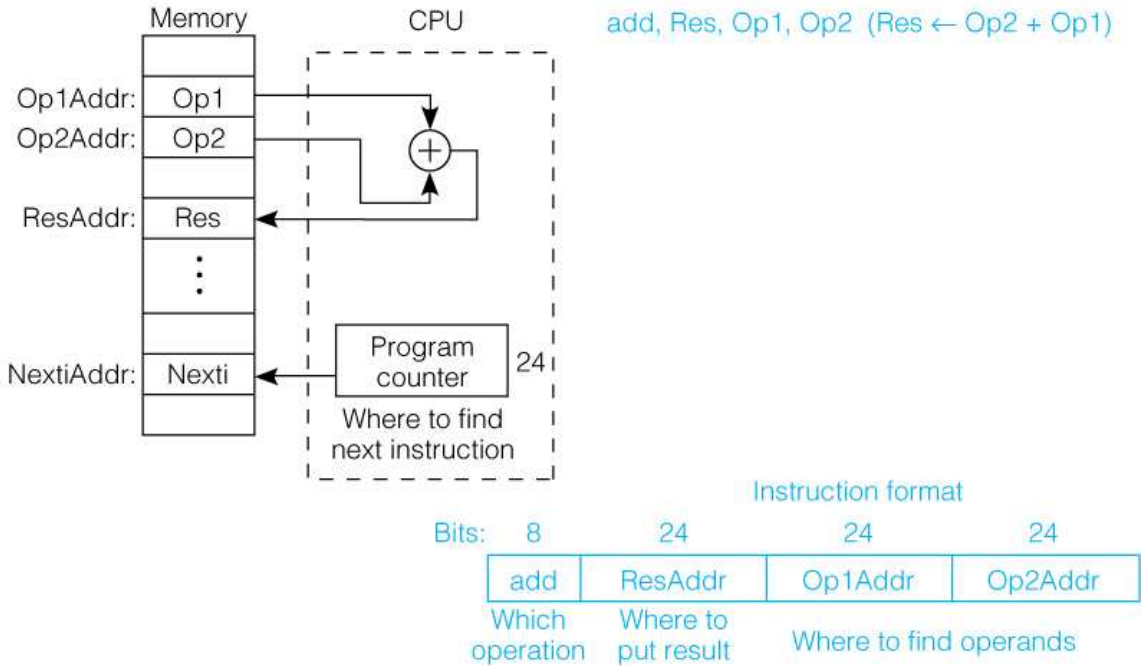
- The key issue is “how many of these are specified by memory addresses, as opposed to being specified implicitly”
- A 3 address instruction specifies memory addresses for both operands and the result: $R \leftarrow \text{Op1 op Op2}$
- A 2 address instruction overwrites one operand in memory with the result: $\text{Op2} \leftarrow \text{Op1 op Op2}$
- A 1 address instruction has a register, called the **accumulator register** to hold one operand & the result (no address needed):
 $\text{Acc} \leftarrow \text{Acc op Op1}$
- A 0 address + uses a CPU register stack to hold both operands and the result: $\text{TOS} \leftarrow \text{TOS op SOS}$ where TOS is Top Of Stack, SOS is Second On Stack)
- The 4-address instruction, hardly ever seen, also allows the address of the next instruction to specified explicitly.

Fig. 2.3 The 4 Address Instruction



- Explicit addresses for operands, result & next instruction
- Example assumes 24-bit addresses
 - Discuss: size of instruction in bytes

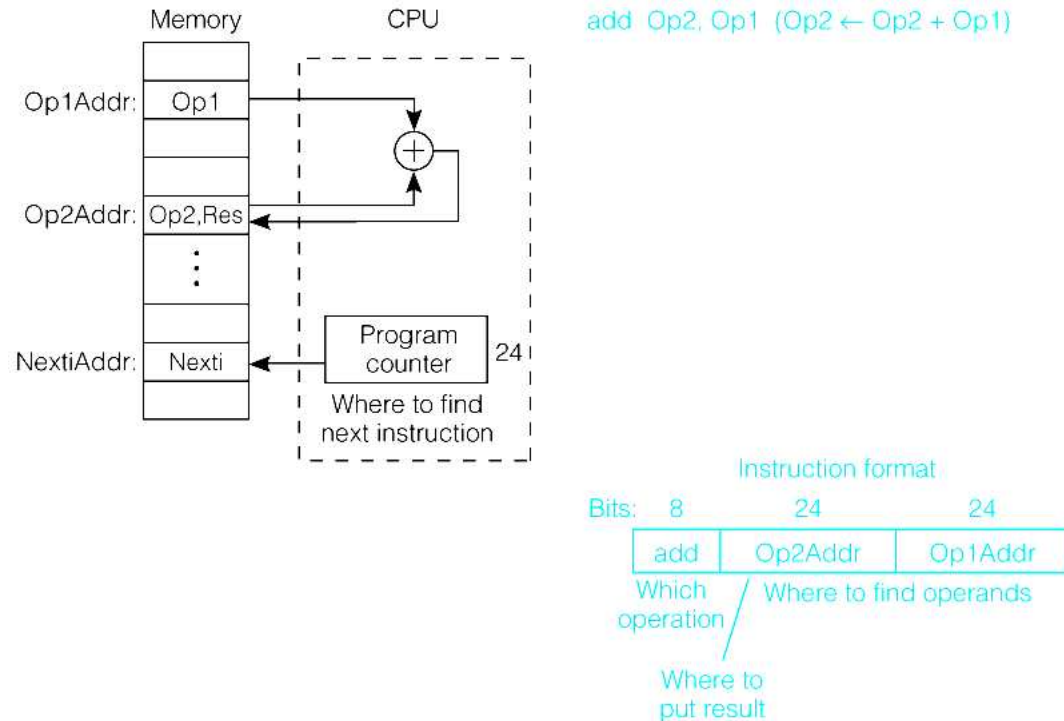
Fig 2.4 The 3 Address Instruction



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- Address of next instruction kept in a processor state register—the PC (Except for explicit Branches/Jumps)
- Rest of addresses in instruction
 - Discuss: savings in instruction word size

Fig. 2.5 The 2 Address Instruction

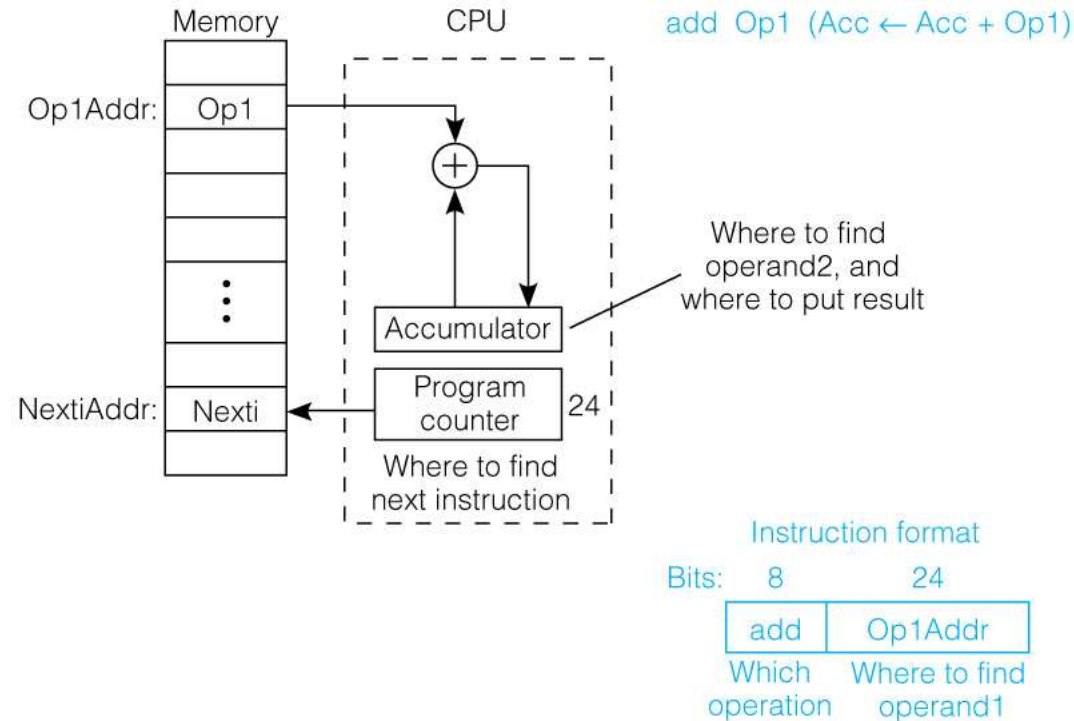


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- Be aware of the difference between address, Op1Addr, and data stored at that address, Op1.
- Result overwrites Operand 2, Op2, with result, Res
- This format needs only 2 addresses in the instruction but there is less choice in placing data

Fig. 2.6 1 Address Instructions

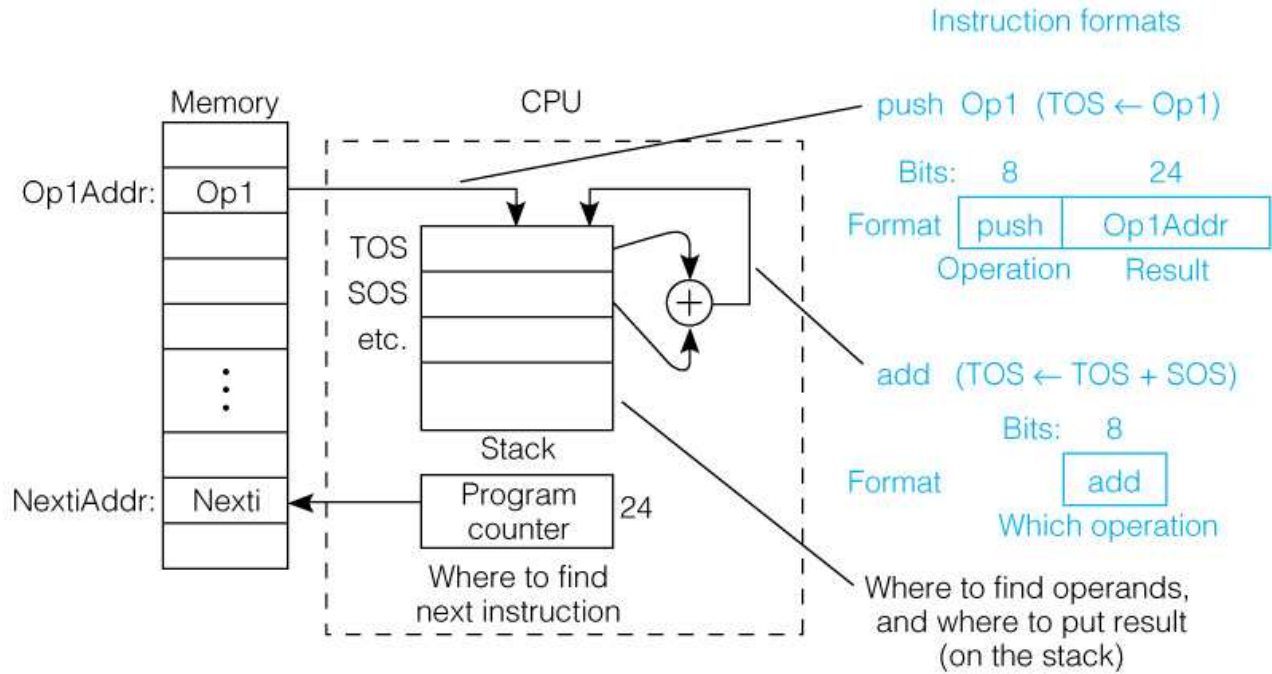
We now need instructions to load and store operands:
LDA OpAddr
STA OpAddr



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- Special CPU register, the accumulator, supplies 1 operand and stores result
- One memory address used for other operand

Fig. 2.7 The 0 Address Instruction



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- Uses a push down stack in CPU
- Arithmetic uses stack for both operands. The result replaces them on the TOS
- Computer must have a 1 address instruction to push and pop operands to and from the stack

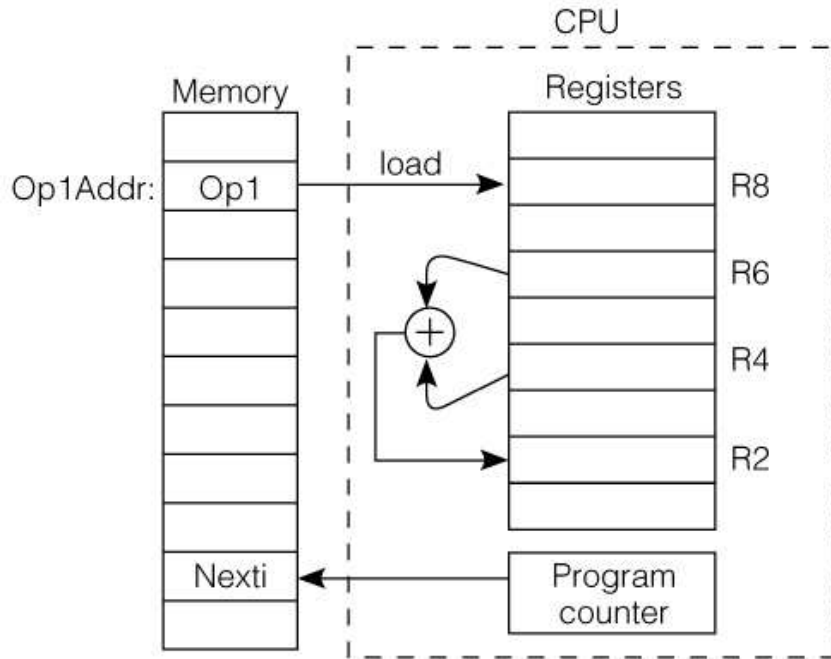
Example 2.1 Expression evaluation for 3-0 address instructions.

Evaluate $a = (b+c)*d-e$ for 3- 2- 1- and 0-address machines.

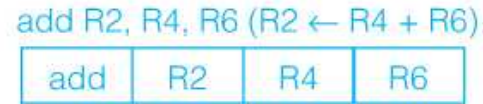
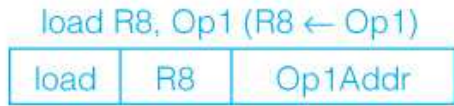
3-Address	2-Address	Accumulator	Stack
<pre>add a,b,c mpy a,a,d sub a,a,e</pre>	<pre>load a,b add a,c mpy a,d sub a,e</pre>	<pre>lda b add c mpy d sub e sta a</pre>	<pre>push b push c add push d mpy push e sub pop a</pre>

- # of instructions & # of addresses both vary
- Discuss as examples: size of code in each case

Fig. 2.8 General Register Machines



Instruction formats



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- It is the most common choice in today's general purpose computers
- *Which* register is specified by small "address" (3 to 6 bits for 8 to 64 registers)
- Load and store have one long & one short address: 1 1/2 addresses
- 2-Operand arithmetic instruction has 3 "half" addresses

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Real Machines are Not So Simple

- Most real machines have a mixture of 3, 2, 1, 0, 1 1/2 address instructions
- A distinction can be made on whether arithmetic instructions use data from memory
- If ALU instructions only use registers for operands and result, machine type is **load-store**
 - Only load and store instructions reference memory
- Other machines have a mix of register-memory and memory-memory instructions

Addressing Modes

- An addressing mode is hardware support for a useful way of determining a memory address
- Different addressing modes solve different HLL problems
 - Some addresses may be known at compile time, e.g. global vars.
 - Others may not be known until run time, e.g. pointers
 - Addresses may have to be *computed*: Examples include:
 - Record (struct) components:
 - variable base(full address) + const.(small)
 - Array components:
 - const. base(full address) + index var.(small)
 - Possible to store constant values w/o using another memory cell by storing them with or adjacent to the instruction itself.

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Addressing modes are simpler than you think

- Operand types (only three basic types)
 - Register specifier (which register)
 - Constant that is part of the instruction
 - Memory contents
- Addressing mode types
 - Register direct
 - Base plus displacement
 - Immediate
 - All others are combinations or degenerate varieties
 - Relative addressing uses PC as a base register
 - Indirect is based with zero displacement
 - Autoincrement/autodecrement is a combined indirect plus increment/decrement

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HLL Examples of Structured Addresses

- C language: `rec -> count`
 - `rec` is a pointer to a record: full address variable
 - `count` is a field name: fixed byte offset, say 24
- C language: `v[i]`
 - `v` is fixed base address of array: full address constant
 - `i` is name of variable index: no larger than array size
- Variables must be contained in registers or memory cells
- Small constants can be contained in the instruction
- Result: need for “address arithmetic.”
 - E.g. Address of `Rec -> Count` is address of `Rec` + offset of `count`.

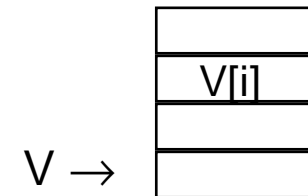
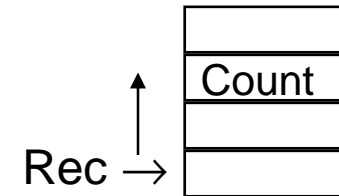
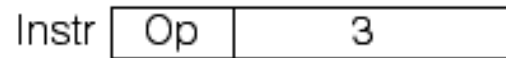


Fig 2.9 Common Addressing Modes a-d

(a) Immediate addressing:

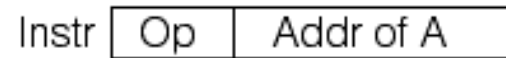
instruction contains the operand



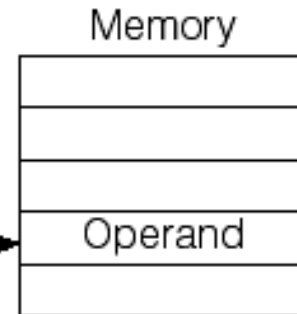
load #3, ...

(b) Direct addressing:

instruction contains address of operand

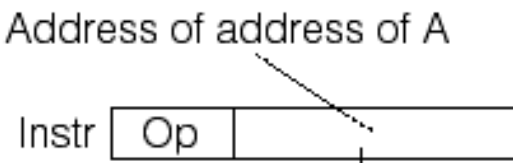


load A, ...

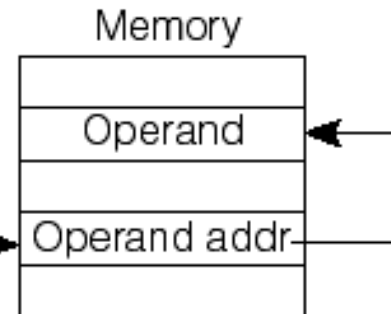


(c) Indirect addressing:

instruction contains address of address of operand



load (A), ...



(d) Register direct addressing:

register contains operand



load R1, ...

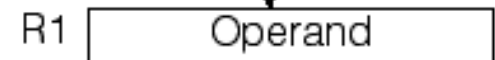
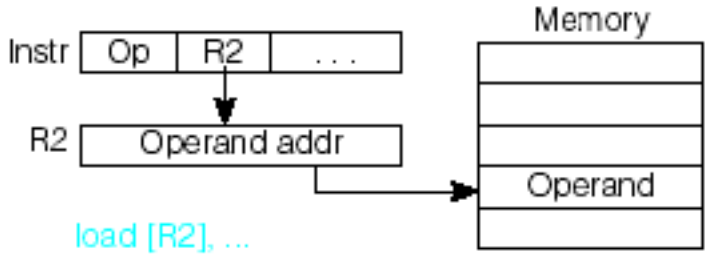
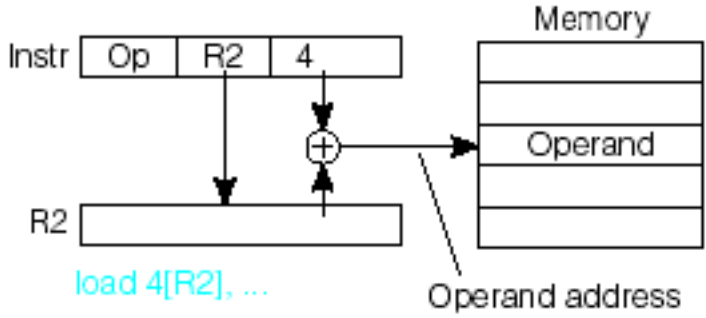


Fig 2.9 Common Addressing Modes e-g

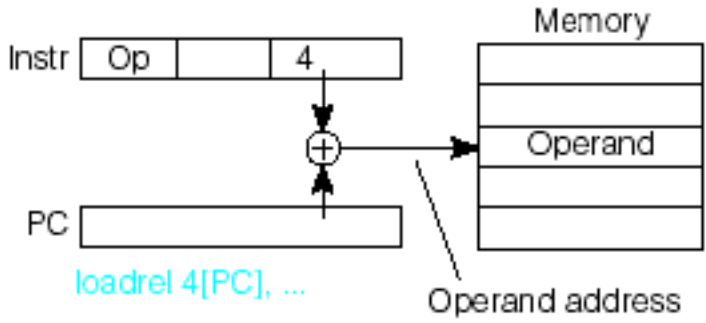
(e) Register indirect addressing:
register contains address of operand



(f) Displacement (based or indexed) addressing:
address of operand = register + constant



(g) Relative addressing:
address of operand = PC + constant

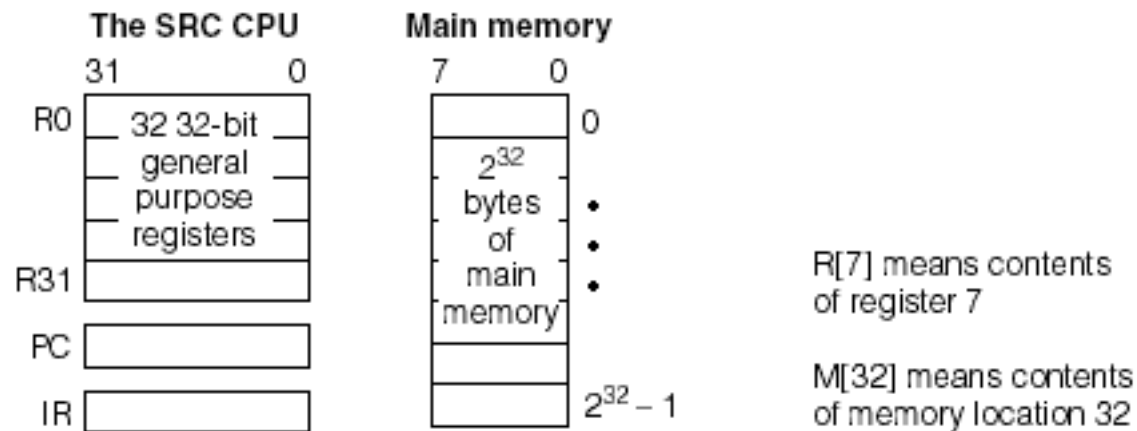


Many addressing modes are really the same mode

- The base plus displacement mode includes many others
 - The base register can also be the zero register or the PC
 - PC-based causes relative addressing
 - Zero-based is absolute – refers only to base page because displacement is small
 - Based-indexed (8086 style, two registers) can be done by an LA, followed by a based-mode
 - Autoincrement modes require additional steps and are used in CISC machines only
 - The address computation step in the processor is the same for zero-register, relative, and based

Fig. 2.10a Example Computer, SRC Simple RISC Computer

- 32 general purpose registers of 32 bits
- 32 bit program counter, PC and instruction reg., IR
- 2^{32} bytes of memory address space



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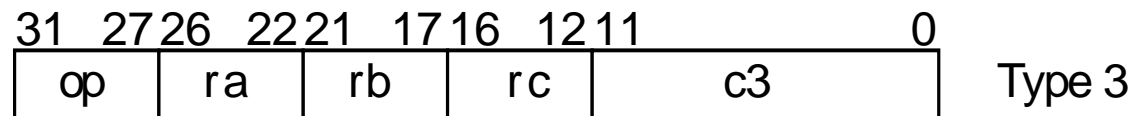
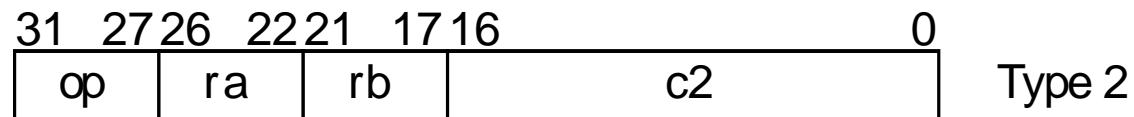
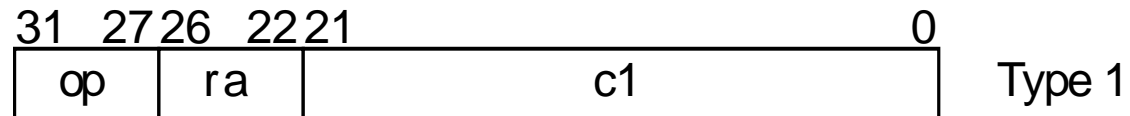
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SRC Characteristics

- (=) Load-store design: only way to access memory is through load and store instructions
 - (–) Operation on 32-bit words only, no byte or half-word operations.
 - (=) Only a few addressing modes are supported
 - (=) ALU Instructions are 3-register type
 - (–) Branch instructions can branch unconditionally or conditionally on whether the value in a specified register is = 0, <> 0, >= 0, or < 0.
 - (–) Branch-and-link instructions are similar, but leave the value of current PC in any register, useful for subroutine return.
 - (–) Can only branch to an address in a register, not to a direct address.
 - (=) All instructions are 32-bits (1-word) long.
- (=) – Similar to commercial RISC machines
- (–) – Less powerful than commercial RISC machines.

SRC Basic Instruction Formats

- There are three basic instruction format types
- The number of register specifier fields and length of the constant field vary
- Other formats result from unused fields or parts



• **Details of formats:**

The repertoire

- The instruction set is inside the back cover of the text
- Instruction types
 - Arithmetic/logic
 - Arithmetic (add/sub) (3-register/immediate)
 - Logic (and/or) (3-register/immediate)
 - Shift/rotate (left/logical right/arithmetic right/circular) (count in register/immediate)
 - Load/store
 - Load (base or relative)
 - Load address (base or relative)
 - Store (base or relative)

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The repertoire (more instruction classes)

- Conditional branch
 - Branch on cc (condition code)
 - Branch on condition and link
- Specials
 - Related to interrupt system
 - Nop
 - Stop
- Addressing modes
 - Only one mode – base and displacement
 - This mode encompasses relative and absolute
 - Address = contents of base register + displacement
 - For relative, PC is the base register
 - For absolute, register zero, which is always zero is the base
 - Normally a general register is the base

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Arithmetic and logic instructions

- Unary operations
 - Both have the same format $op\ ra,rb$ means $(ra) = op\ rb$
 - Operations are not and neg
- Binary operations
 - Two formats
 - Register – three register operands
 $op\ ra, rb, rc$ means $(ra) = rb\ op\ rc$
 - Immediate – two register operands and a number
 $op\ ra, rb,n$ means $(ra) = rb\ op\ n$
 - Operations are add, sub, and, or
 - Immediate versions are addi, andi, ori
 - Subi is done by addi with a negative constant
 - Note that all ALU instructions work with registers only, not memory

Shift instructions

- Operations are:
 - left shift (a zero is shifted in at right)
 - logical right shift (a zero is shifted in at left)
 - arithmetic right shift (the sign bit is shifted in at left)
 - left circular shift (the sign bit is shifted in at right)
- Number of places to shift can be either in a fourth register or an immediate constant (field in the instruction register)

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Load/store instructions

- Only three instructions and one addressing mode
 - ld and ldr
 - st and str
 - la and lar – like ld and ldr but:
 - the address is placed in a register rather than being used for a memory cycle
 - la is really the same as the addi instruction
- Addressing modes
 - Base and displacement is n(rb)
 - Relative is n(PC), coded as a label, assembler calculates n the mnemonic is ldr, str, or lar
 - Absolute is n(r0)
 - Indirect is 0(rb)
- Assemblers often calculate the base and displacement values for you from program or data labels

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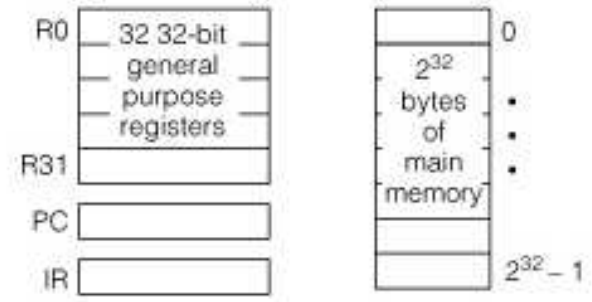
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Branch (including branch and link) instructions

- The only two branch instructions are:
 - br?? branch on condition code
 - brl?? branch on condition code and save PC in link
 - Condition codes are
 - (blank) always, antonym nv – never
 - Zr zero, antonym nz – nonzero
 - mi minus, antonym pl – plus or zero
 - Condition code is based on register rc of the instruction
 - Destination is address in rb, almost always placed there by a preceding lar instruction
 - Return address is placed in ra if the instruction is a brl
- Examples
 - brlnz ra, rb, rc – branch to address in rb if rc is not zero, store return address in ra
 - br rb – unconditional branch to address in rb , rc not needed
 - brl rb – unconditional gosub to address in rb , return address in ra, rc not needed
 - brlmi rb –conditional gosub to address in rb , return address in ra, if rc is minus

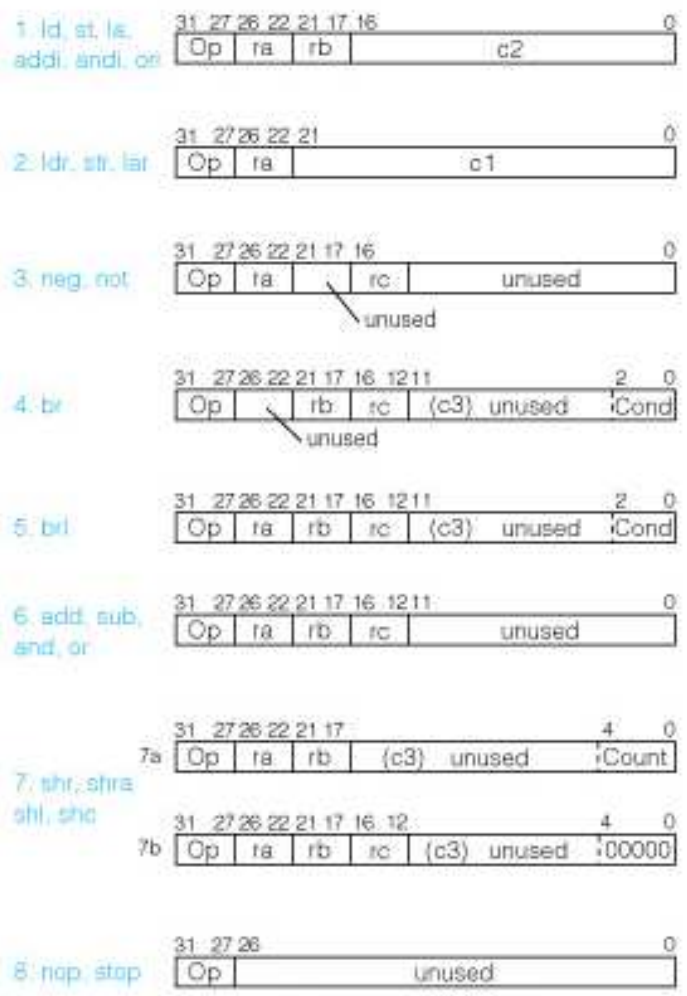
Fig 2.10 cont'd. SR(instructions



R[7] means contents of register 7

M[32] means contents of memory location 32

Instruction formats



Example

ld r3, A (R[3] = M[A])
ld r3, 4(r5) (R[3] = M[R[5] + 4])
addi r2, r4, 1 (R[2] = R[4] + 1)

ldr r5, 8 (R[5] = M[PC + 8])
lsr r6, 45 (R[6] = PC + 45)

neg r7, r9 (R[7] = -R[9])

brz r4, r0 (branch to R[4] if R[0] == 0)

brnz r6, r4, r0 (R[6] = PC; branch to R[4] if R[0] ≠ 0)

add r0, r2, r4 (R[0] = R[2] + R[4])

shr r0, r1, 4 (R[0] = R[1] shifted right by 4 bits)

shl r2, r4, r6 (R[2] = R[4] shifted left by count in R[6])

stop

Tbl 2.4 Example Load & Store Instructions: Memory Addressing

- Address can be constant, constant+register, or constant+PC
- Memory contents or address itself can be loaded

Instruction	op	ra	rb	c1	Meaning	Addressing Mode
ld r1, 32	1	1	0	32	$R[1] \leftarrow M[32]$	Direct
ld r22, 24(r4)	1	22	4	24	$R[22] \leftarrow M[24+R[4]]$	Displacement
st r4, 0(r9)	3	4	9	0	$M[R[9]] \leftarrow R[4]$	Register indirect
la r7, 32	5	7	0	32	$R[7] \leftarrow 32$	Immediate
ldr r12, -48	2	12	-	-48	$R[12] \leftarrow M[PC -48]$	Relative
lar r3, 0	6	3	-	0	$R[3] \leftarrow PC$	Register (!)

(note use of la to load a constant)

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Assembly Language Forms of Arithmetic and Logic Instructions

Format	Example	Meaning
neg ra, rc	neg r1, r2	;Negate ($r1 = -r2$)
not ra, rc	not r2, r3	;Not ($r2 = r3'$)
add ra, rb, rc	add r2, r3, r4	;2's complement addition
sub ra, rb, rc		;2's complement subtraction
and ra, rb, rc		;Logical and
or ra, rb, rc		;Logical or
addi ra, rb, c2	addi r1, r3, 1	;Immediate 2's complement add
andi ra, rb, c2		;Immediate logical and
ori ra, rb, c2		;Immediate logical or

- Immediate subtract not needed since constant in addi may be negative

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Branch Instruction Format

2/ There are actually only two branch op codes:

`br rb, rc, c3<2..0>` ;branch to R[rb] if R[rc] meets
; the condition defined by `c3<2..0>`

`brl ra, rb, rc, c3<2..0>` ; R[ra] ← PC; branch as above

- It is `c3<2..0>`, the 3 lsbs of `c3`, that governs what the branch condition is:

<u>lsbs</u>	<u>condition</u>	<u>Assy language form</u>	<u>Example</u>
000	never	<code>brInv</code>	<code>brInv r6</code>
001	always	<code>br, brl</code>	<code>br r5, brl r5</code>
010	if <code>rc = 0</code>	<code>brzr, brl zr</code>	<code>brzr r2, r4</code>
011	if <code>rc ≠ 0</code>	<code>brnz, brlnz</code>	
100	if <code>rc ≥ 0</code>	<code>brpl, brlpl</code>	
101	if <code>rc < 0</code>	<code>brmi, brlmi</code>	

- Note that branch target address is always in register R[rb].
- It must be placed there explicitly by a previous instruction.

Tbl. 2.6 Branch Instruction Examples

Ass'y lang.	Example instr.	Meaning	op	ra	rb	rc	c3 ⟨2..0⟩	Branch Cond'n.
brlnv	brlnv r6	$R[6] \leftarrow PC$	9	6	—	—	000	never
br	br r4	$PC \leftarrow R[4]$	8	—	4	—	001	always
brl	brl r6,r4	$R[6] \leftarrow PC;$ $PC \leftarrow R[4]$	9	6	4	—	001	always
brzr	brzr r5,r1	if (R[1]=0) $PC \leftarrow R[5]$	8	—	5	1	010	zero
brlzt	brlzt r7,r5,r1	$R[7] \leftarrow PC;$	9	7	5	1	010	zero
brnz	brnz r1, r0	if (R[0]≠0) $PC \leftarrow R[1]$	8	—	1	0	011	nonzero
brlnzt	brlnzt r2,r1,r0	$R[2] \leftarrow PC;$ if (R[0]≠0) $PC \leftarrow R[1]$	9	2	1	0	011	nonzero
brpl	brpl r3, r2	if (R[2]□0) $PC \leftarrow R[3]$	8	—	3	2	100	plus
brlpl	brlpl r4,r3,r2	$R[4] \leftarrow PC;$ if (R[2]□0) $PC \leftarrow R[3]$	9	4	3	2		plus
brmi	brmi r0, r1	if (R[1]<0) $PC \leftarrow R[0]$	8	—	0	1	101	minus
brlmi	brlmi r3,r0,r1	$R[3] \leftarrow PC;$ if (r1<0) $PC \leftarrow R[0]$	9	3	0	1		minus

Branch Instructions—Example

C: goto Label3

SRC:

```
    lar r0, Label3      ; put branch target address into tgt reg.  
    br r0               ; and branch  
    . . .
```

Label3 . . .

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Example of conditional branch

in C: #define Cost 125
if (X<0) then X = -X;

in SRC:

```
Cost .equ 125           ;define symbolic constant
      .org 1000         ;next word will be loaded at address 100010
X:    .dw 1             ;reserve 1 word for variable X
      .org 5000        ;program will be loaded at location 500010
      lar r31, Over    ;load address of "false" jump location
      ld r1, X          ;load value of X into r1
      brpl r31, r1     ;branch to Else if r1 ≥ 0
      neg r1, r1       ;negate value
Over: ...              ;continue
```


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RTN (Register Transfer Notation)

- Provides a formal means of describing machine structure and function
- Is at the “just right” level for machine descriptions
- Does not replace hardware description languages.
- Can be used to describe *what* a machine does (an Abstract RTN) without describing *how* the machine does it.
- Can also be used to describe a particular hardware implementation (A Concrete RTN)

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RTN Notation (Cont'd.)

- At first you may find this “meta description” confusing, because it is a language that is used to describe a language.
- You will find that developing a familiarity with RTN will aid greatly in your understanding of new machine design concepts.
- We will describe RTN by using it to describe SRC.

Some RTN Features— Using RTN to describe a machine's static properties

Static Properties

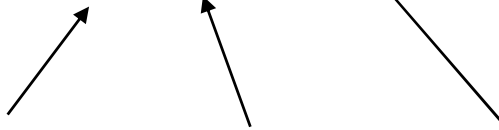
- Specifying registers
 - $IR\langle 31..0 \rangle$ specifies a register named “IR” having 32 bits numbered 31 to 0
- “Naming” using the := naming operator:
 - $op\langle 4..0 \rangle := IR\langle 31..27 \rangle$ specifies that the 5 msbs of IR be called op, with bits 4..0.
 - Notice that this does not create a new register, it just generates another name, or “alias” for an already existing register or part of a register.

Using RTN to describe Dynamic Properties

Dynamic Properties

- Conditional expressions:

$(op=12) \rightarrow R[ra] \leftarrow R[rb] + R[rc];$; defines the add instruction



“if” condition “then” RTN Assignment Operator

This fragment of RTN describes the SRC add instruction. It says, “when the op field of IR = 12, then store in the register specified by the ra field, the result of adding the register specified by the rb field to the register specified by the rc field.”



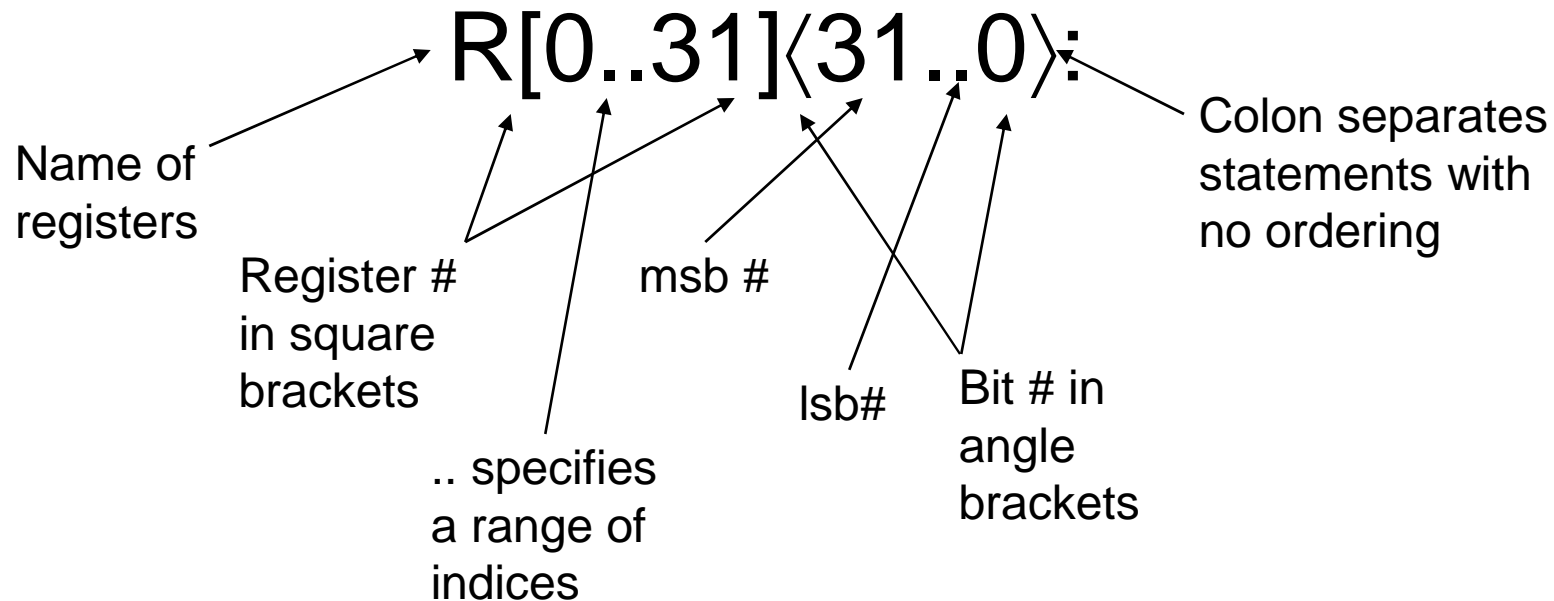
Using RTN to describe the SRC (static) Processor State

Processor state

- PC $\langle 31..0 \rangle$: program counter
(memory addr. of next inst.)
- IR $\langle 31..0 \rangle$: instruction register
- Run: one bit run/halt indicator
- Strt: start signal
- R[0..31] $\langle 31..0 \rangle$: general purpose registers

RTN Register Declarations

- General register specifications shows some features of the notation
- Describes a set of 32 32-bit registers with names R[0] to R[31]



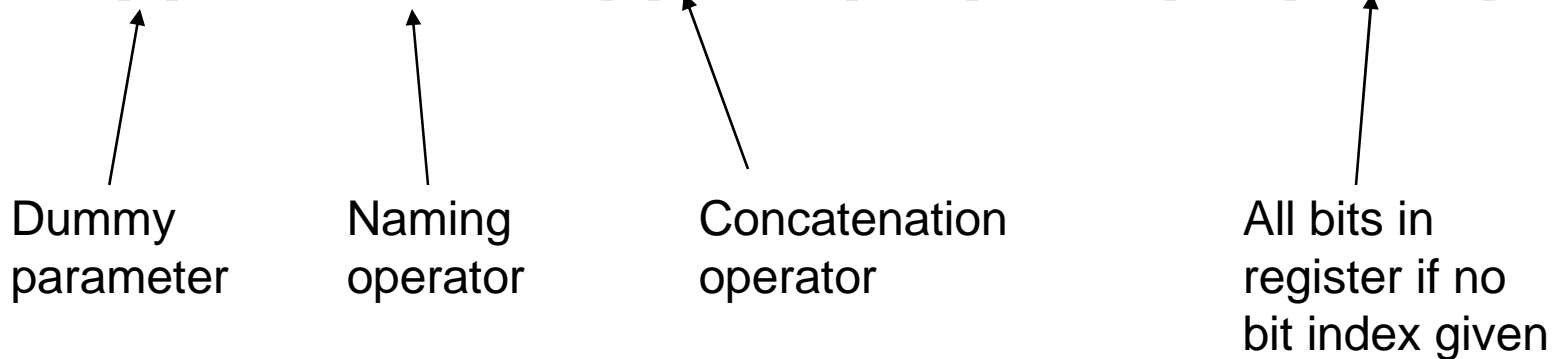
Memory Declaration: RTN Naming Operator

- Defining names with formal parameters is a powerful formatting tool
- Used here to define word memory (big endian)

Main memory state

$\text{Mem}[0..2^{32} - 1]\langle 7..0 \rangle$: 2^{32} addressable bytes of memory

$\text{M}[x]\langle 31..0 \rangle := \text{Mem}[x]\#\text{Mem}[x+1]\#\text{Mem}[x+2]\#\text{Mem}[x+3]$:





RTN Instruction Formatting Uses Renaming of IR Bits

Instruction formats

$op\langle 4..0 \rangle := IR\langle 31..27 \rangle:$	operation code field
$ra\langle 4..0 \rangle := IR\langle 26..22 \rangle:$	target register field
$rb\langle 4..0 \rangle := IR\langle 21..17 \rangle:$	operand, address index, or branch target register
$rc\langle 4..0 \rangle := IR\langle 16..12 \rangle:$	second operand, conditional test, or shift count register
$c1\langle 21..0 \rangle := IR\langle 21..0 \rangle:$	long displacement field
$c2\langle 16..0 \rangle := IR\langle 16..0 \rangle:$	short displacement or immediate field
$c3\langle 11..0 \rangle := IR\langle 11..0 \rangle:$	count or modifier field

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Specifying dynamic properties of SRC: RTN Gives Specifics of Address Calculation

Effective address calculations (occur at runtime):

$\text{disp}\langle 31..0 \rangle := ((\text{rb}=0) \rightarrow \text{c2}\langle 16..0 \rangle \{\text{sign extend}\}:$	displacement
$(\text{rb}\neq 0) \rightarrow \text{R}[\text{rb}] + \text{c2}\langle 16..0 \rangle \{\text{sign extend, 2's comp.}\}):$	address
$\text{rel}\langle 31..0 \rangle := \text{PC}\langle 31..0 \rangle + \text{c1}\langle 21..0 \rangle \{\text{sign extend, 2's comp.}\}:$	relative
address	

- Renaming defines displacement and relative addrs.
- New RTN notation is used
 - $\text{condition} \rightarrow \text{expression}$ means if condition then expression
 - modifiers in $\{ \}$ describe type of arithmetic or how short numbers are extended to longer ones
 - arithmetic operators (+ - * / etc.) can be used in expressions
- Register R[0] cannot be added to a displacement

Detailed Questions Answered by the RTN for Addresses

- What set of memory cells can be addressed by direct addressing (displacement with $rb=0$)
 - If $c2\langle 16\rangle=0$ (positive displacement) absolute addresses range from 00000000H to 0000FFFFH
 - If $c2\langle 16\rangle=1$ (negative displacement) absolute addresses range from FFFF0000H to FFFFFFFFH
- What range of memory addresses can be specified by a relative address
 - The largest positive value of $C1\langle 21..0\rangle$ is $2^{21}-1$ and its most negative value is -2^{21} , so addresses up to $2^{21}-1$ forward and 2^{21} backward from the current PC value can be specified
- Note the difference between rb and $R[rb]$

Instruction Interpretation: RTN Description of Fetch/Execute

- Need to describe actions (not just declarations)
- Some new notation

Logical NOT

Logical AND

instruction_interpretation := (
 \neg Run \wedge Strt \rightarrow Run \leftarrow 1:
 Run \rightarrow (IR \leftarrow M[PC]; PC \leftarrow PC + 4; instruction_execution));

Register transfer

Separates statements that occur in sequence

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RTN Sequence and Clocking

- In general, RTN statements separated by `:` take place during the same clock pulse
- Statements separated by `;` take place on successive clock pulses
- This is not entirely accurate since some things written with one RTN statement can take several clocks to perform
- More precise difference between `:` and `;`
 - The order of execution of statements separated by `:` does not matter
 - If statements are separated by `;` the one on the left must be complete before the one on the right starts

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Synchronous vs. asynchronous logic

- HLL's (imperative languages) describe sequential systems because they operate with a single thread of control
- Real systems are multithreaded
- Simulation languages (Spice, Matlab, VHDL) can describe such dynamical systems
- If you describe a processor in an imperative language (C family) you have to adapt your description to fit the sequential nature of the language
- LogicWorks is really a hybrid
- RTN describes only clocked logic – each clock cycle can include several noninteracting operations active in the same cycle
- The synchronization operators are (:, simultaneous but independent) and (;, sequential)

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More about Instruction Interpretation RTN

- In the expression $IR \leftarrow M[PC]: PC \leftarrow PC + 4;$ which value of PC applies to $M[PC]$?
- The rule in RTN is that all right hand sides of “:” - separated RTs are evaluated before any LHS is changed
 - In logic design, this corresponds to “master-slave” operation of flip-flops
- We see what happens when Run is true and when Run is false but Strt is true. What about the case of Run and Strt both false?
 - Since no action is specified for this case, the RTN implicitly says that no action occurs in this case

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Individual Instructions

- `instruction_interpretation` contained a forward reference to `instruction_execution`
- `instruction_execution` is a long list of conditional operations
 - The condition is that the op code specifies a given inst.
 - The operation describes what that instruction does
- Note that the operations of the instruction are done after (;) the instruction is put into IR and the PC has been advanced to the next inst.

RTN Instruction Execution for Load and Store Instructions

```

instruction_execution := (
  ld (:= op= 1) → R[ra] ← M[disp]:      load register
  ldr (:= op= 2) → R[ra] ← M[rel]:      load register relative
  st (:= op= 3) → M[disp] ← R[ra]:      store register
  str (:= op= 4) → M[rel] ← R[ra]:      store register relative
  la (:= op= 5 ) → R[ra] ← disp:load displacement address
  lar (:= op= 6) → R[ra] ← rel:         load relative address

```

- The in-line definition (:= op=1) saves writing a separate definition `ld := op=1` for the `ld` mnemonic
- The previous definitions of `disp` and `rel` are needed to understand all the details

SRC RTN—The Main Loop

```

ii := instruction_interpretation:
ie := instruction_execution :

ii := ( ¬Run ∧ Strt → Run ← 1:
        Run → (IR ← M[PC]: PC ← PC + 4;
                ie) );

ie := (
    ld (:= op= 1) → R[ra] ← M[disp]:
    ldr (:= op= 2) → R[ra] ← M[rel]:
    ...
    stop (:= op= 31) → Run ← 0:
); ii

```

Big switch
statement
on the opcode

Thus ii and ie invoke each other, as coroutines.
This pair actually defines the fetch-execute cycle; running until a stop instruction halts the processor

Use of RTN Definitions: Text Substitution Semantics

ld (:= op= 1) → R[ra] ← M[disp]:

disp⟨31..0⟩ := ((rb=0) → c2⟨16..0⟩ {sign extend}):

(rb≠0) → R[rb] + c2⟨16..0⟩ {sign extend, 2's comp.}):

ld (:= op= 1) → R[ra] ← M[

((rb=0) → c2⟨16..0⟩ {sign extend}):

(rb≠0) → R[rb] + c2⟨16..0⟩ {sign extend, 2's comp.}):

]:

- An example:
 - If IR = 00001 00101 00011 00000000000001011
 - then ld → R[5] ← M[R[3] + 11]:

RTN Descriptions of SRC Branch Instructions

- Branch condition determined by 3 lsbs of inst.
- Link register (R[ra]) set to point to next inst.

cond := (c3<2..0>=0 → 0:	never
c3<2..0>=1 → 1:	always
c3<2..0>=2 → R[rc]=0:	if register is zero
c3<2..0>=3 → R[rc]≠0:	if register is nonzero
c3<2..0>=4 → R[rc]<31>=0:	if positive or zero
c3<2..0>=5 → R[rc]<31>=1):	if negative
br (:= op= 8) → (cond → PC ← R[rb]):	conditional branch
brl (:= op= 9) → (R[ra] ← PC: cond → (PC ← R[rb]))):	branch and link

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RTN for Arithmetic and Logic

add ($:=$ op=12) \rightarrow R[ra] \leftarrow R[rb] + R[rc]:

addi ($:=$ op=13) \rightarrow R[ra] \leftarrow R[rb] + c2<16..0> {2's comp. sign ext.}:

sub ($:=$ op=14) \rightarrow R[ra] \leftarrow R[rb] - R[rc]:

neg ($:=$ op=15) \rightarrow R[ra] \leftarrow -R[rc]:

and ($:=$ op=20) \rightarrow R[ra] \leftarrow R[rb] \wedge R[rc]:

andi ($:=$ op=21) \rightarrow R[ra] \leftarrow R[rb] \wedge c2<16..0> {sign extend}:

or ($:=$ op=22) \rightarrow R[ra] \leftarrow R[rb] \vee R[rc]:

ori ($:=$ op=23) \rightarrow R[ra] \leftarrow R[rb] \vee c2<16..0> {sign extend}:

not ($:=$ op=24) \rightarrow R[ra] \leftarrow \neg R[rc]:

- Logical operators: and \wedge or \vee and not \neg

RTN for Shift Instructions

- Count may be 5 lsbs of a register or the instruction
- Notation: @ - replication, # - concatenation

$$n := (\quad (c3\langle 4..0 \rangle = 0) \rightarrow R[rc]\langle 4..0 \rangle : \\ (c3\langle 4..0 \rangle \neq 0) \rightarrow c3\langle 4..0 \rangle) :$$
$$\text{shr} (:= \text{op}=26) \rightarrow R[ra]\langle 31..0 \rangle \leftarrow (n @ 0) \# R[rb]\langle 31..n \rangle :$$
$$\text{shra} (:= \text{op}=27) \rightarrow R[ra]\langle 31..0 \rangle \leftarrow (n @ R[rb]\langle 31 \rangle) \# R[rb]\langle 31..n \rangle :$$
$$\text{shl} (:= \text{op}=28) \rightarrow R[ra]\langle 31..0 \rangle \leftarrow R[rb]\langle 31-n..0 \rangle \# (n @ 0) :$$
$$\text{shc} (:= \text{op}=29) \rightarrow R[ra]\langle 31..0 \rangle \leftarrow R[rb]\langle 31-n..0 \rangle \# R[rb]\langle 31..32-n \rangle :$$

Example of Replication and Concatenation in Shift

- Arithmetic shift right by 13 concatenates 13 copies of the sign bit with the upper 19 bits of the operand

shra r1, r2, 13

R[2]=

1001 0111 1110 1010 1110 1100 0001 0110

R[1]=

13@R[2]<31> #	R[2]<31..13>
1111 1111 1111 1	100 1011 1111 0101 0111

Assembly Language for Shift

- Form of assembly language instruction tells whether to set c3=0

```
shr ra, rb, rc           ;Shift rb right into ra by 5 lsbs of rc
shr ra, rb, count       ;Shift rb right into ra by 5 lsbs of inst
shra ra, rb, rc         ;AShift rb right into ra by 5 lsbs of rc
shra ra, rb, count     ;AShift rb right into ra by 5 lsbs of inst
shl ra, rb, rc          ;Shift rb left into ra by 5 lsbs of rc
shl ra, rb, count       ;Shift rb left into ra by 5 lsbs of inst
shc ra, rb, rc          ;Shift rb circ. into ra by 5 lsbs of rc
shc ra, rb, count       ;Shift rb circ. into ra by 5 lsbs of inst
```

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End of RTN Definition of instruction_execution

nop (:= op= 0) → :	No operation
stop (:= op= 31) → Run ← 0:	Stop instruction
);	End of instruction_execution
instruction_interpretation.	

- We will find special use for nop in pipelining
- The machine waits for Strt after executing stop
- The long conditional statement defining instruction_execution ends with a direction to go repeat instruction_interpretation, which will fetch and execute the next instruction (if Run still =1)

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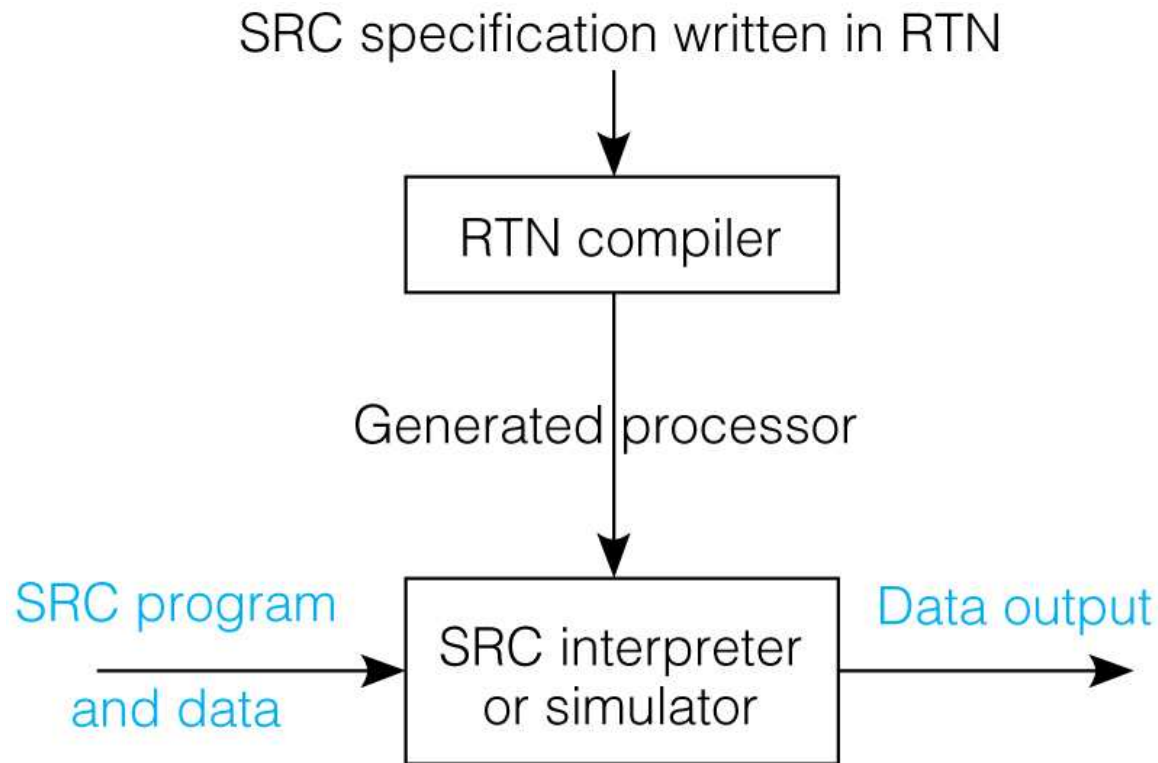
Confused about RTN and SRC?

- SRC is a Machine Language
 - It can be interpreted by either hardware or software simulator.
- RTN is a *Specification Language*
 - Specification languages are languages that are used to specify other languages or systems—a *metalanguage*.
 - Other examples: LEX, YACC, VHDL, Verilog

Figure 2.10 may help clear this up...

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Fig 2.11 The Relationship of RTN to SRC



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A Note about Specification Languages

- They allow the description of *what* without having to specify *how*.
- They allow precise and unambiguous specifications, unlike natural language.
- They reduce errors:
 - errors due to misinterpretation of imprecise specifications written in natural language
 - errors due to confusion in design and implementation - “human error.”
- Now the designer must debug the specification!
- Specifications can be automatically checked and processed by tools.
 - An RTN specification could be input to a simulator generator that would produce a simulator for the specified machine.
 - An RTN specification could be input to a compiler generator that would generate a compiler for the language, whose output could be run on the simulator.

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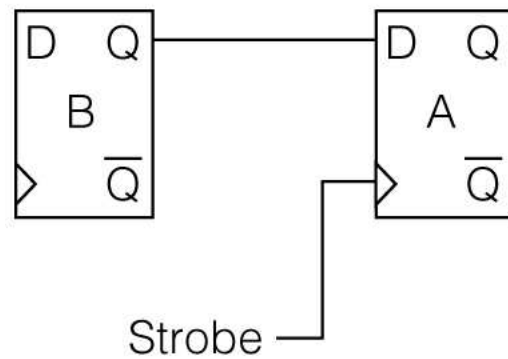
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Addressing Modes Described in RTN (Not SRC)

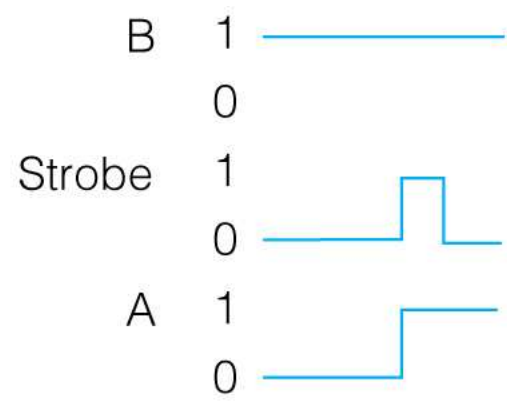
<u>Mode name</u>	<u>Assembler Syntax</u>	<u>RTN meaning</u>	<u>Use</u>
Register	Ra	$R[t] \leftarrow R[a]$	Target register Tmp. Var.
Register indirect	(Ra)	$R[t] \leftarrow M[R[a]]$	Pointer
Immediate	#X	$R[t] \leftarrow X$	Constant
Direct, absolute	X	$R[t] \leftarrow M[X]$	Global Var.
Indirect	(X)	$R[t] \leftarrow M[M[X]]$	Pointer Var.
Indexed, based, or displacement	X(Ra)	$R[t] \leftarrow M[X + R[a]]$	Arrays, structs
Relative	X(PC)	$R[t] \leftarrow M[X + PC]$	Vals stored w pgm
Autoincrement	(Ra)+	$R[t] \leftarrow M[R[a]]; R[a] \leftarrow R[a] + 1$	Sequential
Autodecrement	-(Ra)	$R[a] \leftarrow R[a] - 1; R[t] \leftarrow M[R[a]]$	access.

Fig. 2.12 Register transfers can be mapped to Digital Logic Circuits.

- Implementing the RTN statement $A \leftarrow B$



(a) Hardware

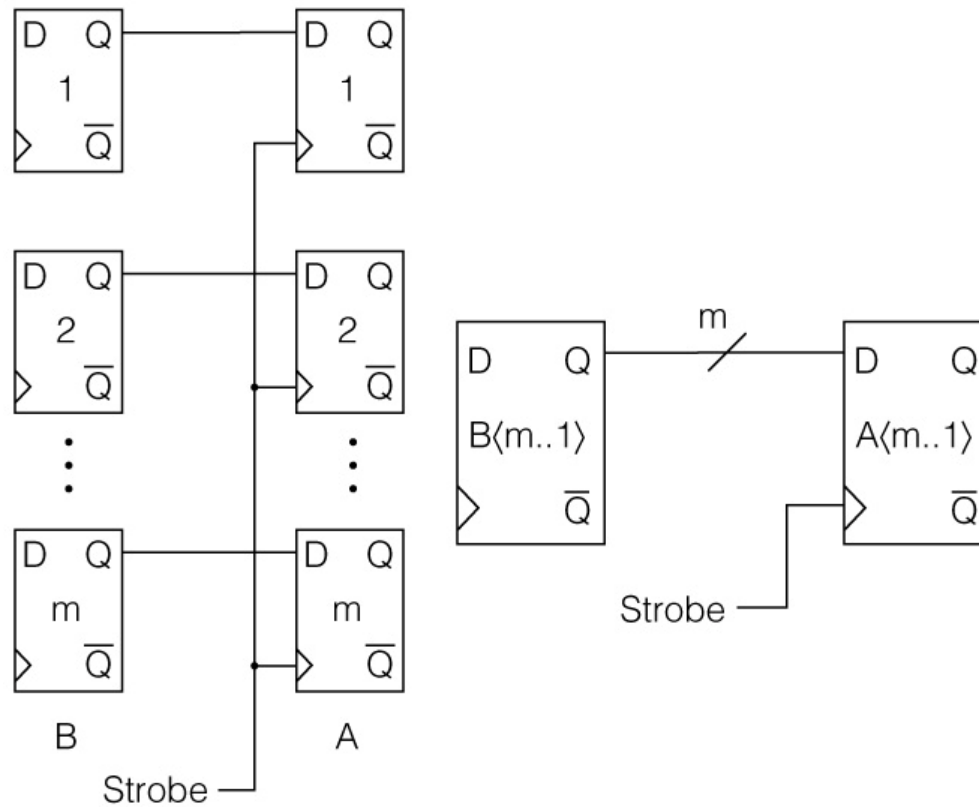


(b) Timing

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Fig. 2.13 Multiple Bit Register Transfer

- Implementing $A\langle m..1 \rangle \leftarrow B\langle m..1 \rangle$



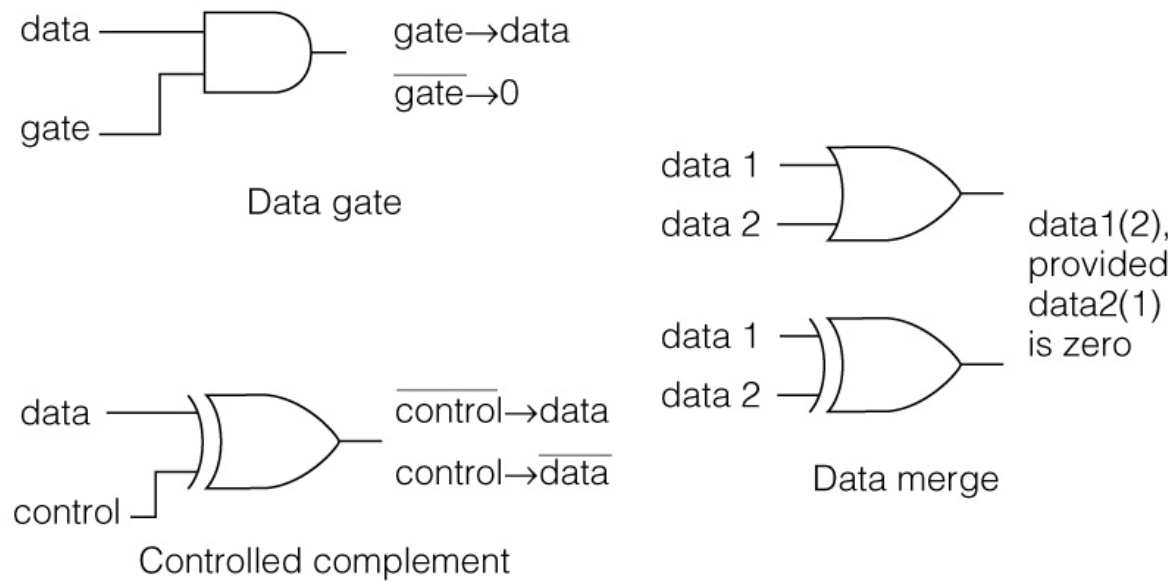
(a) Individual flip-flops

(b) Abbreviated notation

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Fig. 2.14 Data Transmission View of Logic Gates

- Logic gates can be used to control the transmission of data:



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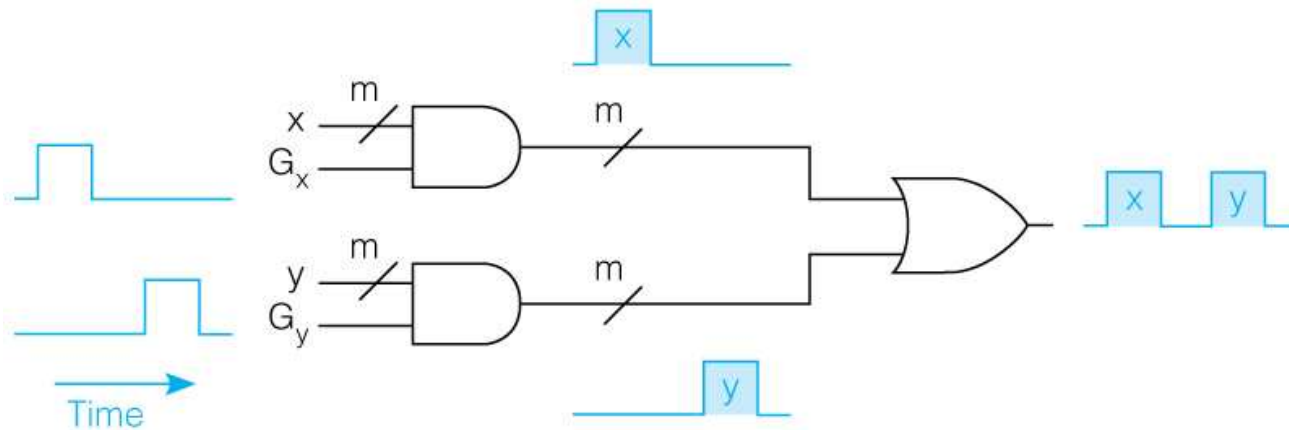
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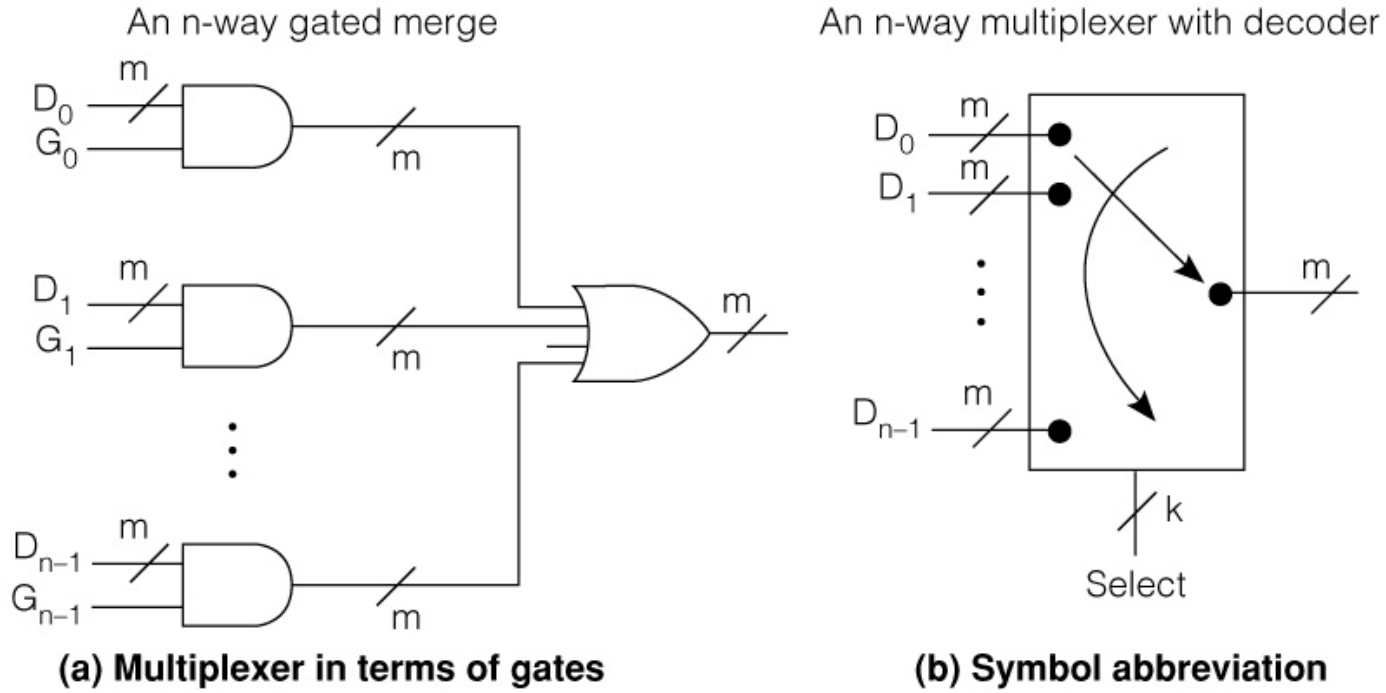
Fig. 2.15 Multiplexer as a 2 Way Gated Merge

- Data from multiple sources can be selected for transmission



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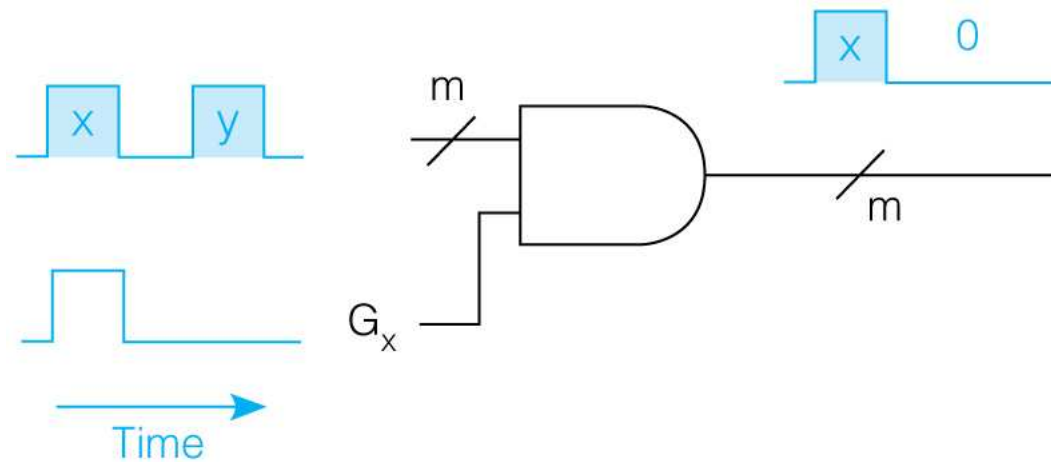
Fig. 2.16 m-bit Multiplexer and Symbol



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- Multiplexer gate signals G_i may be produced by a binary to one-out-of-n decoder

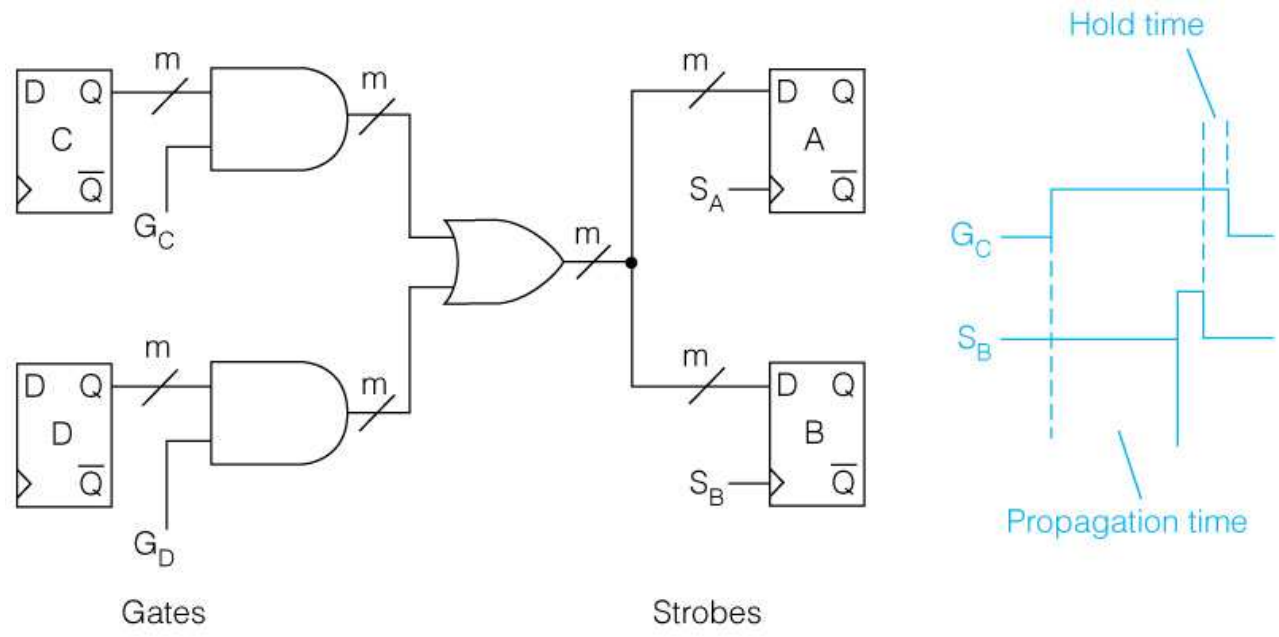
Fig. 2.17 Separating Merged Data



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- Merged data can be separated by gating at the right time
- It can also be strobed into a flip-flop when valid

Fig. 2.18 Multiplexed Register Transfers using Gates and Strobes



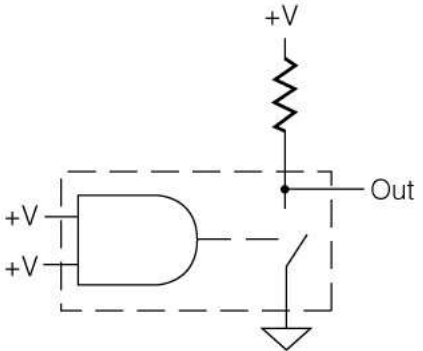
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- Selected gate and strobe determine which Register is Transferred to where.
- $A \leftarrow C$, and $B \leftarrow C$ can occur together, but not $A \leftarrow C$, and $B \leftarrow D$

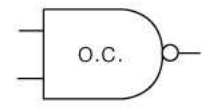
Fig. 2.19 Open-Collector NAND Gate Output Circuit

Inputs		Output	
0v	0v	Open	(Out = +V)
0v	+V	Open	(Out = +V)
+V	0v	Open	(Out = +V)
+V	+V	Closed	(Out = 0v)

(a) Open-collector NAND truth table



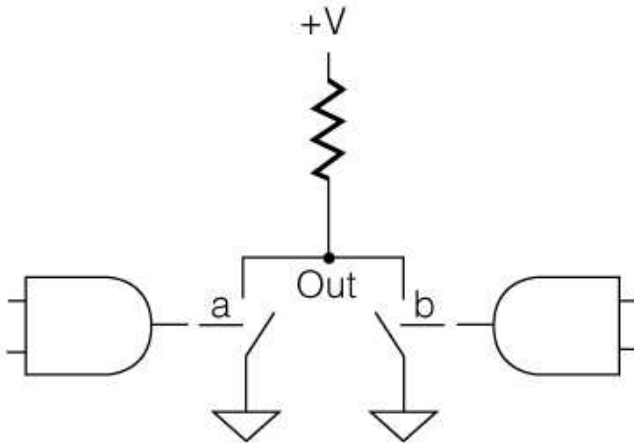
(b) Open-collector NAND



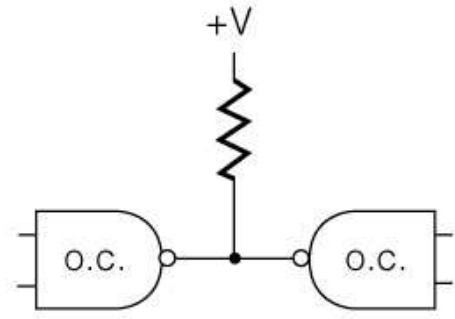
(c) Symbol

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Fig. 2.20 Wired AND Connection of Open-Collector Gates



(a) Wired AND connection



(b) With symbols

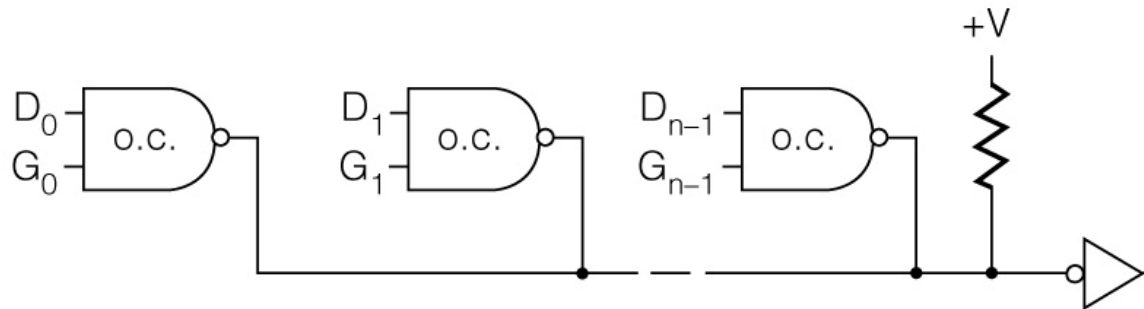
Switch		Wired AND output
a	b	
Closed(0)	Closed(0)	0v (0)
Closed(0)	Open (1)	0v (0)
Open (1)	Closed(0)	0v (0)
Open (1)	Open (1)	+V (1)

(c) Truth table

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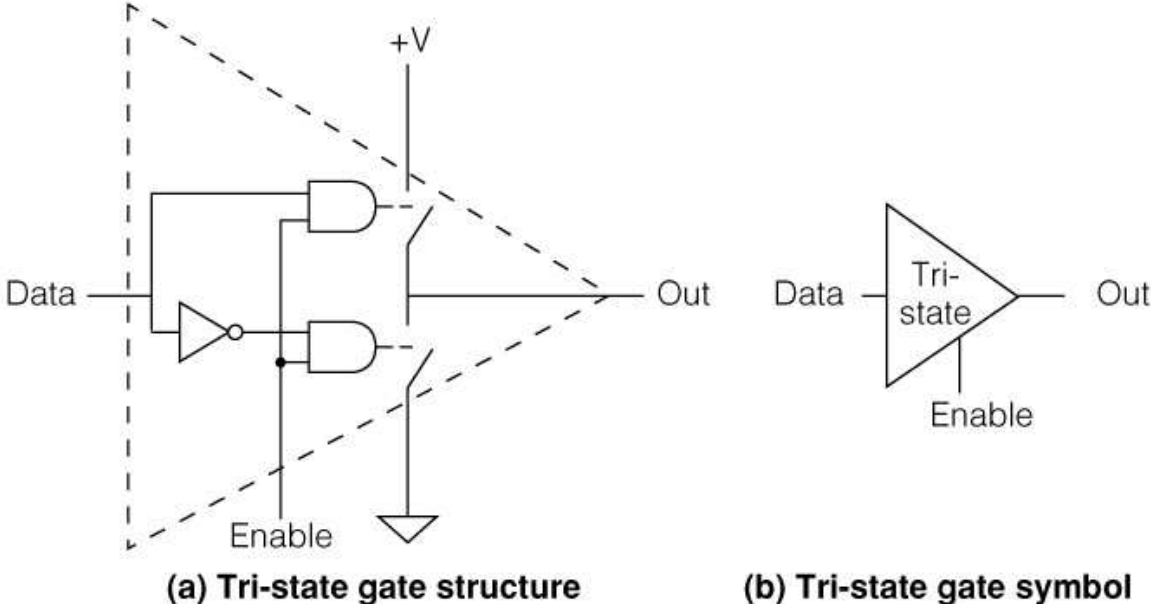
Fig. 2.21 Open Collector Wired OR Bus

- DeMorgan's OR by not of AND of nots
- Pull-up resistor removed from each gate - open collector
- One pull-up resistor for whole bus
- Forms an OR distributed over the connection



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Fig. 2.22 Tri-state Gate Internal Structure and Symbol



(a) Tri-state gate structure

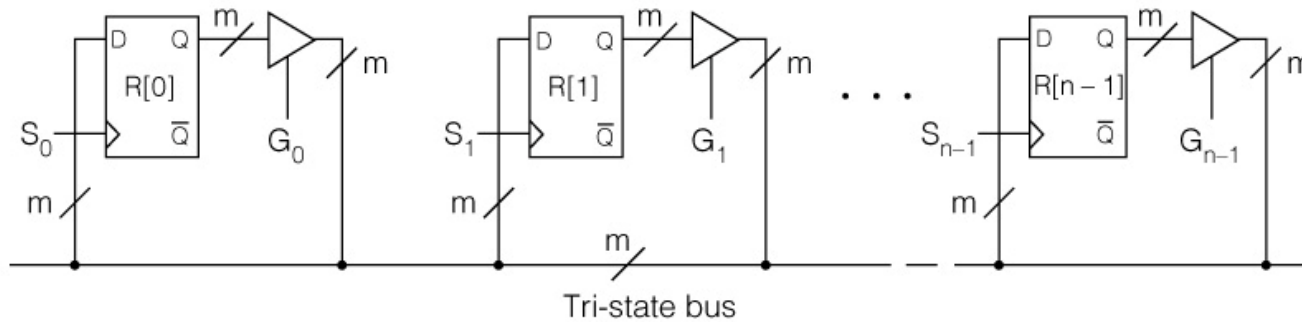
(b) Tri-state gate symbol

Enable	Data	Output
0	0	Hi-Z
0	1	Hi-Z
1	0	0
1	1	1

(c) Tri-state gate truth table

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Fig. 2.23 Registers Connected by a Tri-state Bus



- Can make any register transfer $R[i] \leftarrow R[j]$
- Can't have $G_i = G_j = 1$ for $i \neq j$
- Violating this constraint gives low resistance path from power supply to ground—with predictable results!

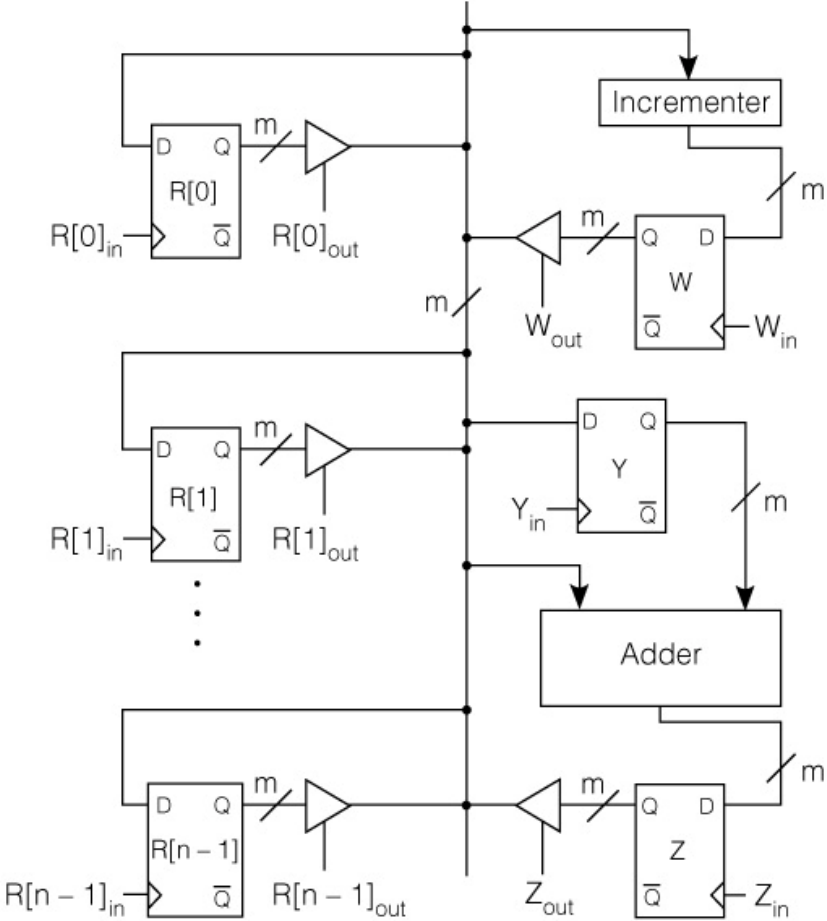
C
S
D
A
2/e

Fig. 2.24 Registers and Arithmetic Connected by One Bus

Example
Abstract RTN
 $R[3] \leftarrow R[1]+R[2];$

Concrete RTN
 $Y \leftarrow R[2];$
 $Z \leftarrow R[1]+Y;$
 $R[3] \leftarrow Z;$

Control Sequence
 $R[2]_{out}, Y_{in};$
 $R[1]_{out}, Z_{in};$
 $Z_{out}, R[3]_{in};$



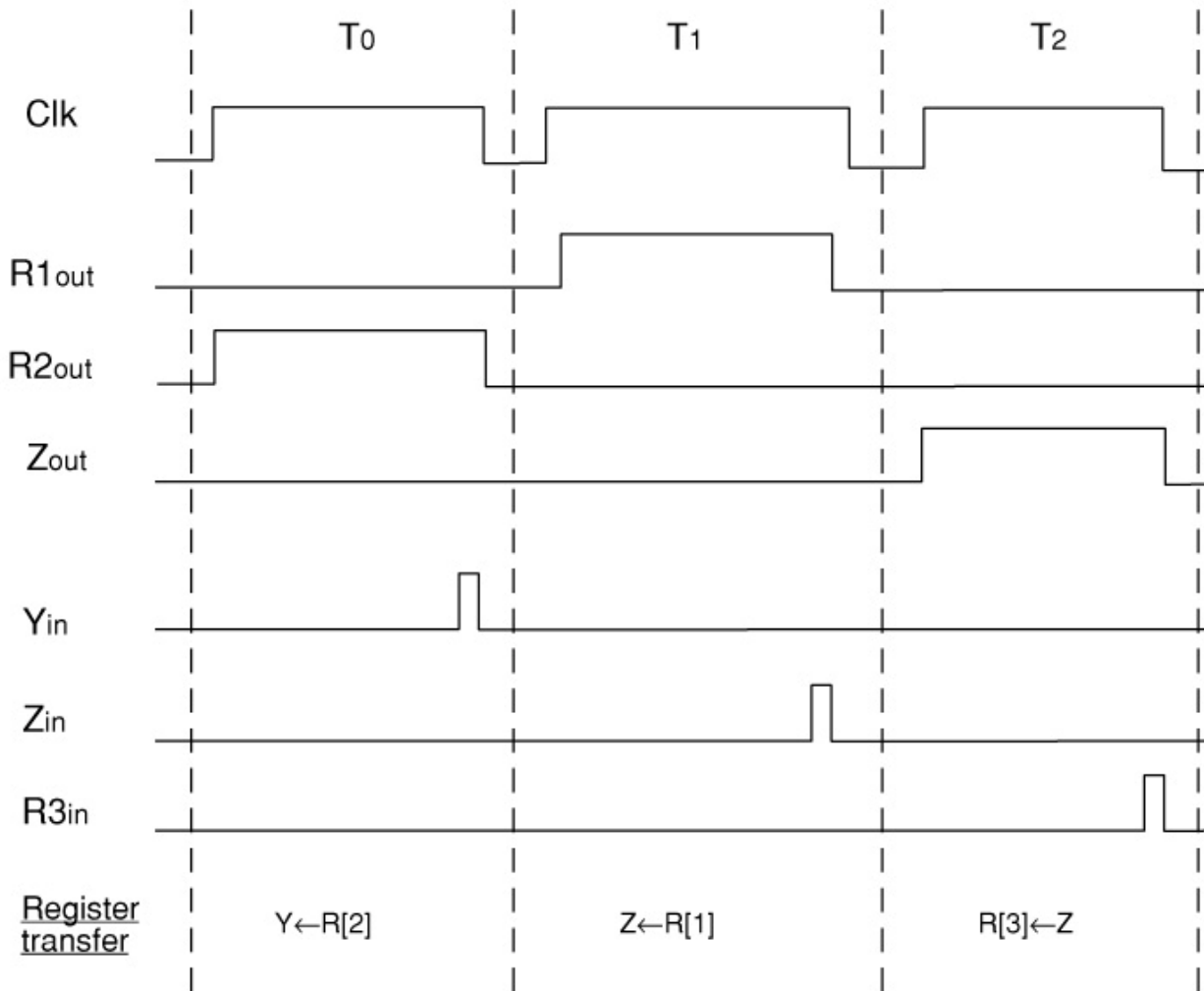
Combinational Logic—no memory

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Notice that what could be described in one step in the abstract RTN took three steps on this particular hardware

Figure 2.25 Timing of the Register Transfers

- Discuss: difference between gating signals and strobing signals
- Discuss factors influencing minimum clock period.



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C

S

D

A

2/e

RT's Possible with the One Bus Structure

- $R[i]$ or Y can get the contents of anything but Y
- Since result different from operand, it cannot go on the bus that is carrying the operand
- Arithmetic units thus have result registers
- Only one of two operands can be on the bus at a time, so adder has register for one operand
- $R[i] \leftarrow R[j] + R[k]$ is performed in 3 steps: $Y \leftarrow R[k]$; $Z \leftarrow R[j] + Y$; $R[i] \leftarrow Z$;
- $R[i] \leftarrow R[j] + R[k]$ is high level RTN description
- $Y \leftarrow R[k]$; $Z \leftarrow R[j] + Y$; $R[i] \leftarrow Z$; is concrete RTN
- Map to control sequence is: $R[2]_{out}, Y_{in}; R[1]_{out}, Z_{in}; Z_{out}, R[3]_{in};$



From Abstract RTN to Concrete RTN to Control Sequences

- The ability to begin with an abstract description, then describe a hardware design and resulting concrete RTN and control sequence is powerful.
- We shall use this method in Chapter 4 to develop various hardware designs for SRC

Chapter 2 Summary

- Classes of computer ISAs
- Memory addressing modes
- SRC: a complete example ISA
- RTN as a description method for ISAs
- RTN description of addressing modes
- Implementation of RTN operations with digital logic circuits
- Gates, strobos, and multiplexers